

## Correlation of diffusing photons and level crossing spectroscopy

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**Abstract** – We show that an enhanced intensity correlation shows up in the diffusion of photons multiply scattered by an atomic gas of large optical depth b. This enhancement occurs only for scattering atoms that are Zeeman degenerate and it leads to a deviation from the Rayleigh law. The fluctuations measured by their variance, display a resonance peak as a function of an applied magnetic field. The resonance width is proportional to the small factor 1/b. We derive closed analytic expressions for all these physical quantities which are directly accessible experimentally.

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We consider in this letter coherent multiple scattering of photons propagating in cold atomic gases. For Zeemandegenerate atoms, there is an enhancement of the fluctuations of light intensity (speckle pattern) transmitted through a gas of large optical depth, but without change of the average transmitted intensity [1]. This enhancement shows up in a significant deviation from the Rayleigh law which states that for classical scatterers without internal structure, the variance  $\overline{\delta T^2} = \overline{T^2} - \overline{T}^2$  of the transmission coefficient  $\mathcal{T}$  is related to its average value  $\overline{\mathcal{T}}$  by  $\overline{\delta \mathcal{T}^2} = \overline{\mathcal{T}}^2$ . The averaging over configurations denoted by  $\overline{\cdots}$  will be defined later. The enhancement results from the presence of additional cross-terms that involve the ground-state Zeeman sublevels of the atoms. The dependence of these cross-terms on magnetic quantum numbers suggests that it is sensitive to an applied magnetic field H. Our purpose in this letter is to show that indeed the amplified variance presents a resonance as a function of H around a crossing point, and the width of this resonance is

$$\Delta H \simeq a \frac{\hbar \Gamma}{g\mu_0} \frac{l}{L},\tag{1}$$

where l is the photon elastic mean free path through the atomic gas confined into a slab of width L, g is the Landé factor and  $\mu_0$  the Bohr magneton. Here, a is a constant of order unity to be determined later, that depends on the details of the atomic structure. All these features are obtained in the limit of diffusing photons, *i.e.*, in a regime where  $L \gg l$ . Thus, the narrowing of the resonance is in principle not limited, which might prove useful in level-crossing spectroscopic measurements.



Fig. 1: Experimental setup. A CW laser beam is incident onto atoms confined in a slab of width L. A detector placed along the direction  $\hat{\mathbf{s}}_b$ , records the intensity. During the time interval  $\tau$ , assumed to be short, the scatterers stay at rest. However, the two photons 1 and 2 experience different atomic internal configurations due to all other photons between them. The measurement is repeated after a time  $T \gg \tau$ .

We shall see that the effect we present here shares some kind of analogy with the well-known Franken or Hanle effects [2,3]. Nevertheless, we emphasize that both the underlying physical mechanisms and the quantities that are being measured are very different from these two effects [4,5].

We consider the setup of fig. 1. A photon of polarization  $\hat{\varepsilon}_a$  is incident along a direction  $\hat{\mathbf{s}}_a$  onto the atomic gas. It is detected in transmission with polarization  $\hat{\varepsilon}_b$ , along  $\hat{\mathbf{s}}_b$  after being multiply scattered. A time  $\tau$  later, a second identical photon is detected. We assume that  $\tau$  is short enough so that the atoms stay at rest between the two

events. The same measurement is repeated after a time  $T \gg \tau$ , during which the scatterers move. The averaging over spatial disorder results from this motion. The transmitted intensity  $\mathcal{T}$  is proportional to the probability of a photon incoming along  $\hat{\mathbf{s}}_a$ , to emerge along  $\hat{\mathbf{s}}_b$ . Atoms are modeled as degenerate two-level systems. We denote by  $|m_g\rangle$  the ground-state Zeeman sublevels with total angular momentum  $j_g$ ,  $|m_e\rangle$  are the excited states sublevels with total angular momentum  $j_e$ , and m is the projection on a quantization axis.

