

# Multi-bit magnetic memory using $\text{Fe}_8$ high spin molecules

Oren Shafir

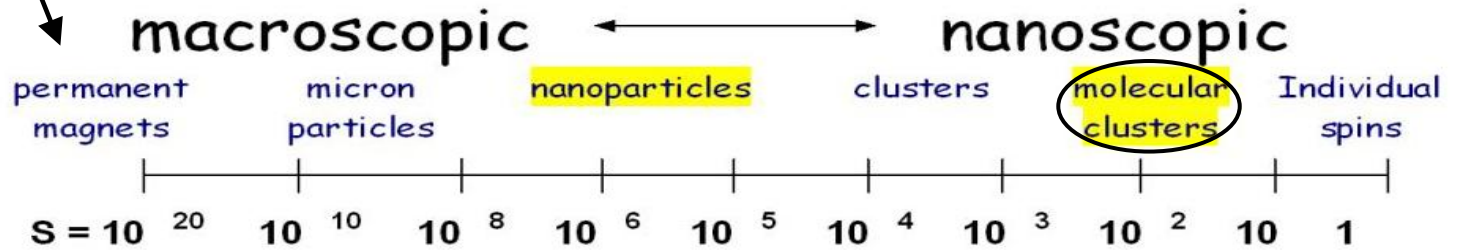
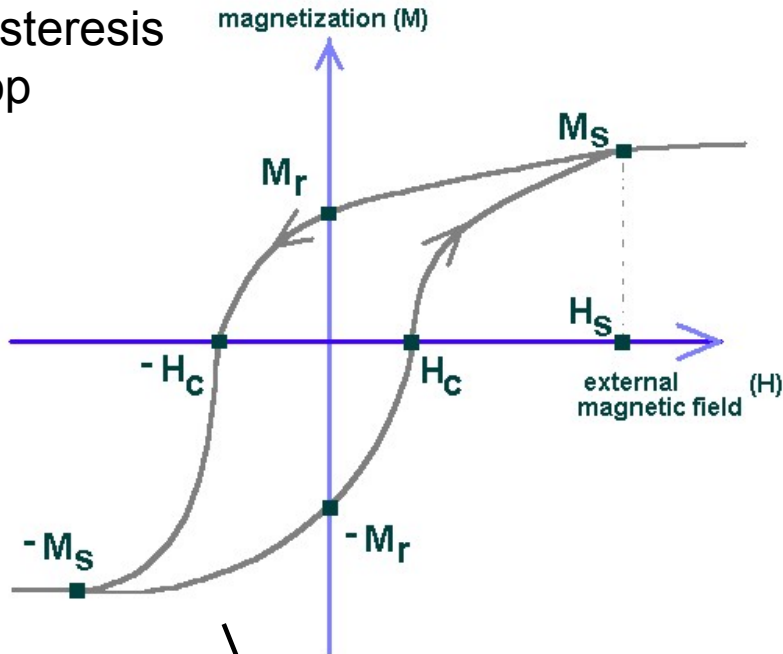
Magnetism Group, Physics Department

# Outline

- **Preface: memory unit**
- **Fe<sub>8</sub> as a high spin molecule**
- **Quantum tunneling In Fe<sub>8</sub>**
- **Experiments:**
  - **Faraday force magnetometer**
  - **$\mu$ SR**
- **Discussion**
- **Summary**

# The “memory” of a memory unit

Hysteresis loop

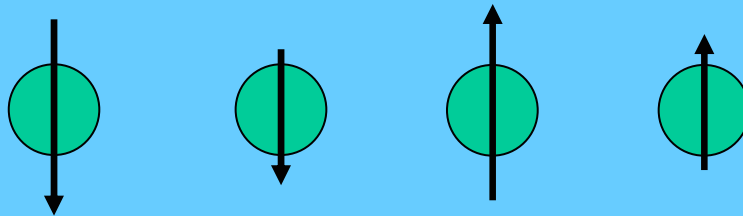


# What do we mean by multi-bit memory?

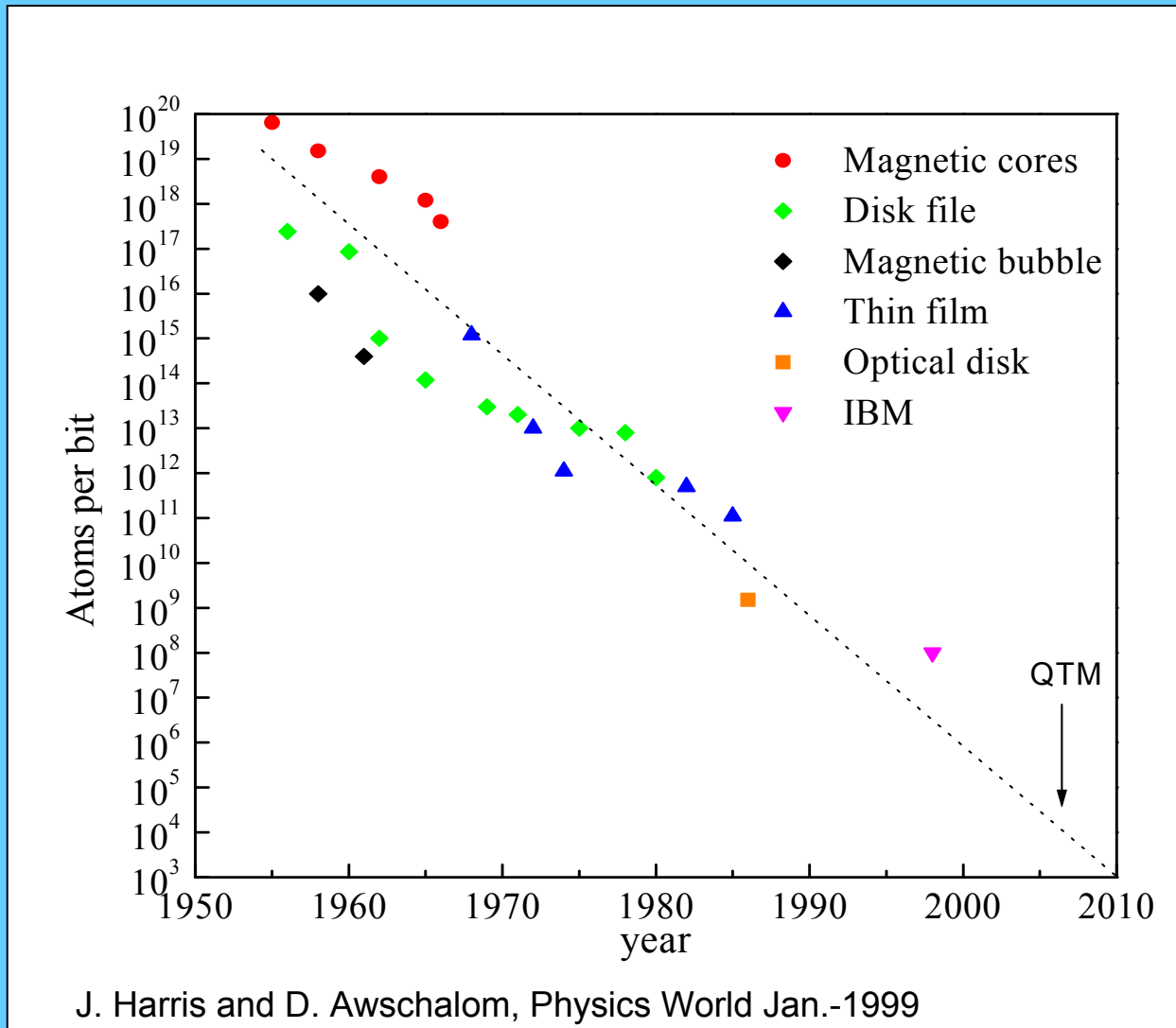
- **Single-bit Memory** → using the same measurement one can distinguish between two different preparation processes.



- **Multi-bit Memory** → using the same measurement one can distinguish between more than two preparation processes.



# Memory Unit Evolution



# Outline

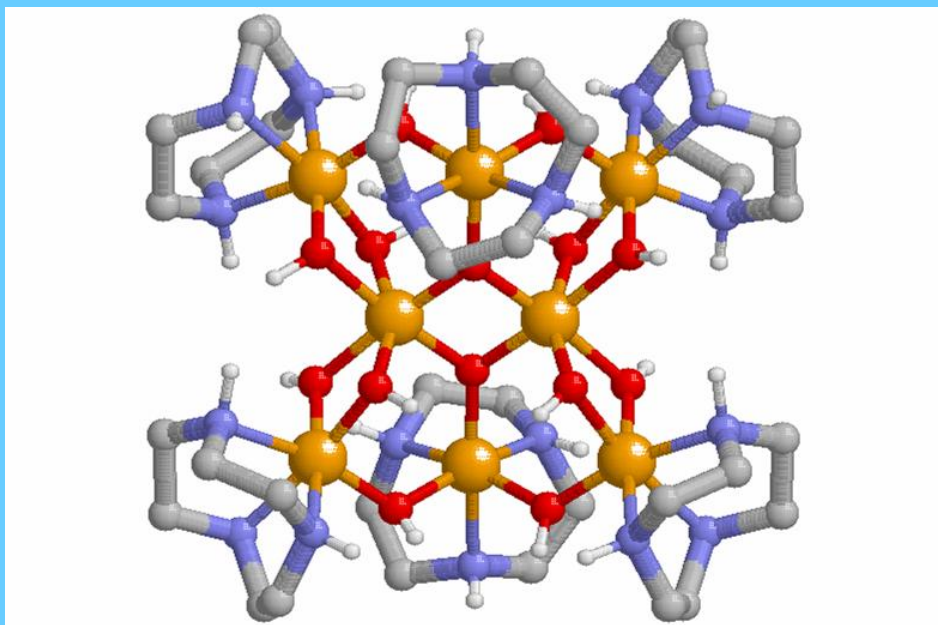
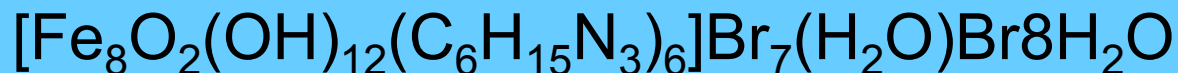
- Preface: memory unit
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# Molecules as magnetic memory

There are some properties that molecules must have if one wants to use them as magnetic memory:

- Existence of an hysteresis loop (energy barrier between two magnetization states) = the molecule can “remember”.
- Large interaction between the spins in the molecule ( $J$ ) = the molecule acts as a single unit.
- Weak magnetic coupling between the molecules = every molecule behaves independently.

# Fe<sub>8</sub> Molecule



- Iron
- Oxygen
- Nitrogen
- Carbon
- Hydrogen

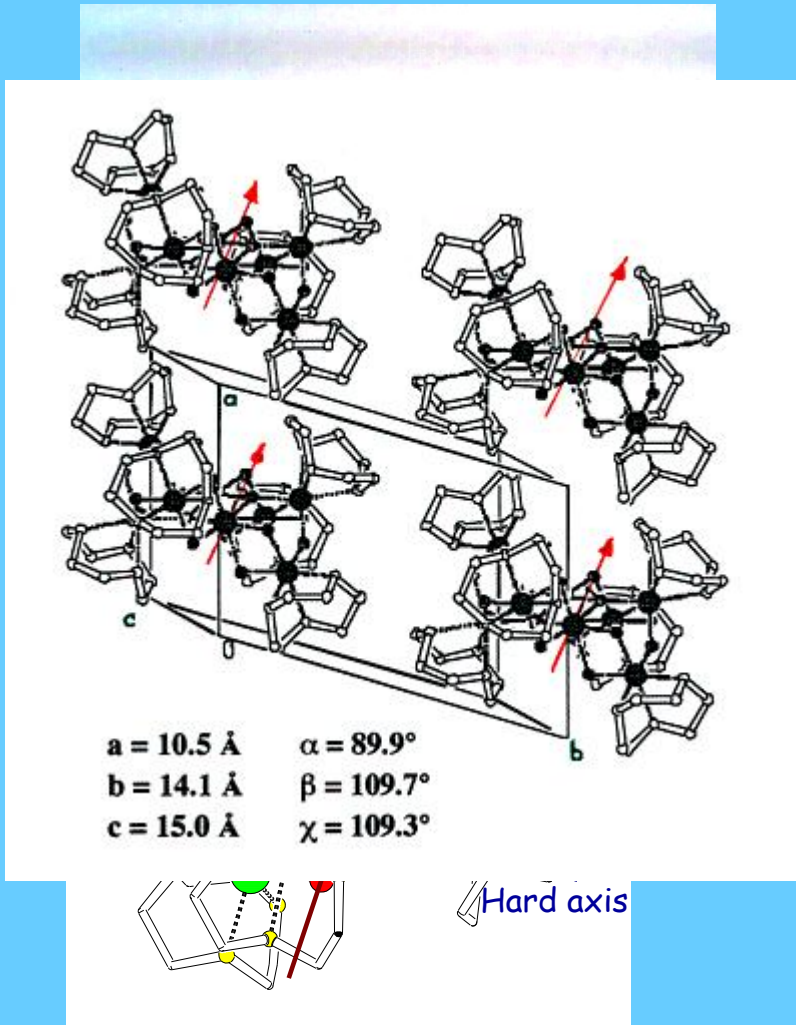
K. Wieghardt, K. Pohl,  
I. Jibril and G. Huttner,  
*Angew. Chem. Int. Ed.*  
*Engl.* 23 (1984), 77.