The average transmission coefficient  $\overline{\mathcal{T}}$  is obtained by squaring the sum of the scattering amplitudes,  $A_n^{\{R,m\}}$ , corresponding to a given configuration  $\{R,m\}$ . Here  $\{R\}$ accounts for the spatial positions of all atoms,  $\{m\}$  is a notation for their internal Zeeman states both before and after scattering and the index *n* denotes one possible multiple-scattering path. Then,

$$\overline{\mathcal{T}} = \overline{\left|\sum_{n} A_{n}^{\{R,m\}}\right|^{2}} = \sum_{nn'} \overline{A_{n}^{\{R,m\}} A_{n'}^{\{R,m\}*}}, \qquad (2)$$

where  $\overline{\cdots}$  denotes a configuration average over both  $\{R\}$  and  $\{m\}$ . When averaging over  $\{R\}$ , all cross-terms  $n \neq n'$  vanish because of large fluctuating phase shifts, so that  $\overline{\mathcal{T}} \simeq \sum_n \overline{|A_n^{\{m\}}|^2}$ . This expression is the leading approximation in the weak-disorder limit  $k_0 l \gg 1$ , where  $k_0$  is the photon wave number [6]. The two photons detected at t=0 and  $t=\tau$  are separated by many undetected photons (see fig. 1) which may change the internal states of atoms. Therefore, if  $\{m\}$  and  $\{m'\}$  refer to the atomic internal configuration seen by the two detected photons, then we can assume that there is no correlation between  $\{m\}$  and  $\{m'\}$ .

Similarly, the correlation function of the transmission coefficients  $\mathcal{T}$  and  $\mathcal{T}'$  of the two detected photons is

$$\overline{\mathcal{TT'}} = \sum_{ijkl} \overline{A_i^{\{R,m\}} A_j^{\{R,m\}*} A_k^{\{R,m'\}} A_l^{\{R,m'\}*}}.$$
 (3)

As before, the averaging over  $\{R\}$  leaves only pairs of amplitudes having exactly opposite phase shifts. Thus, to leading order in weak disorder, the only non-vanishing contributions involve two possible pairings of amplitudes, either  $i = j, \ k = l$ , which gives  $\overline{\mathcal{T}} \ \overline{\mathcal{T}'}$ , or  $i = l, \ j = k$ , so that defining  $C^2 = \overline{\mathcal{T}} \ \overline{\mathcal{T}'} - \overline{\mathcal{T}} \ \overline{\mathcal{T}'}$ , we obtain [1]

$$\mathcal{C}^{2} = \left| \sum_{i} \overline{A_{i}^{\{m\}} A_{i}^{\{m'\}*}} \right|^{2}.$$
(4)

Since generally  $\{m\} \neq \{m'\}$ , these cross-terms occur between distinct Zeeman sublevels of the *ground state*, unlike the Franken or Hanle effects, where the interference involves distinct *excited* sublevels.

In the theory of multiple scattering it is helpful to use a continuous description [6]. In this framework, one defines

two *Diffuson* functions  $\mathcal{D}^{(i,c)}$  by<sup>1</sup>

$$\overline{\mathcal{T}} = \int d\mathbf{r} d\mathbf{r}' \mathcal{D}^{(i)}(\mathbf{r}, \mathbf{r}') \quad \text{and} \quad \mathcal{C} = \left| \int d\mathbf{r} d\mathbf{r}' \mathcal{D}^{(c)}(\mathbf{r}, \mathbf{r}') \right|.$$
(5)

The two functions  $\mathcal{D}^{(i,c)}$  are obtained from an iteration equation (also called ladder diagram) whose structure is based on two elementary vertices  $\mathcal{V}^{(i,c)}$ , that describe the microscopic details of the scattering process. The iteration of the elementary vertices is written symbolically as

$$\mathcal{D} = \mathcal{V} + \mathcal{V}\mathcal{W}\mathcal{V} + \dots = \mathcal{V} + \mathcal{D}\mathcal{W}\mathcal{V}, \tag{6}$$

where  $\mathcal{D}$ ,  $\mathcal{V}$  stand for  $\mathcal{D}^{(i,c)}$ ,  $\mathcal{V}^{(i,c)}$ .  $\mathcal{V}$  accounts for a single scattering and  $\mathcal{DWV}$  represents its iteration. The quantity  $\mathcal{W}$  describes the propagation of the photon intensity between successive scattering events and it will be described later on.

Generally, the elementary vertex is obtained by coupling two scattering amplitudes. It is given by

$$\mathcal{V} = \sum_{m_i m_e m'_e} \frac{\langle m_2 | V(\hat{\varepsilon}_1, \hat{\varepsilon}_2) | m_1 \rangle \langle m_4 | V(\hat{\varepsilon}_3, \hat{\varepsilon}_4) | m_3 \rangle^*}{(\omega - \omega_{m_1 m_e} + i\frac{\Gamma}{2})(\omega - \omega_{m_3 m'_e} - i\frac{\Gamma}{2})}, \quad (7)$$

where the operator  $V(\hat{\varepsilon}', \hat{\varepsilon}) = \hat{\varepsilon}'^* \cdot \mathbf{d} |m_e\rangle \langle m_e | \mathbf{d} \cdot \hat{\varepsilon}$  results from the dipolar interaction energy  $-\mathbf{d} \cdot \mathbf{E}$  between atoms and photons.  $\mathbf{d}$  and  $\mathbf{E}$  are, respectively, the atomic-dipole and electric-field operators. The states  $|m_i\rangle$  are Zeeman sublevels of the atomic ground state, and  $|m_e\rangle$ ,  $|m'_e\rangle$  are those of the excited state. We have defined the energy difference  $\hbar \omega_{ij} = E_j - E_i$  and the photon frequency  $\omega$ . We assume that the ground-state Zeeman sublevels are equiprobable so that the corresponding density matrix reduces to the factor  $1/(2j_g + 1)$ .

The elementary vertex  $\mathcal{V}^{(i)}$ , that corresponds to the average intensity, is obtained by setting  $m_1 = m_3$ ,  $m_2 = m_4$ ,  $\hat{\varepsilon}_1 = \hat{\varepsilon}_3$  and  $\hat{\varepsilon}_2 = \hat{\varepsilon}_4$  in (7). Up to a proportionality factor,  $\mathcal{V}^{(i)}$  is nothing but the differential cross-section for this scattering process. Assuming a broad line excitation [7], we average  $\mathcal{V}^{(i)}$  over  $\omega$ , leading to [3]

$$\mathcal{V}^{(i)} = \sum_{m_1 m_2} \sum_{m_e m'_e} \frac{B_{12}(m_e) B^*_{12}(m'_e)}{i \,\omega_{m_e m'_e} + \Gamma},\tag{8}$$

where  $B_{12}(m_e) = \langle m_2 | \hat{\varepsilon}_2^* \cdot \mathbf{d} | m_e \rangle \langle m_e | \mathbf{d} \cdot \hat{\varepsilon}_1 | m_1 \rangle$ . A magnetic field removes the level degeneracy and leads to a Zeeman splitting, so that two kinds of terms appear in (8) depending on whether  $m_e = m'_e$  or  $m_e \neq m'_e$ . Terms for which  $m_e = m'_e$ , are independent of the magnetic field and give the incoherent scattering cross-section. The terms  $m_e \neq m'_e$  depend on the magnetic field and describe interferences between two distinct scattering amplitudes.

For the vertex  $\mathcal{V}^{(c)}$ , each of the two coupled scattering amplitudes in (7) might belong to a distinct atomic configuration (see (4)), meaning that we must consider distinct

<sup>&</sup>lt;sup>1</sup>All prefactors that depend on the geometry of the sample and on the strength and shape of the photon source have been absorbed in the definitions of  $\mathcal{D}^{(i,c)}$ .



Fig. 2: Example of a term which, for the transition  $j_g = 1 \rightarrow j_e = 2$ , contributes to  $\mathcal{V}^{(c)}$ , but not to  $\mathcal{V}^{(i)}$ . The solid and dashed lines refer, respectively, to the two quantum amplitudes that appear in (7). For large enough magnetic field, this contribution vanishes since Zeeman splitting takes it far from resonance.

couples of initial  $(|m_1\rangle, |m_3\rangle)$  and final  $(|m_2\rangle, |m_4\rangle)$ atomic states, as well as two initial  $(\hat{\varepsilon}_1, \hat{\varepsilon}_3)$  and final  $(\hat{\varepsilon}_2, \hat{\varepsilon}_4)$  polarization states. Summations over the quantum numbers  $m_i$  result from averaging over initial atomic states and from non-detected final states. The vertex  $\mathcal{V}^{(c)}$  involves more interference-like cross-terms than those already appearing in  $\mathcal{V}^{(i)}$ . A non-degenerate ground state leads immediately, using (7), to  $\mathcal{V}^{(i)} = \mathcal{V}^{(c)}$  so that we recover the Rayleigh law,  $\mathcal{C}^2 = \overline{\mathcal{T}} \, \overline{\mathcal{T}'}$  [6]. Degenerate states produce additional cross-terms in  $\mathcal{V}^{(c)}$  so that  $\mathcal{C}^2 > \overline{\mathcal{T}} \, \overline{\mathcal{T}'}$ (see fig. 2). An applied magnetic field removes the degeneracy and therefore affects the interference pattern.