- The magnitude of magnetic interactions between the spins of the ions is between 20 to 170K.
- The magnetic interactions between the molecules are negligibly small.

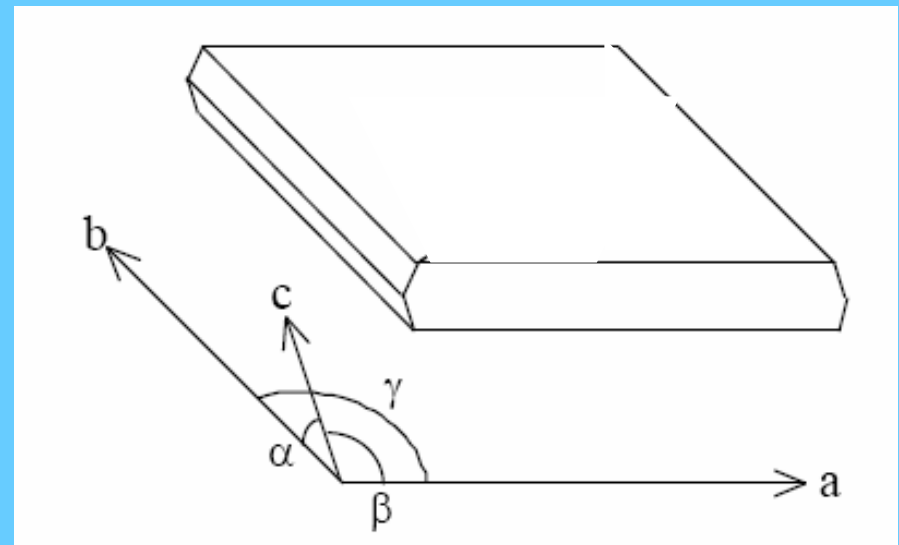


# Single crystal of Fe8

- Single array of nanomagnets

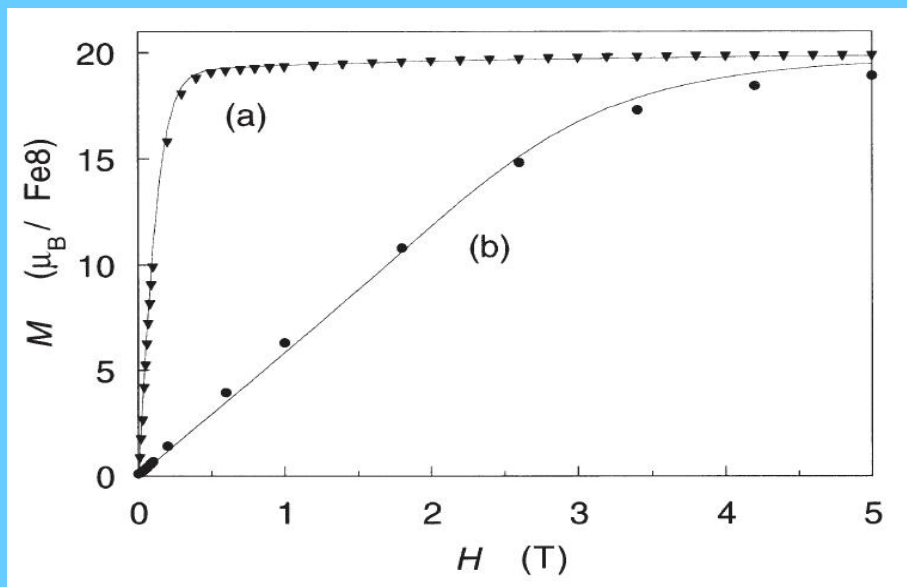


The magnetization is preferentially oriented parallel to an axis called the "easy axis".

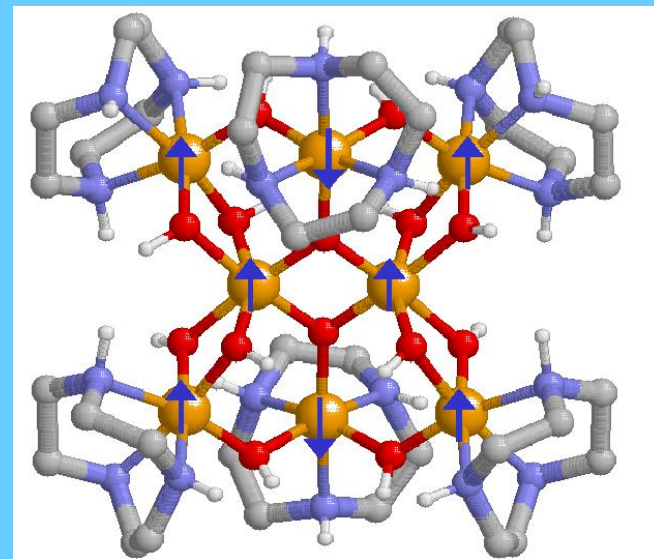


$a = 10.5 \text{ \AA}$	$\alpha = 89.9^\circ$
$b = 14.1 \text{ \AA}$	$\beta = 109.7^\circ$
$c = 15.0 \text{ \AA}$	$\chi = 109.3^\circ$

# The molecular spin in low temperatures



$S=10$



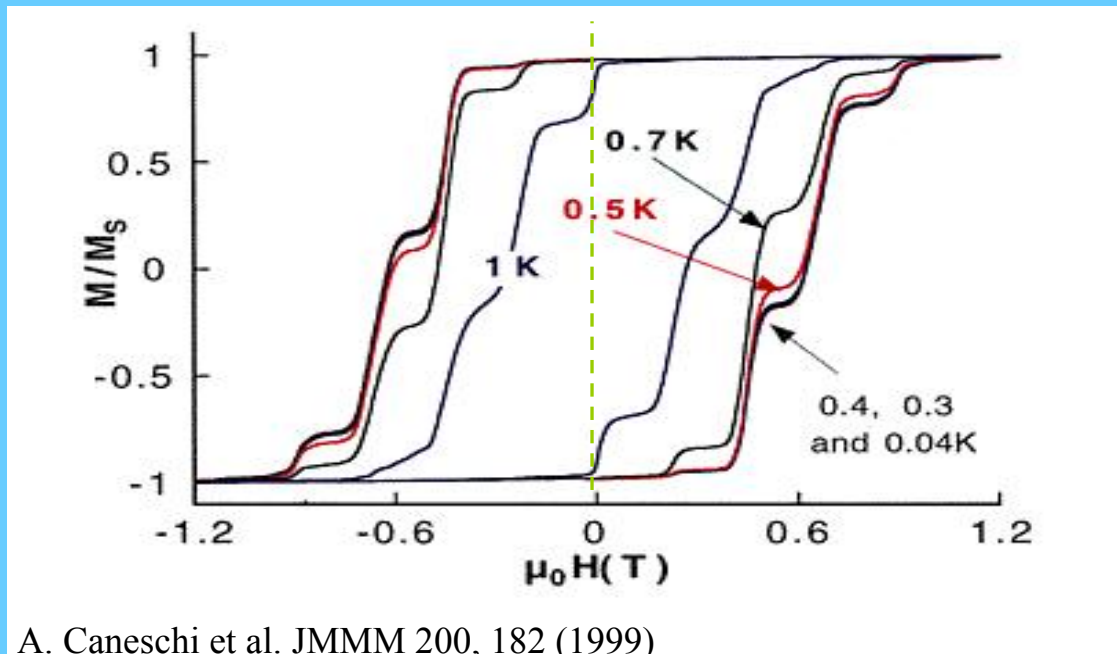
- (a) is parallel to the easy axis.
- (b) is perpendicular to the easy axis.

M. Ueda & S. Maegawa, J. Phys. Soc. Jpn. 70 (2001)

$$S = 6 \times \left(\frac{5}{2}\right) + 2 \times \left(-\frac{5}{2}\right) = 10$$

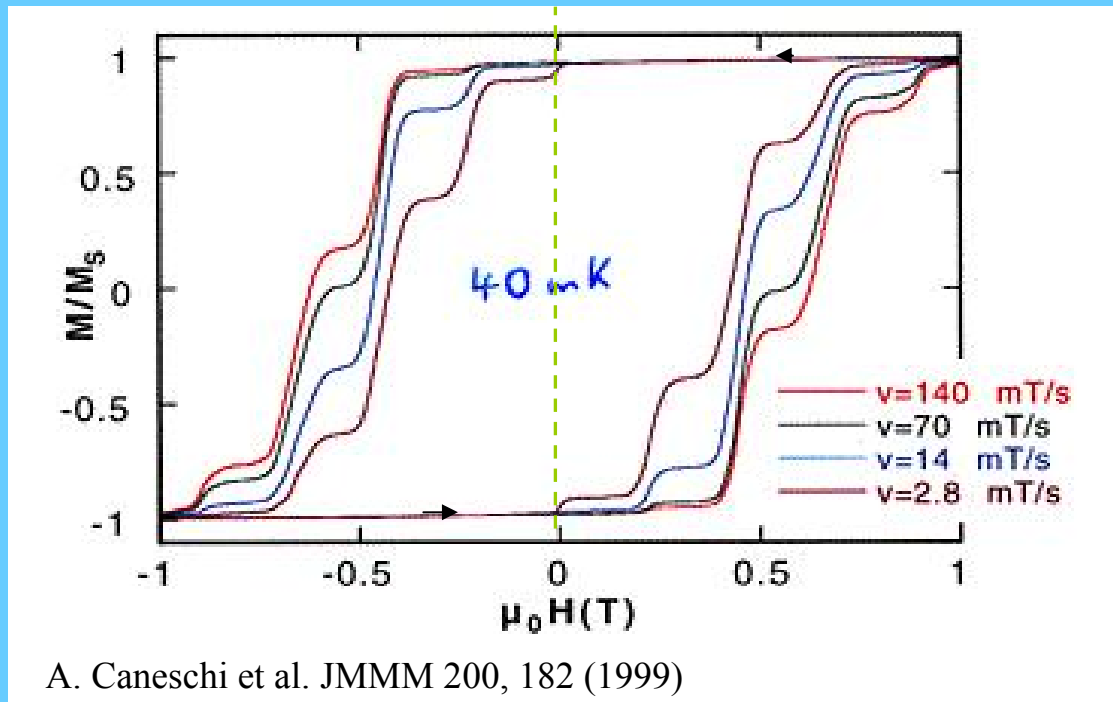
This was confirmed by a polarized neutron-diffraction experiment.

# Hysteresis loop of Fe8 – Temperature dependence



- There is a temperature dependence above 0.4K.
- Equally separated steps can be seen at  $H_m \approx n \times 0.22T$
- The lower the temperature, the wider the hysteresis loop

# Hysteresis loop of Fe8 – sweeping rate dependence



- Equally separated steps can be seen at  $H_m \approx n \times 0.22T$
- Fast sweeping rate  $\rightarrow$  wider hysteresis loop

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# The concept of tunnel splitting: $S = 1$

$$\mathcal{H} = -DS_z^2 + E(S_x^2 - S_y^2) = \begin{pmatrix} -D & 0 & E \\ 0 & 0 & 0 \\ E & 0 & -D \end{pmatrix} \quad |up\rangle = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} \quad |middle\rangle = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \quad |down\rangle = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

Energy levels with  $E=0$

0

-D double degenerate

Energy levels with  $E \neq 0$ .