We now calculate the Diffusons  $\mathcal{D}$  given by the iteration (6). We first decompose the various terms into components in a standard basis,

$$\mathcal{V} = \sum_{\alpha\beta\gamma\delta} (\hat{\varepsilon}_1)_{-\alpha} (\hat{\varepsilon}_2)^*_{\gamma} (\hat{\varepsilon}_3)^*_{-\beta} (\hat{\varepsilon}_4)_{\delta} \ \mathcal{V}_{\alpha\beta,\gamma\delta} \,. \tag{9}$$

Likewise, eq. (6) acquires a tensorial form,

$$\mathcal{D}_{\alpha\beta,\gamma\delta} = \mathcal{V}_{\alpha\beta,\gamma\delta} + W \sum_{\mu\nu\rho\sigma} \mathcal{D}_{\alpha\beta,\mu\nu} \mathcal{P}_{\mu\nu,\rho\sigma} \mathcal{V}_{\rho\sigma,\gamma\delta}.$$
 (10)

Here W describes the scalar part of W and  $\mathcal{P}_{\alpha\beta,\gamma\delta} = \langle (\delta_{\alpha\gamma} - (-)^{\gamma} \hat{s}_{\alpha} \hat{s}_{-\gamma}) (\delta_{\beta\delta} - (-)^{\beta} \hat{s}_{-\beta} \hat{s}_{\delta}) \rangle$  accounts for the polarization-dependent part. This follows at once by noticing that after being scattered by an atom, the two outgoing photon amplitudes propagate with a wave vector  $\hat{\mathbf{s}} = \mathbf{k}/k_0$ , random in direction but identical for both, and with two different polarization components. Since  $\hat{\mathbf{s}}$  is random, the intensity propagation is averaged  $\langle \cdots \rangle$  over photon wave vectors direction. The term  $\delta_{\mu\nu} - (-)^{\nu} \hat{s}_{\mu} \hat{s}_{-\nu}$  expresses transversality. The two tensors  $\mathcal{P}_{\alpha\beta,\gamma\delta}$  and  $\mathcal{V}_{\alpha\beta,\gamma\delta}$  can be written as  $9 \times 9$  matrices. The iteration (7) rewrites  $\mathcal{D} = (1 + W\mathcal{VP} + (W\mathcal{VP})^2 + \cdots)\mathcal{V}$ . We now use the spectral decomposition theorem to expand  $\mathcal{VP} = \sum_{K} u_K T^{(K)}$ , where  $u_K$ 's are the eigenvalues of  $\mathcal{VP}$  and the  $T^{(K)}$ 's define an orthonormal set of (generally) 9 projectors [1]. Then, with the help of (10), we find

$$\mathcal{D}_{\alpha\beta,\gamma\delta}^{(i,c)} = \sum_{K} U_{K}^{(i,c)} \left( \mathcal{V}_{K}^{(i,c)} \right)_{\alpha\beta,\gamma\delta} \tag{11}$$

with  $\mathcal{V}_{K}^{(i,c)} = T^{(K)}\mathcal{V}^{(i,c)}$  and

$$U_K^{(i,c)} \simeq \frac{8\pi c\Lambda}{3l^2} \frac{1/u_K^{(i,c)}}{\gamma_K^{(i,c)} + Dq^2},$$
(12)

where  $\Lambda = (2j_e + 1)/3(2j_g + 1)$  and **q** (with  $q = |\mathbf{q}|$ ) is the Fourier variable of the difference  $\mathbf{R} = \mathbf{r}' - \mathbf{r}$  between the two endpoints of a multiple-scattering sequence. The r.h.s. in (12) is obtained by using the diffusion approximation (*i.e.*  $ql \ll 1$ ), so that  $W(q) \simeq \frac{3}{2\Lambda}(1 - q^2l^2/3)$ , where D = cl/3 is the photon diffusion coefficient [6]. We identify the set of characteristic damping rates

$$\gamma_K^{(i,c)} = \frac{c}{l} \left( \frac{2\Lambda}{3u_K^{(i,c)}} - 1 \right).$$
 (13)