0

-D+E

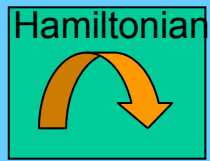
-D-E

$\Delta=2E$

$$\left| \langle down | \exp(-i\mathcal{H}t) | up \rangle \right|^2 = \frac{1 - \cos(2Et)}{2} = \frac{1 - \cos(\Delta t)}{2}$$

14 The spin will tunnel at a rate given by  $\Delta$  from up to down.

# The Hamiltonian of Fe8: S=10



The main part of the spin Hamiltonian:

$$\mathcal{H} = -DS_z^2 - g\mu_B H_z S_z - E \cdot (S_x^2 - S_y^2)$$

D – anisotropic constant ( $\sim 0.27$  K)

E – rhombic parameter ( $\sim 0.046$  K)

The energy levels are:

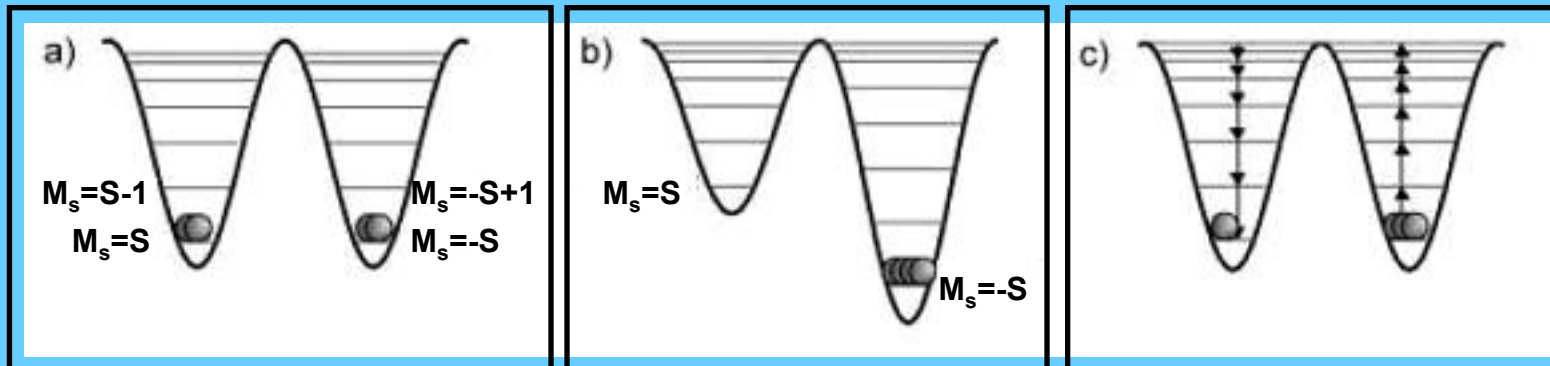
$$\text{Energy}(m) = -Dm^2 - g\mu_B H_z m$$

where  $m$  is the quantum number of the level.

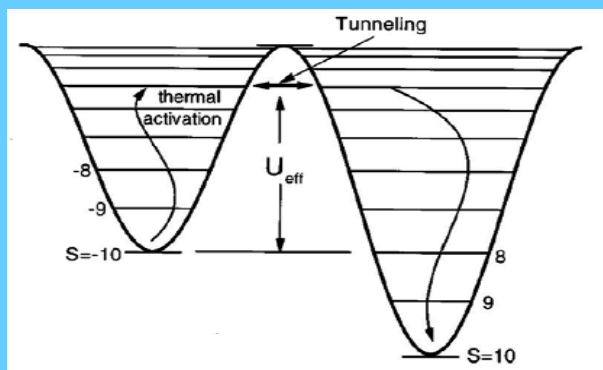
The tunnel splitting between the two degenerated ground states:

$$\Delta_{-S,S} = \frac{8D}{[(S-1)!]^2} (2S)! \left( \frac{E}{8D} \right)^S$$

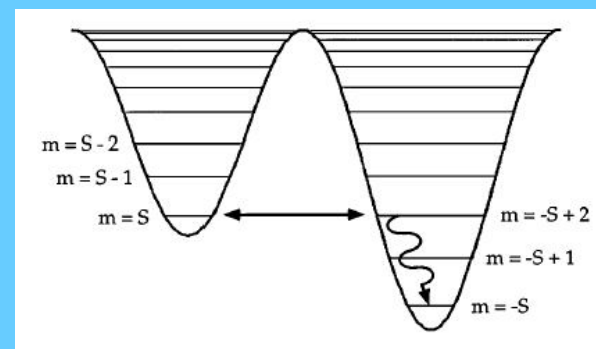
# Experimental realization



- a) In zero field the two wells are equally populated.
- b) An applied magnetic field selectively populates the right well.
- c) After removing the field the system returns to equilibrium (thermally).



Thermally assisted QT

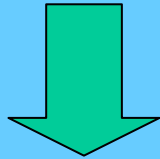


pure QT

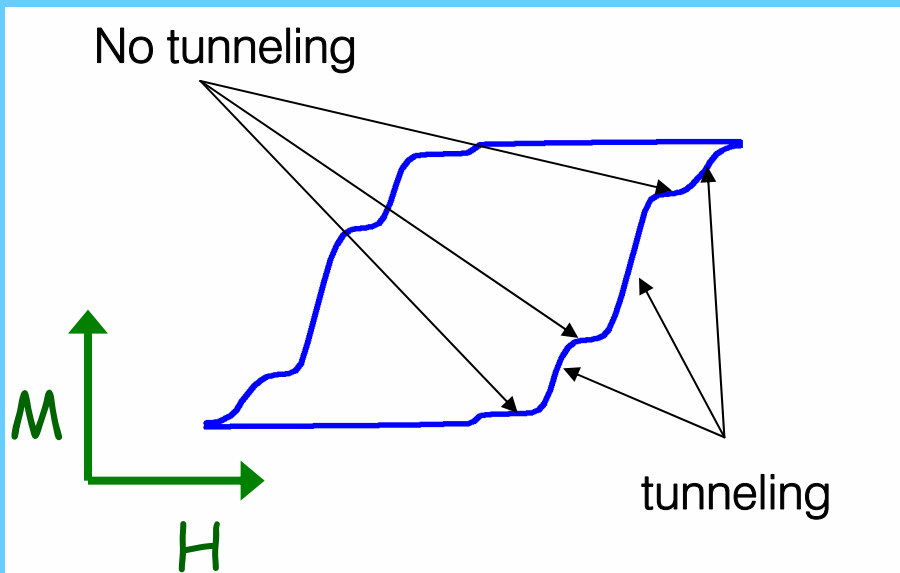
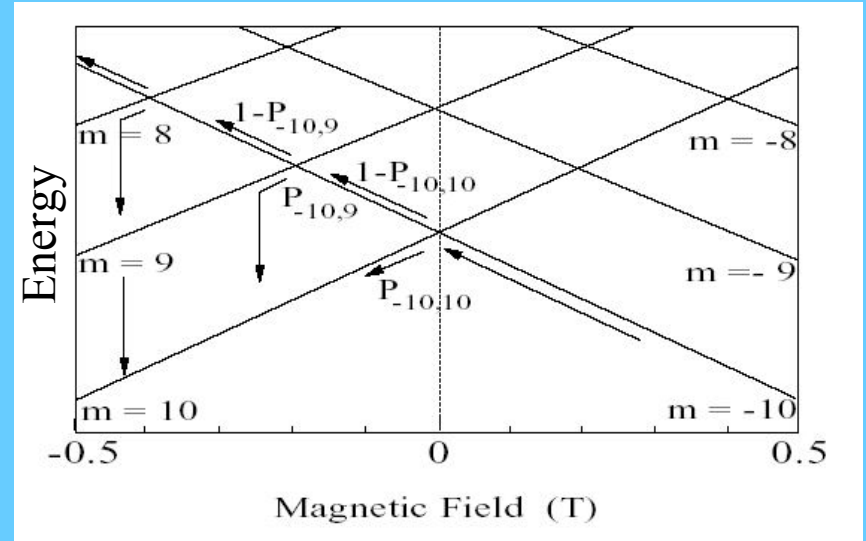


# The model and the hysteresis loop

$$\mathcal{H} = -DS_z^2 + E(S_x^2 - S_y^2) - g\mu_B \mathbf{S} \cdot \mathbf{H}$$



$$H_m(n) = \frac{nD}{g\mu_B} \approx n \times 0.22T.$$



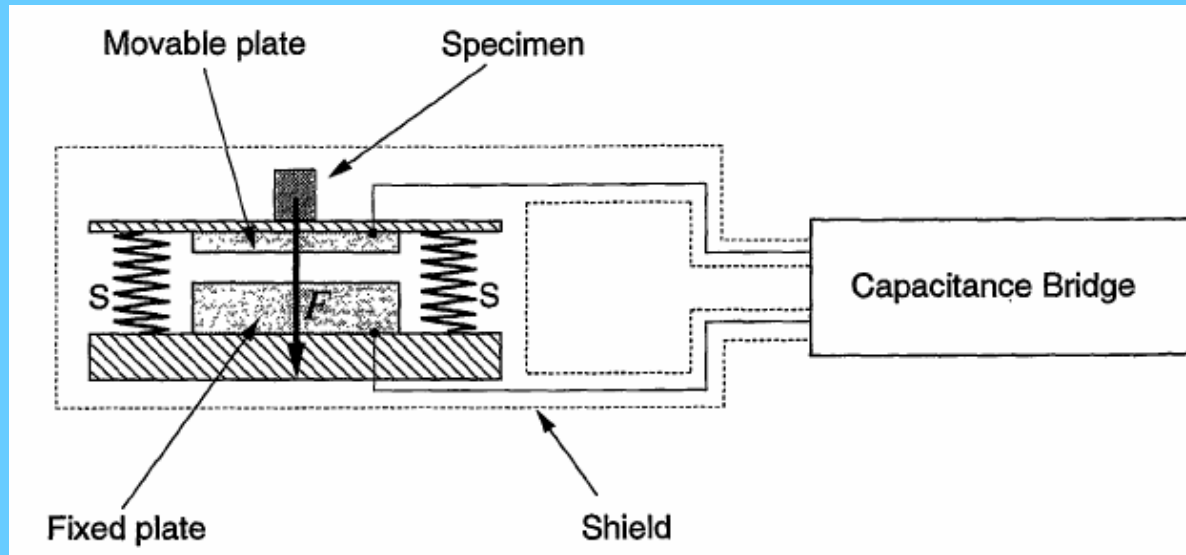
## Landau Zener model

$$P_{m,m'} = 1 - \exp\left[-\frac{\pi\Delta_{m,m'}^2}{2\hbar g\mu_B |m-m'| dH/dt}\right]$$

# Outline

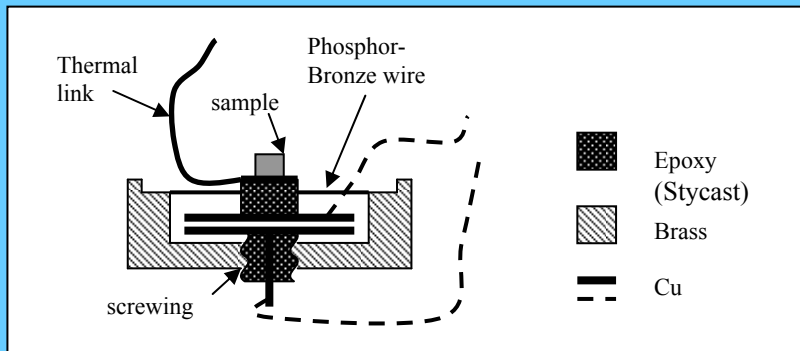
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# Faraday force magnetometer – Principle of measurement



- Measuring the varying capacitance.
- spatially varying magnetic field  $\rightarrow$  magnetic force  $\mathbf{F} = (\mathbf{M} \cdot \nabla)\mathbf{B}$
- The restoring force of the springs balances  $F$  .

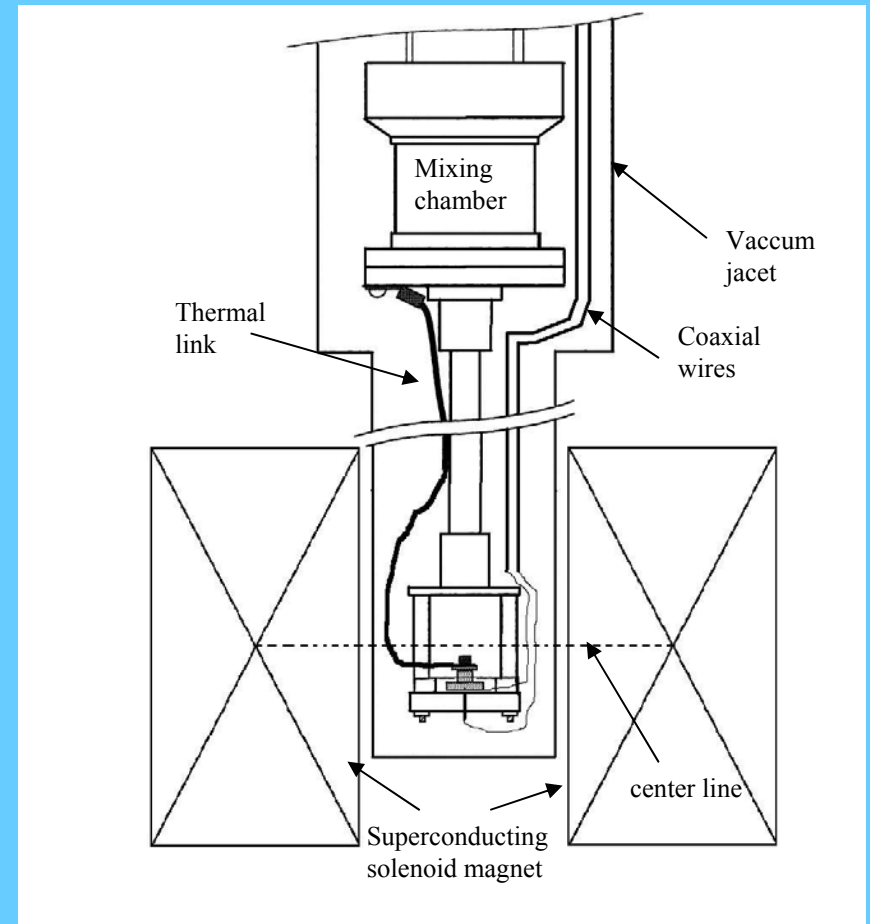
# Faraday force magnetometer – The load cell



The movable plate is suspended by four wires of phosphor bronze.

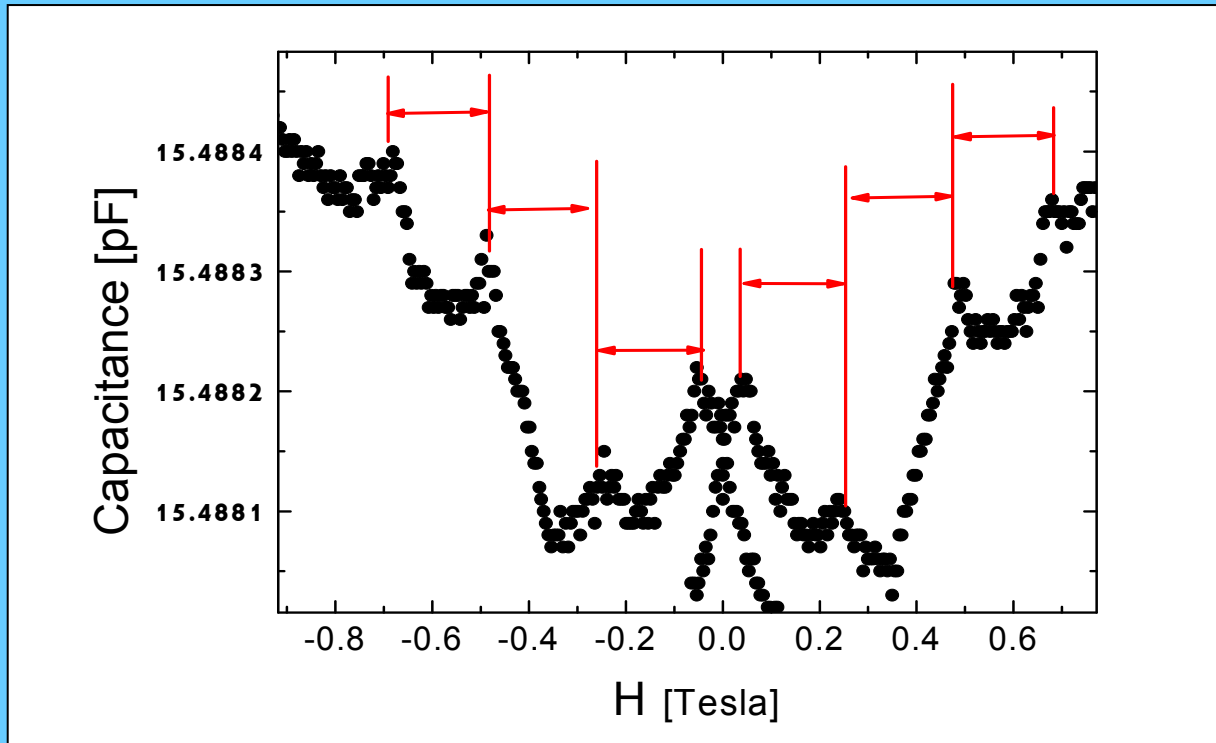
$$C_0^{-1} - C^{-1} = a \cdot M_z \frac{dB_z}{dz}$$

$a$  – Calibration constant



The load cell device, displaced from the center of a solenoid magnet in a dilution refrigerator.

# Results - jumps in matching fields



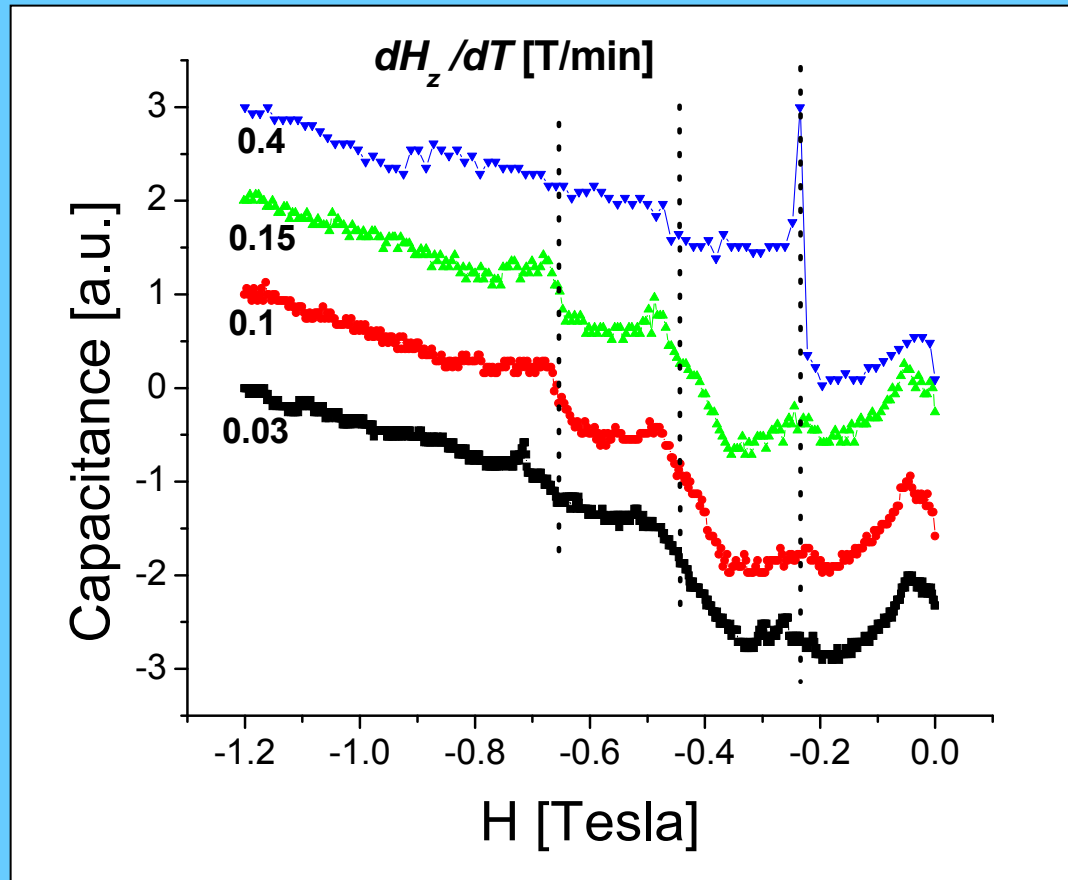
The capacitance versus the magnetic field

( $dH/dt = 0.15$  T/min ,  $T = 40$  mK)

The distance between steps is nearly constant

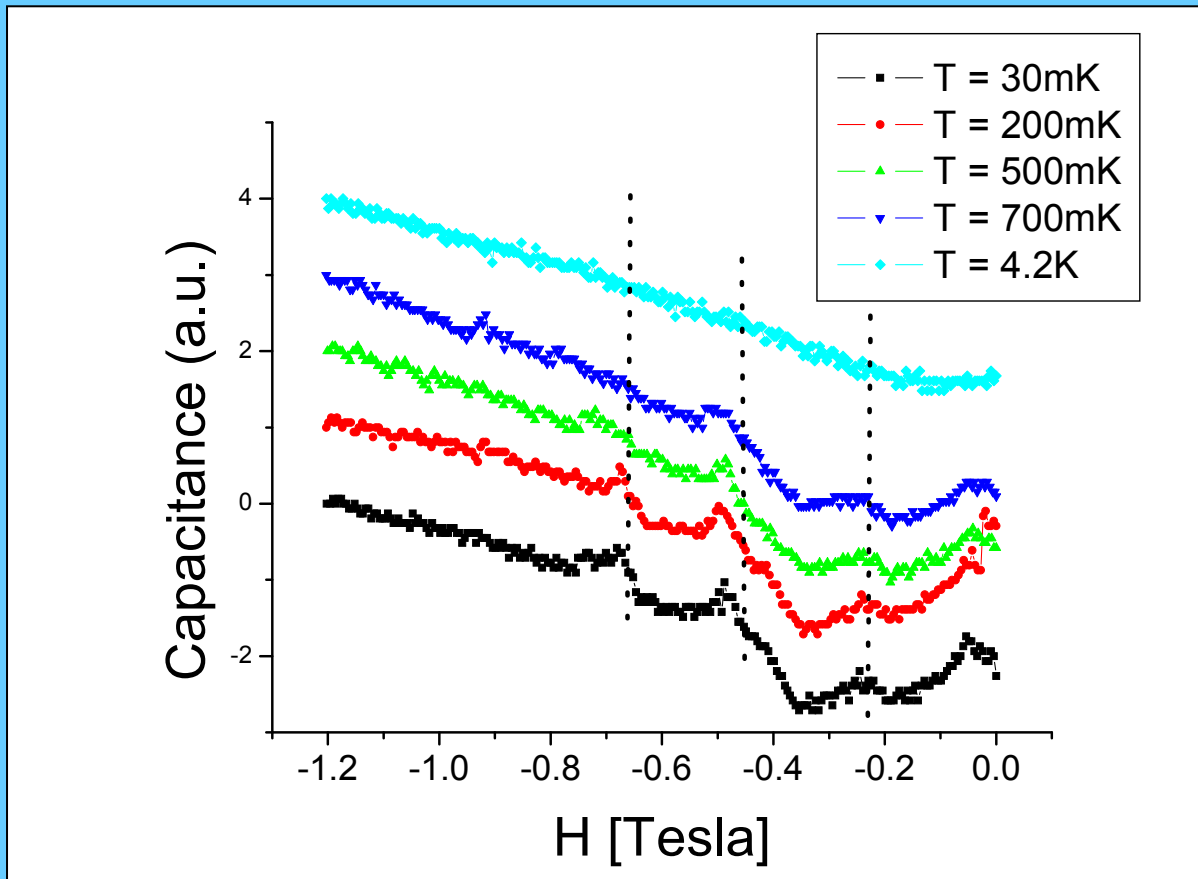
(the arrows are of equal length)

# Sweep rate dependence



Capacitance in arbitrary units for various  $dH_z/dt$  (at  $T=40mK$ ). The vertical dotted lines are at the approximate matching fields  $H_m \approx n \times 0.21T$ .