The term  $\frac{2}{3}\Lambda$  is the total cross-section conveniently normalized. According to the values of  $u_K^{(i,c)}$ , we identify 3 kinds of modes. A positive  $\gamma_K^{(i,c)}$  describes an exponentially damped mode. A vanishing  $\gamma_K^{(i,c)}$  corresponds to an infinite-range stable mode which ensures energy conservation, and a negative damping rate describes an amplified mode. The largest eigenvalue of  $\mathcal{V}^{(i)}\mathcal{P}$ is  $u_0^{(i)} = 2\Lambda/3$ , thus leading to one stable mode. For degenerate scatterers  $(j_g, j_e > 0)$ , and without magnetic field,  $\mathcal{D}^{(c)}$  has one amplified mode, whose occurrence results from the fact that all terms that contribute to  $\mathcal{V}^{(i)}$ , contribute also to  $\mathcal{V}^{(c)}$  [1]. However, there are interference terms that contribute to  $\mathcal{V}^{(c)}\mathcal{P}$  becomes greater than  $\frac{2}{3}\Lambda$ , thus making the corresponding damping rate negative.

We now rewrite (11) in real space,

$$\mathcal{D}^{(i,c)}(\mathbf{r},\mathbf{r}') = \sum_{K} Y_{K}^{(i,c)} \int_{0}^{\infty} \mathrm{d}t \ \mathcal{D}(\mathbf{r},\mathbf{r}',t) \ e^{-\gamma_{K}^{(i,c)}t}, \quad (14)$$

where  $Y_K^{(i,c)}$  are two angular functions that depend on the incoming and outgoing polarizations  $\hat{\varepsilon}_a$  and  $\hat{\varepsilon}_b$  [1]. The scalar Diffusion propagator  $\mathcal{D}(\mathbf{r}, \mathbf{r}', t)$  obeys a diffusion equation whose solution for a slab geometry is well known [6].

The dominant contribution to the average intensity  $\overline{\mathcal{T}}$  is the stable, energy conserving mode  $\gamma_0^{(i)} = 0$ . The two other modes have positive damping rates and are negligible compared to this stable mode. They express photon depolarization in multiple scattering. The stable mode leads to  $\overline{\mathcal{T}} \propto l/L = 1/n\sigma L$ . Here *n* is the density of scatterers and  $\sigma$  is the single-scattering total cross-section. However, the total cross-section is independent of the magnetic field *H* [3]. This can be understood as follows. Starting from (8), the outgoing polarization-dependent part is a sum of terms like  $\sum_{\hat{\varepsilon}_2 \perp \mathbf{k}} \langle m_2 | \hat{\varepsilon}_2^* \cdot \mathbf{d} | m_e \rangle \langle m'_e | \hat{\varepsilon}_2 \cdot \mathbf{d} | m_2 \rangle =$  $\sum_{\mathbf{k}} (\varepsilon_{2\alpha} \varepsilon_{2\beta} + \varepsilon'_{2\alpha} \varepsilon'_{2\beta}) \langle m_2 | d_\alpha | m_e \rangle \langle m'_e | d_{-\beta} | m_2 \rangle$ , where **k** is the outgoing wave vector, and  $(\alpha, \beta)$  are the standard components of **d** that contribute to the transitions. Integrating over **k** imposes  $\alpha = -\beta$ , which implies  $m_e = m'_e$ .



Fig. 3: Plot of C given by (15) as a function of the dimensionless magnetic field s. We denote by  $\Delta$  its FWHM. This plot corresponds to the  $j_g = 1 \rightarrow j_e = 2$  transition and b = 5.

Thus, the interference terms in (8) do not contribute to  $\sigma$ , which is therefore independent of H. As a consequence,  $\overline{\mathcal{T}}$  is also independent of *H*. On the other hand, one cannot take advantage of the preceding argument when considering the generalized vertex (7). In that case, the corresponding differential and total cross-sections depend strongly on H. Moreover, the transitions that contribute to  $\mathcal{V}^{(c)}$  but not to  $\mathcal{V}^{(i)}$  (fig. 2) involve essentially a change in the Zeeman sublevels of atoms (Raman transitions). In a strong enough magnetic field, such transitions are suppressed. The field is thus expected to reduce  $\mathcal{V}^{(c)}$ , and consequently the correlation  $\mathcal C$  . It is shown below that it is indeed the case. It is nevertheless worth noticing that for a monochromatic light, the total intensity cross-section does depend on H, but still this dependence is much weaker than for the correlation.