# Temperature dependence



Capacitance in a.u. for different temperatures ( $dH_z/dt=0.15$  [T/min]). The vertical dotted lines are at the approximate matching fields  $H_m \approx n \times 0.21$  T

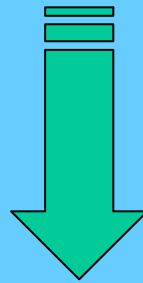
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# Why measure Fe8 with $\mu$ SR?

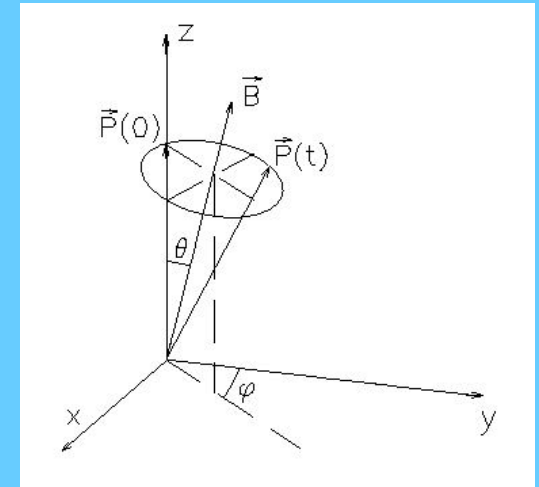
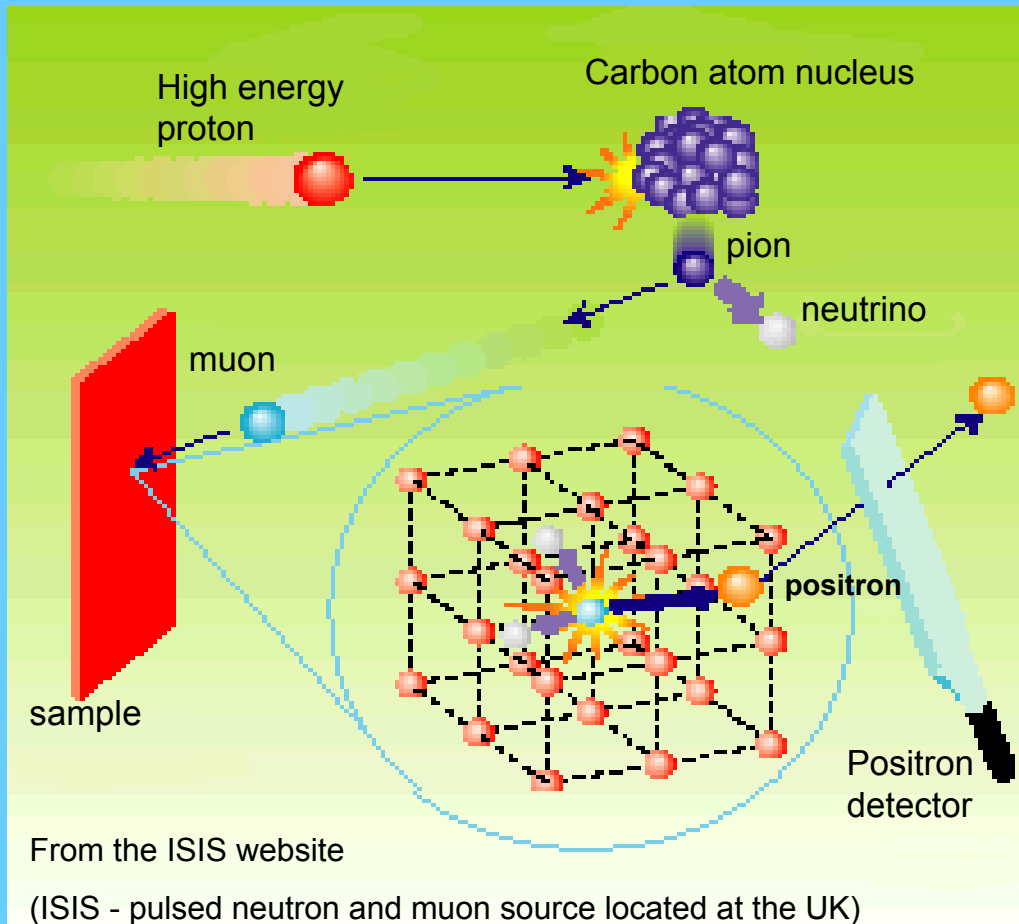
We want to measure the magnetization of a few (or one) molecules



We need a **local probe**

Moreover, there is an ongoing effort to make Fe8 films →  $\mu$ SR is applicable to films (while most techniques are not).

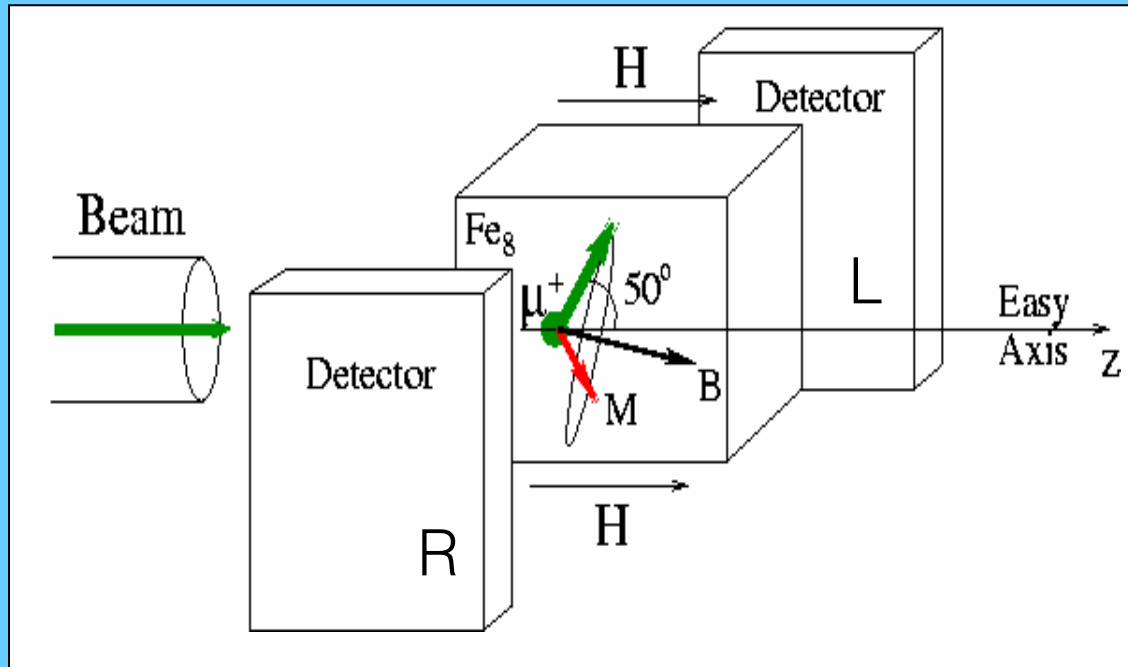
# $\mu$ SR – Muon Spin Relaxation/Rotation



The muon provides information on the magnetic environment in its vicinity.

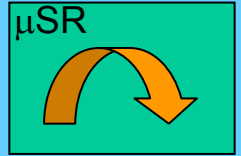
$$\omega_{\mu} = \gamma_{\mu} \cdot \vec{B}$$

# $\mu$ SR experiment setup



- The beam direction  $\parallel$  easy axis of Fe8  $\parallel$  applied field.
- Temperature :  $\sim 100\text{mK}$  (minimize activation effects).
- The initial polarization of the muons is  $50^\circ$  relative to z.

# Asymmetry

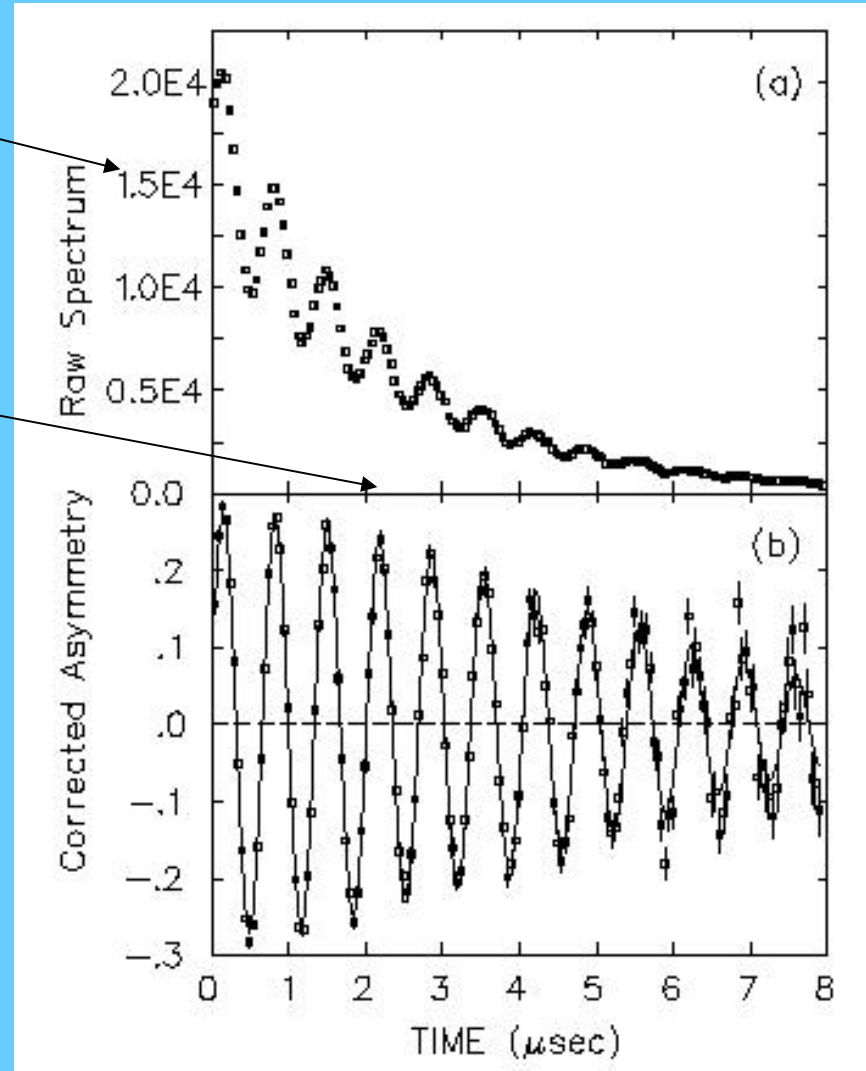


Detected positrons

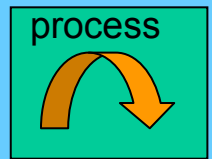
time difference between the  
muon arrival at the sample and  
its decay

Corrected asymmetry:

$$A(t) = \frac{R(t) - L(t)}{R(t) + L(t)} \propto P_{\perp}(t)$$



# The process - three step field cycle:



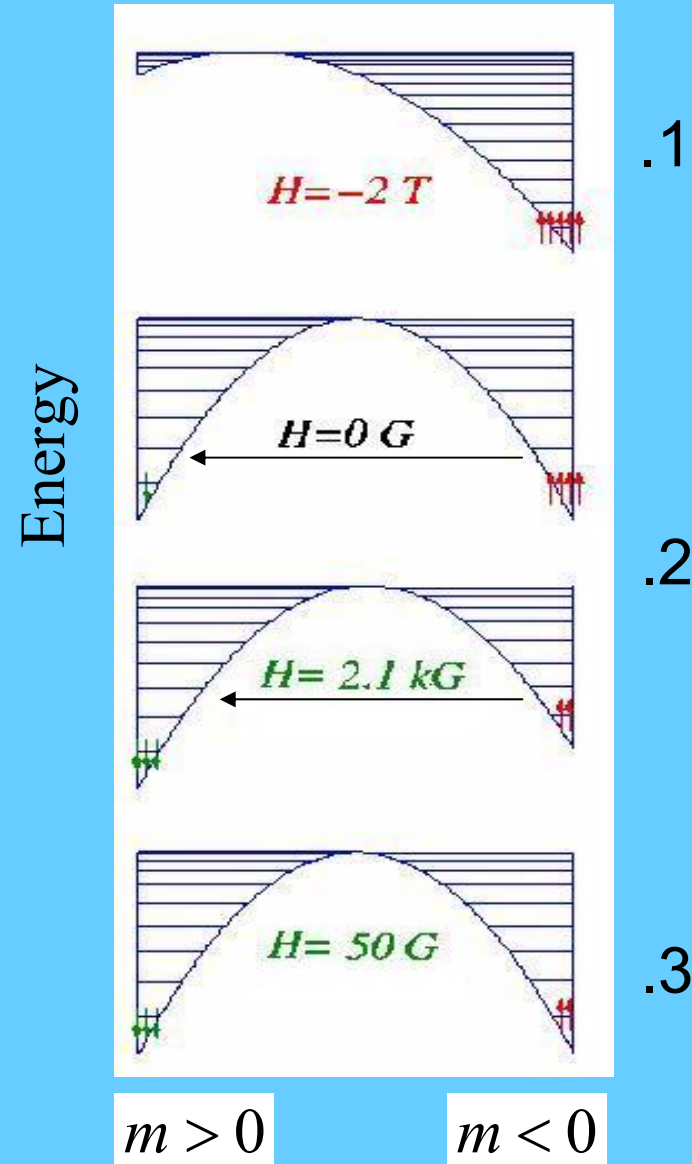
1. A strong negative field of -2T that is parallel to the z axis, polarizes the Fe8 molecules

2. The field is swept to an intermediate positive value  $H_i$ , at a rate of 4 mT/s

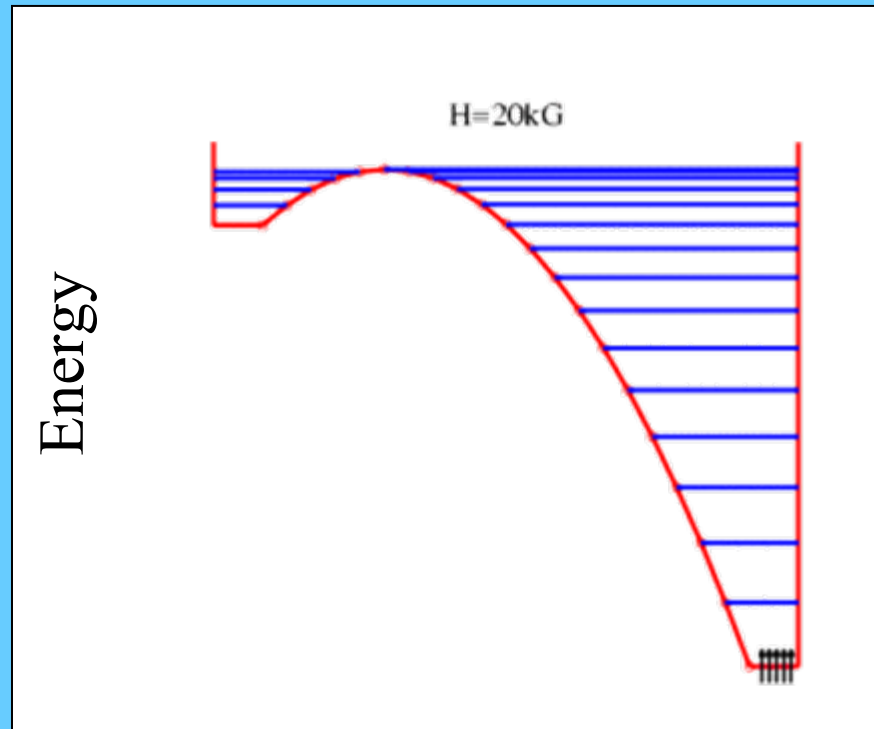
→ different process

3. The field is swept back to +50G at the same rate

→ same measurement



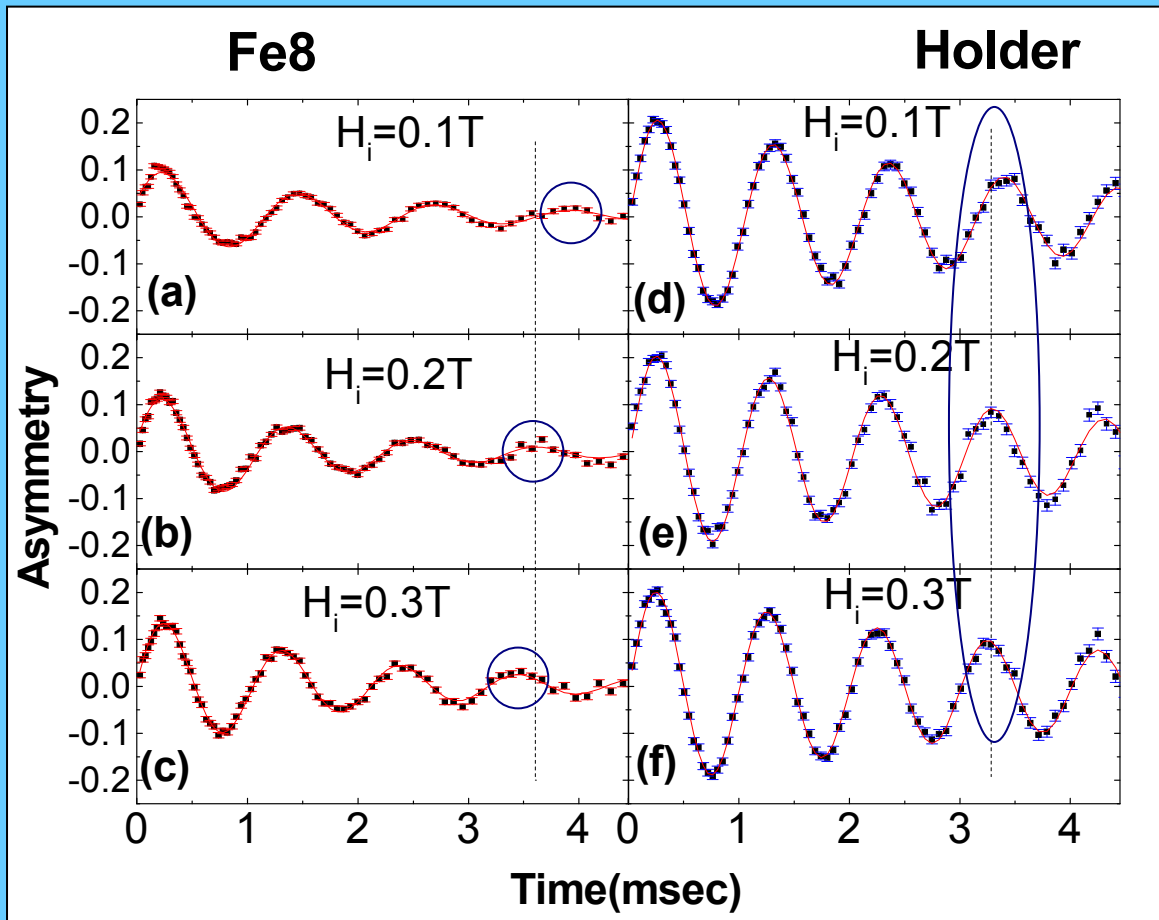
# Illustration of the double well potential in the field cycle



$m > 0$

$m < 0$

# Experiment results



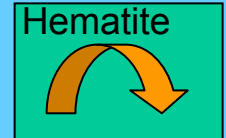
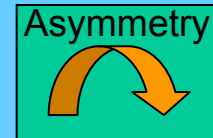
- There is a difference in amplitude.

- The solid lines are the fit to the function:

$$A(t) = A \sin(\omega_\mu t) e^{-\lambda t}$$

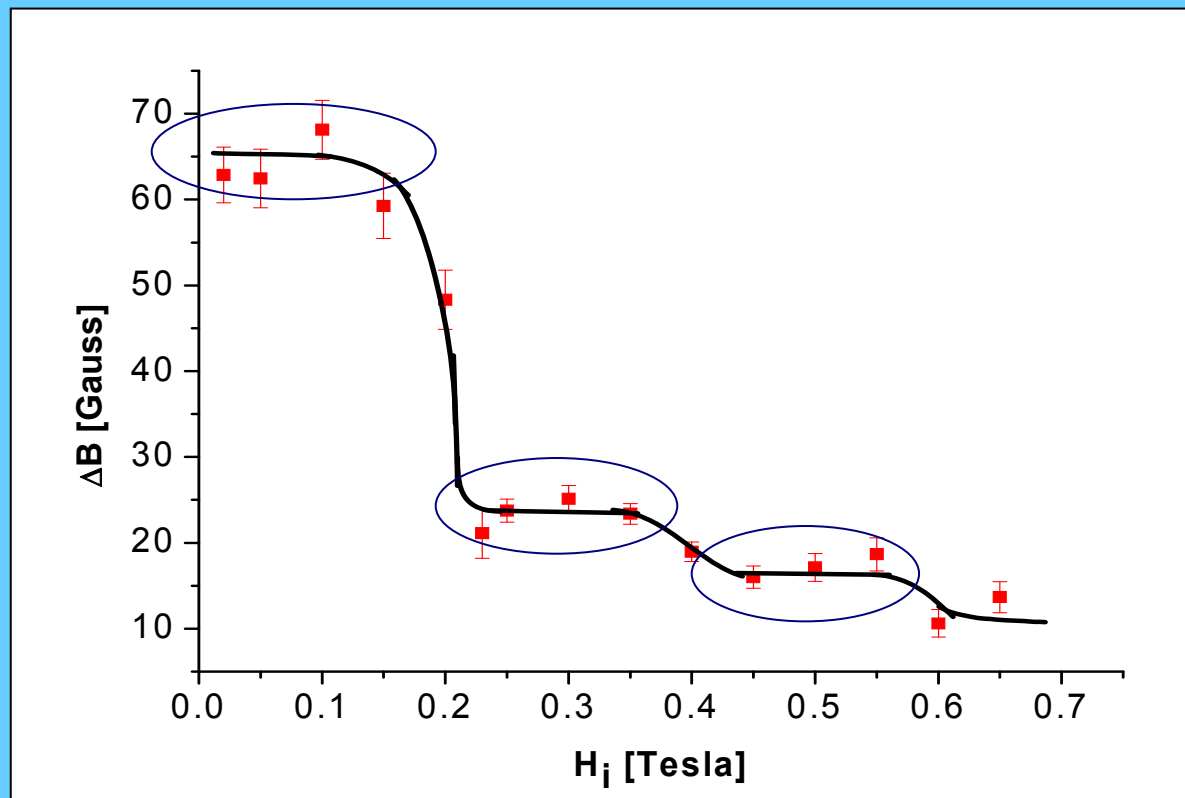
$$\left( \begin{array}{c} \vec{\omega}_\mu = \gamma_\mu \cdot \vec{B} \end{array} \right)$$

- Reproducibility



# Analysis of the results

$$\Delta B = B_{Fe_8} - B_{Holder} = \frac{\omega_{Fe_8}(H_i) - \omega_{Holder}(H_i)}{\gamma_\mu}$$



- The process:  
 $-2T \rightarrow H_i \rightarrow 50G$

- Matching fields:

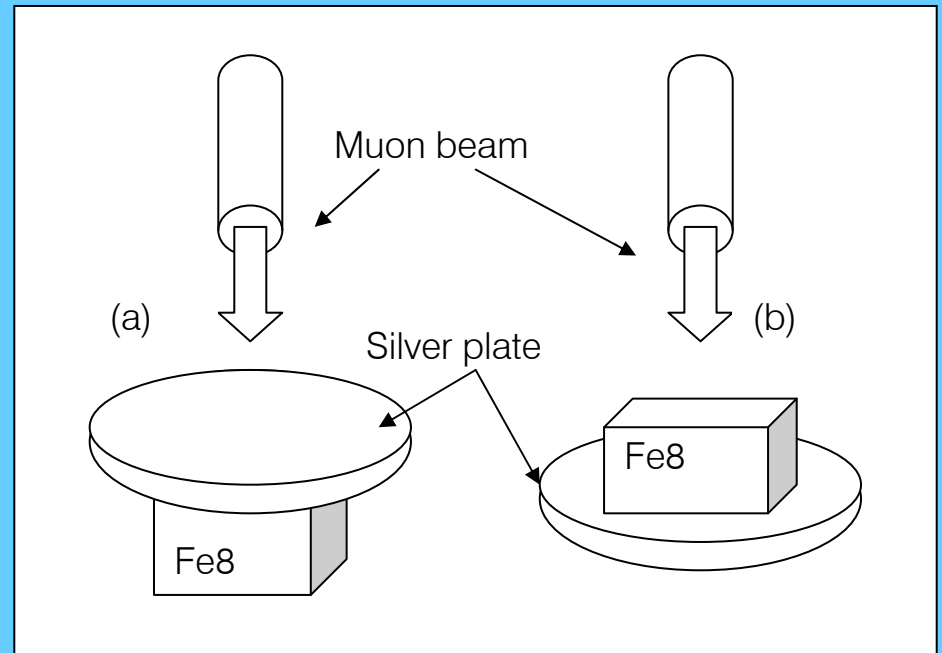
$$H_n = n \times 2.1kG.$$

$$n = 0, 1, 2, \dots$$



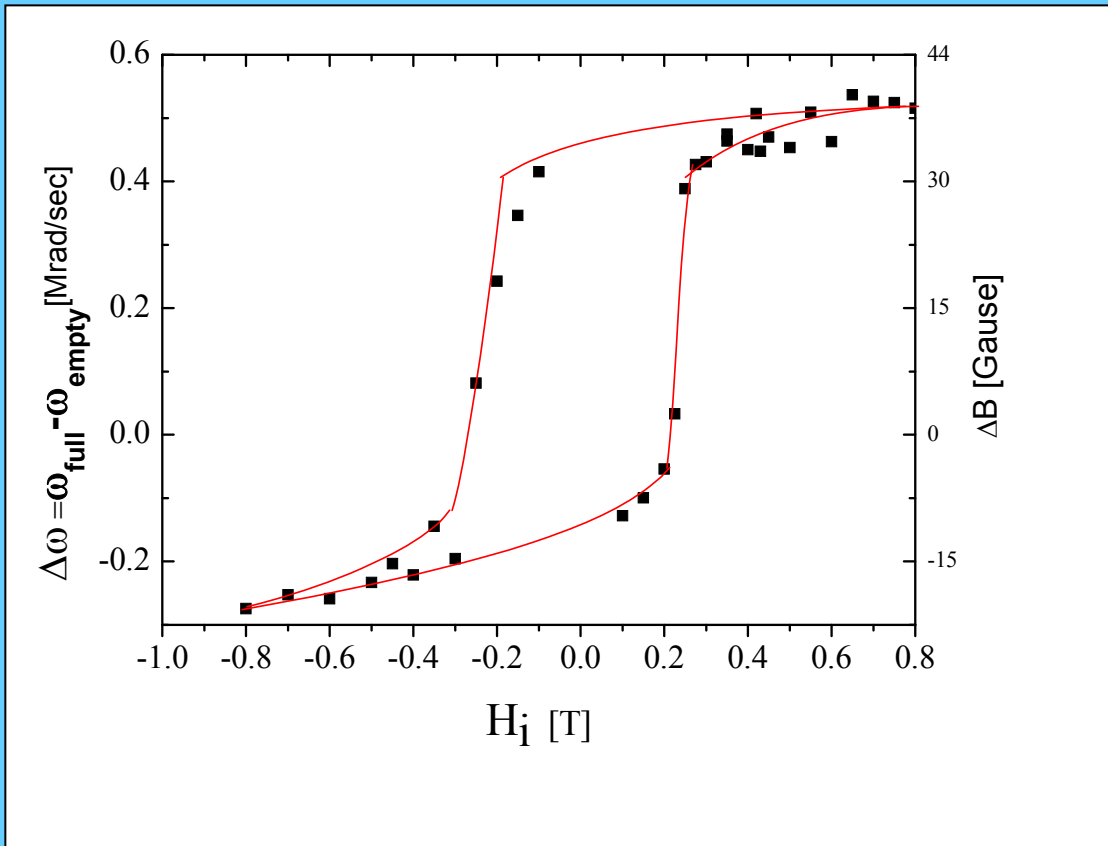
# Two different setups

Several Fe8 single crystals were glued on a small silver plate.



In a different experiment the muons stopped in the silver plate

# Analysis of the results – muons hit the silver plate



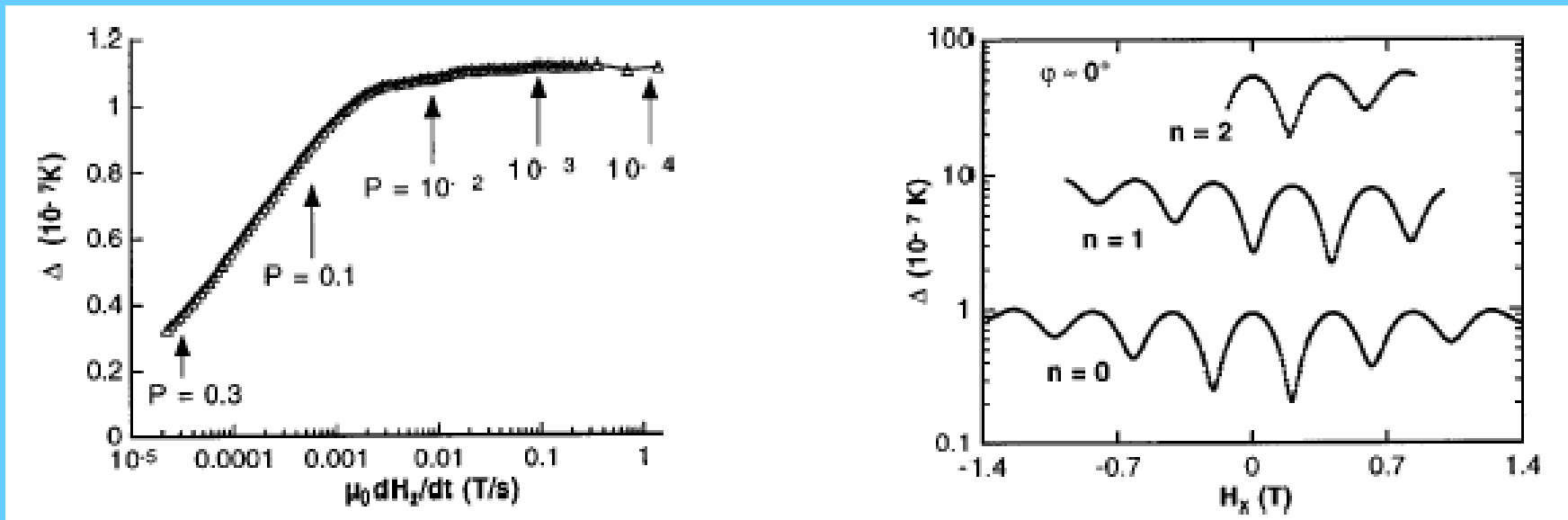
The resolution is worse, but a full hysteresis loop can be seen.

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# Comparison to the Landau-Zener model and to previous experiments

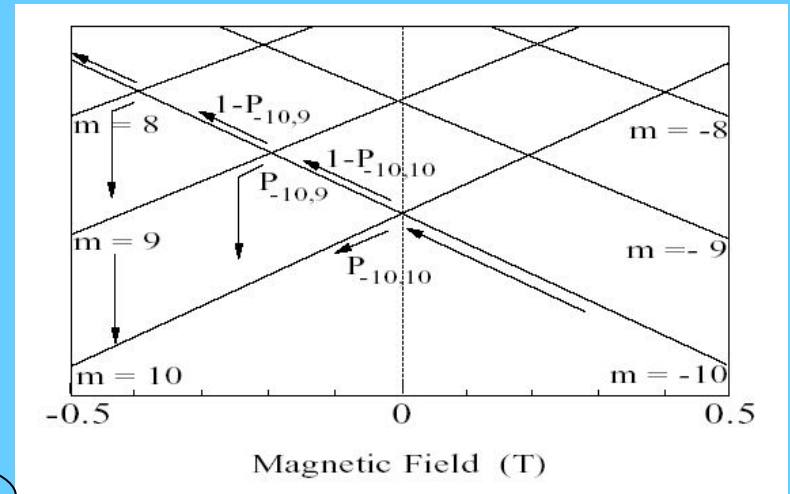
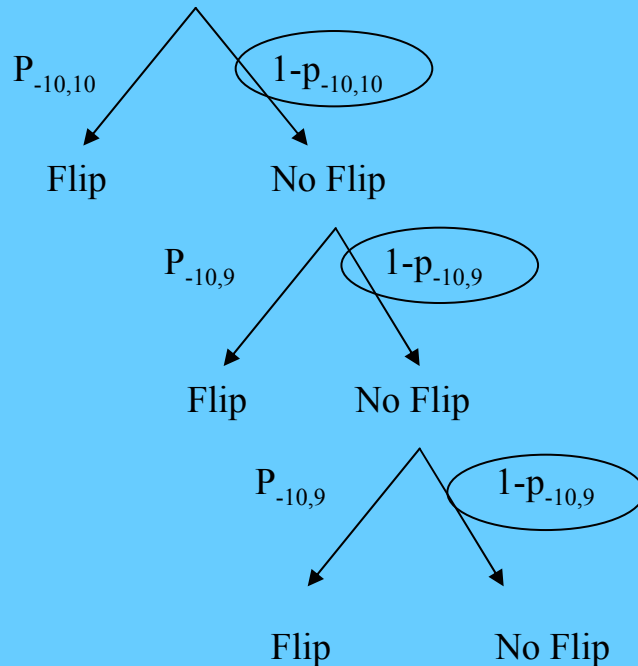
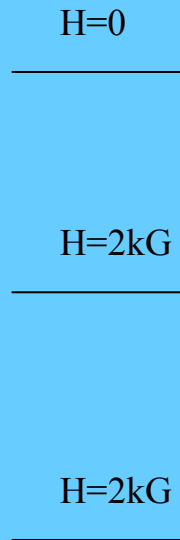
$$P = 1 - \exp\left[-\frac{\pi\Delta_{m,m'}^2}{2\hbar g\mu_B |m - m'| dH/dt}\right]$$