The intensity correlation function C is dominated by the amplified mode driven by the negative damping rate  $\gamma_0^{(c)}$ . The integral in (14) is cutoff by  $t_{max} = \mathcal{L}/c$ , where  $\mathcal{L} = cL^2/D$  is the longest path of a diffusing photon. Expression (14) thus leads to [1]

$$\mathcal{C} = Y_0^{(c)} \left( \frac{\sin^2(\frac{X}{b})}{X \sin X} - 2\sin^2\left(\frac{\pi}{b}\right) \frac{e^{-\pi^2 + X^2}}{\pi^2 - X^2} \right).$$
(15)

We have defined  $X = L/L_0^{(c)}(s)$ , where  $L_0^{(c)}(s) = \sqrt{D/\gamma_0^{(c)}(s)}$  is expressed as a function of the dimensionless magnetic field  $s = g\mu_0 H/\hbar\Gamma$  and b = L/l is the optical depth. This expression is displayed in fig. 3. It retains the shape of a resonance curve whose FWHM is given by (1). To derive it and to obtain X(s), we expand  $\mathcal{V}^{(c)}(s)$  to first order in s, leading for the amplified mode to  $u_0^{(c)}(s) \simeq u_0^{(c)}(0) - \beta s^2$ , where  $\beta$  is a constant that depends on the specific scattering atom. According to (13), the corresponding damping rate becomes

$$\gamma_0^{(c)}(s) \simeq \gamma_0^{(c)}(0) + \frac{2\beta c \Lambda}{3u_0^{(c)2} l} s^2.$$
 (16)



Fig. 4: FWHM  $\Delta$  of C plotted vs. 1/b. The points are obtained from (15) in which  $f_2$  results from a direct numerical calculation of  $\gamma_0^{(c)}(s)$ . The slope of this linear behavior is in good agreement with the predicted expression  $2\sqrt{\ln 2/f_2} \simeq 0.76$  obtained for the transition  $j_g = 1 \rightarrow j_e = 2$ .

By rewriting  $X = b\sqrt{l^2\gamma_0^{(c)}(s)/D}$ , and making use of (16), we obtain  $X = b\sqrt{|f_0 - f_2 s^2|}$ , where the two constants  $f_0$  and  $f_2$  are given by  $f_0 = (2\Lambda/u_0^{(c)}) - 3$  and  $f_2 = 2\Lambda\beta/u_0^{(c)2}$ . For large enough optical depth b = L/l, *i.e.*, in the diffusive regime where expression (15) applies, the FWHM  $\Delta$  behaves linearly with 1/b as shown in fig. 4. The corresponding slope is easily calculated from (15) and restoring units, we obtain for  $\Delta H$  the expression (1) with  $a = 2\sqrt{\ln 2/f_2}$ .

To summarize, we have shown that in multiple scattering of diffusing photons scattered by atoms, the presence of a magnetic field near a level crossing (or close to zero field) shows up as a resonance peak in the intensity correlation function C. Its width, given by (1), is inversely proportional to the optical depth b = L/l. The diffusive regime corresponds to large values of b(typically  $b \simeq 10^2$ ), so that the sensitivity of the interference to a magnetic field is significantly enhanced. This could be used towards more precise measurements in level crossing spectroscopy, in the limit of dense atomic gases where multiple scattering cannot be neglected anymore.

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## REFERENCES

- ASSAF O. and AKKERMANS E., Phys. Rev. Lett., 98 (2007) 083601.
- [2] ARIMONDO E. et al., Rev. Mod. Phys., 49 (1977) 31;
   COHEN-TANNOUDJI C., Optical Pumping and Interaction

of Atoms with the Electromagnetic Field, Cargèse Lect. Phys., edited by LÉVY M. (Gordon and Breach) 1968.

- [3] FRANKEN P. A., Phys. Rev., **121** (1961) 508; ROSE M. E. and CAROVILLANO R. L., Phys. Rev., **122** (1961) 1158.
- [4] BARRAT J. P., J. Phys. Radium, 20 (1959) 633; OMONT A., J. Phys. Radium, 26 (1965) 576.
- [5] SERIES G. W. et al., Proc. R. Soc. London, Ser. A, 293 (1966) 70.
- [6] AKKERMANS E. and MONTAMBAUX G., Mesoscopic Physics of Electrons and Photons (Cambridge University Press) 2007; J. Opt. Soc. Am. B, 21 (2004) 101.
- [7] The broad band assumption is only for convenience. For weak enough magnetic fields, both broad band and monochromatic waves give similar results for the intensity. For more details see RASMUSSEN W. et al., Opt. Commun., 12 (1974) 315 and [1].