W. Wernsdorfer, R. Sessoli, Science 1999, 284, 133.

# The probability to stay at $m=-10$

For example:  $2\text{kG} < H_i < 4\text{kG}$

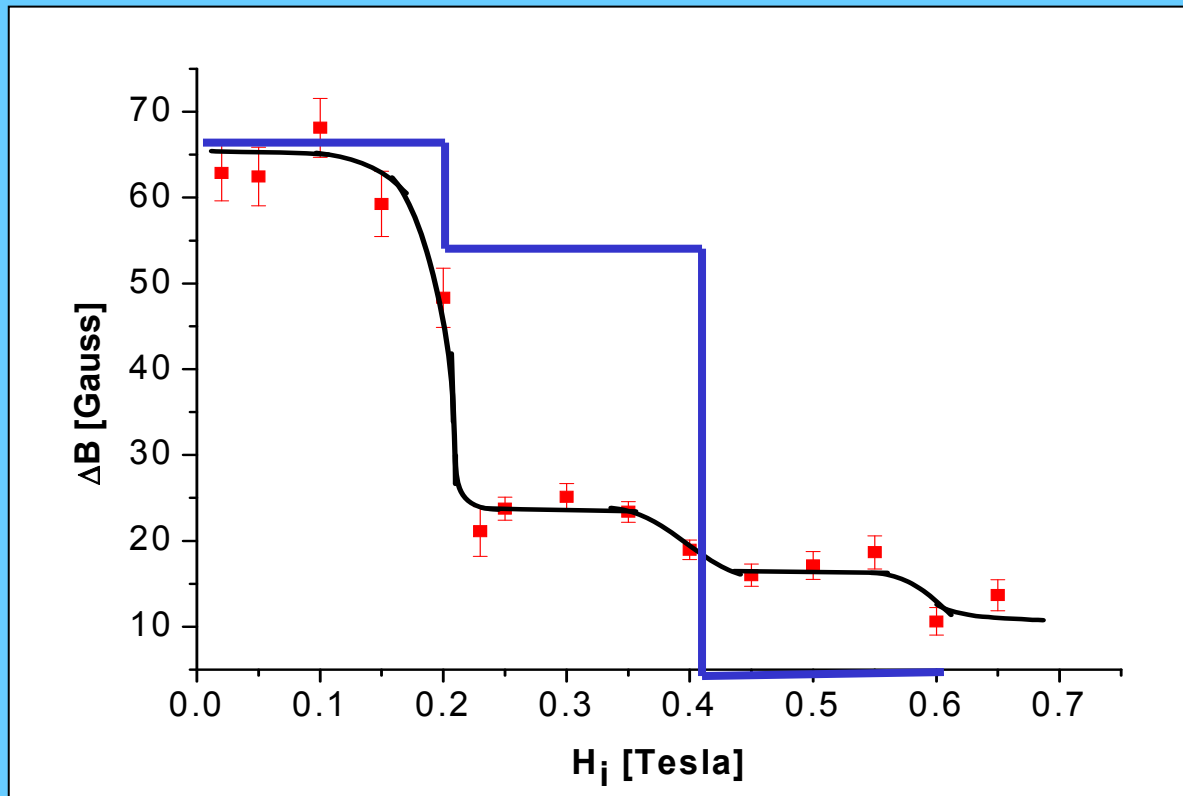


- The process:  
 $-2\text{T} \rightarrow H_i \rightarrow 50\text{G}$

The probability not to tunnel -

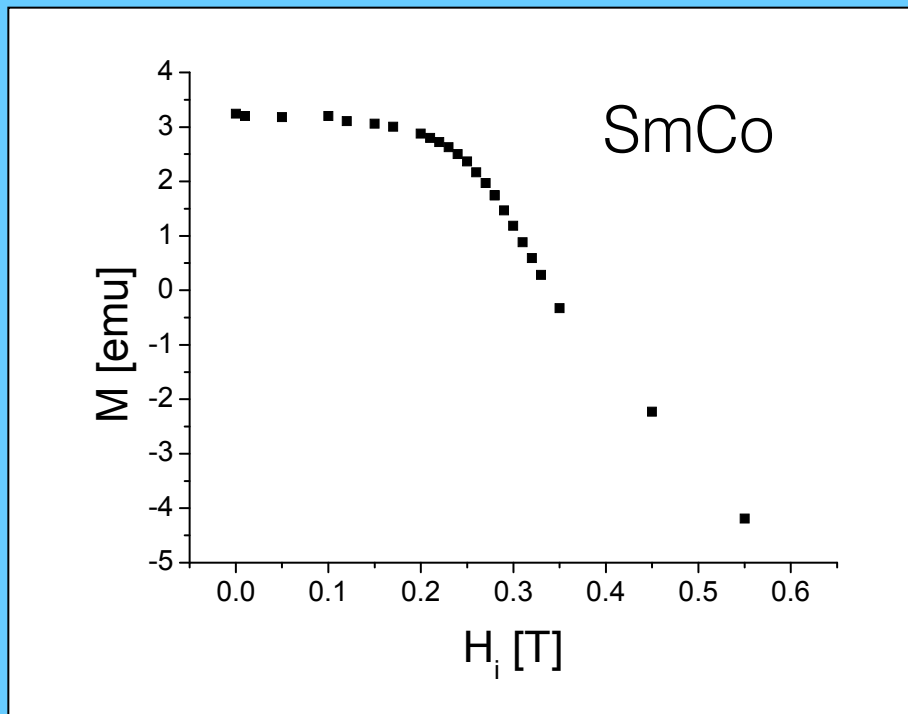
$$(1-P_{-10,10}) \times (1-P_{-10,9})^2$$

# Comparison to the Landau-Zener model

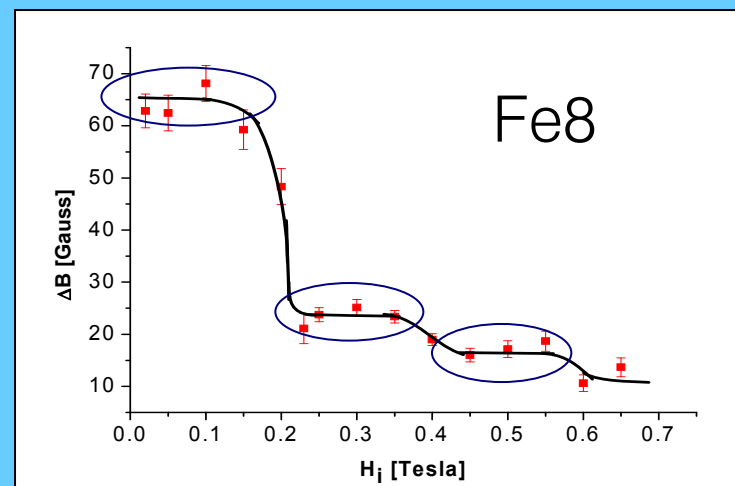


The agreement between theory and experiment is poor.

# The same process for SmCo



$-2T \rightarrow H_i \rightarrow 50G$



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# Summary

- The qualitative result from the Faraday force magnetometer demonstrates again the quantum nature of the Fe<sub>8</sub> crystals.
- Using the mSR technique, which is also applicable to films, we observe quantum tunneling of the magnetization (QTM) in the Fe<sub>8</sub> compound.
- We show that Fe<sub>8</sub> can “remember” for at least 1/2 hour which intermediate field was visited. Using Fe<sub>8</sub>, we can distinguish between at least six processes by performing the same measurement.

**This warrants Fe<sub>8</sub> molecules the candidacy for a multi-bit magnetic memory.**

# Acknowledgments:

**Dr. Y. Sheynin, Dr. M. Kapon, Prof. M. Kaftori** - for sample preparation and characterization

**Prof. E. Polturak and Prof. M. Resnikov** - for helping with the DR

Technicians - Leonid Iomin, **Mordehay Eilon, Shmuel Hoida** – for their help with the DR

**Prof. S. Maegawa, Dr. M. Ueda** - for initial samples, *Kyoto University, Japan*

**Dr. A. Amato, C. Bains** – for  $\mu$ SR instrument support, *PSI, Switzerland*

# Acknowledgments:

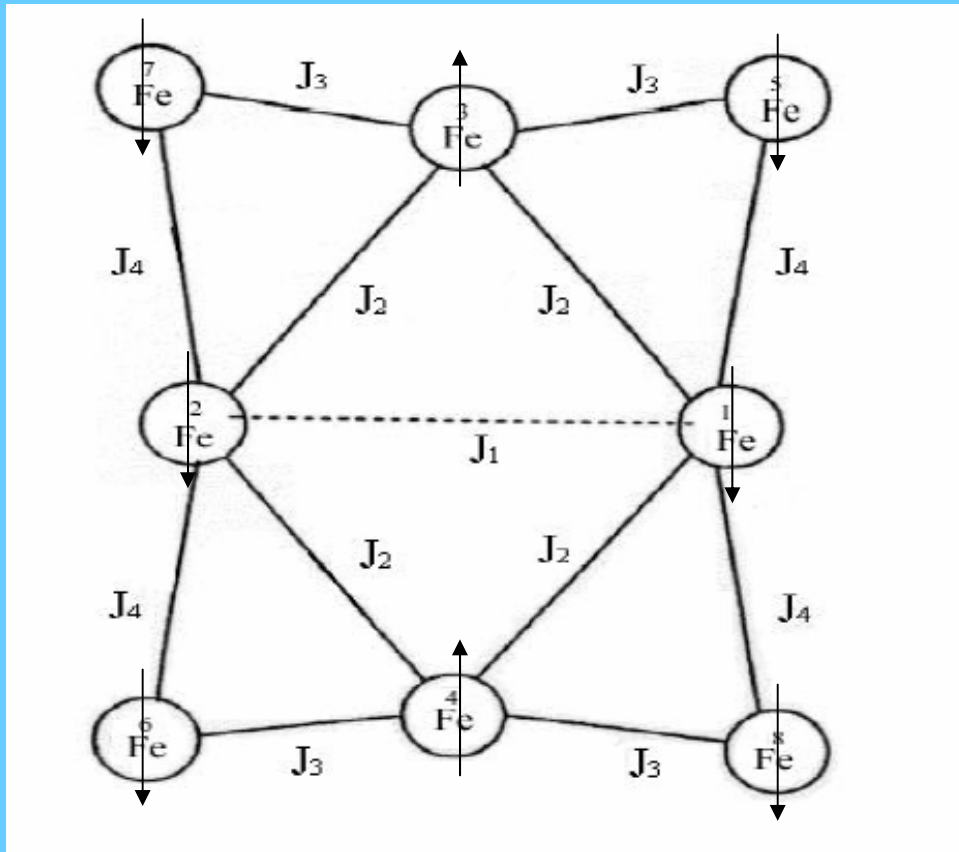
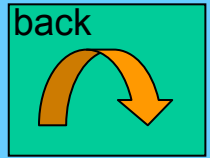
My lab members:

Shahar, Ariel, Meni, Oshri, Rinat, Eva, Lior and  
Amit Kanigel

**Special thank for Prof. Amit Keren.**

**End**

# The exchange path ways connecting iron(III) in Fe8



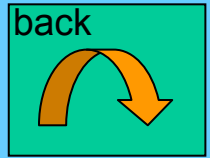
$$J_1 = -147\text{K}$$

$$J_2 = -173\text{K}$$

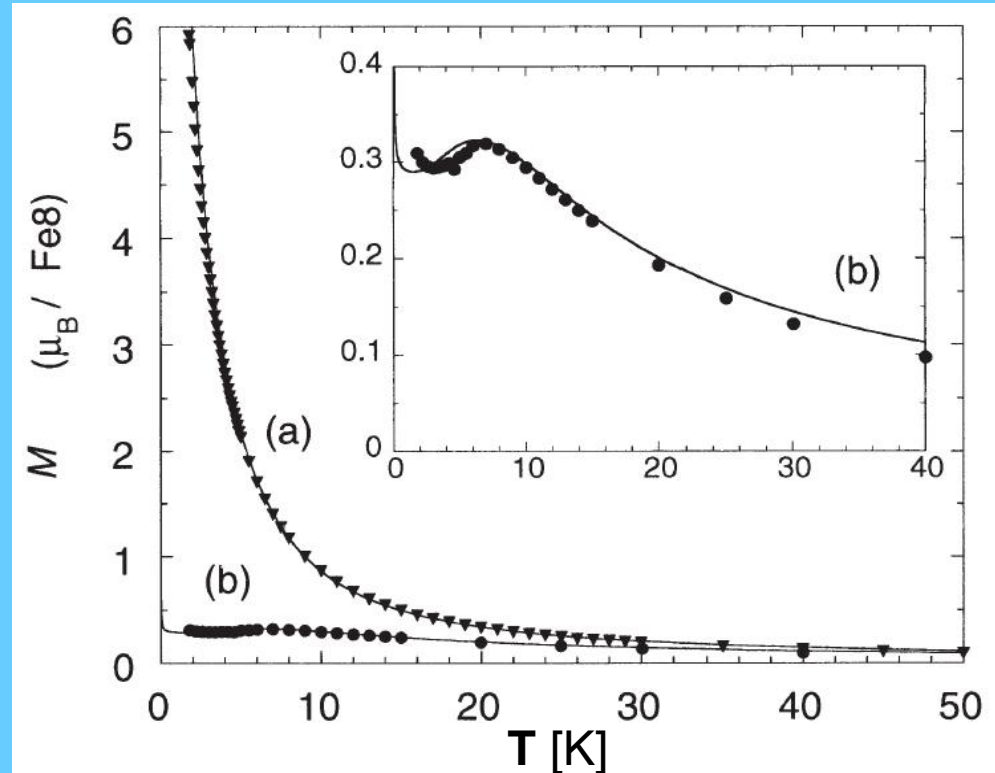
$$J_3 = -22\text{K}$$

$$J_4 = -50\text{K}$$

# Blocking Temperature



At temperatures lower than the magnetic coupling  $J$  between ions inside the molecule, the spins of the ions are locked, and the molecules behave like non-interacting spins.

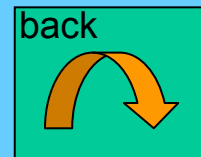


(a) parallel to the easy axis

(b) perpendicular to the easy axis.

M. Ueda & S. Maegawa, J. Phys. Soc. Jpn. 70 (2001)

# Hamiltonian of Fe8



The effective spin Hamiltonian (without the Zeeman term):

$$\mathcal{H} = \mathbf{D} S_z^2 + E (S_x^2 - S_y^2) + B_4^0 O_4^0 + B_4^2 O_4^2 + B_4^4 O_4^4$$

$D$	$ E/D $	$B_4^0$	$B_4^2$	$B_4^4$	Lit.
-0.205	0.19	$1.6 \times 10^{-6}$	$-5.0 \times 10^{-6}$	$-8 \times 10^{-6}$	[158]
-0.203	0.160	$0.7 \times 10^{-6}$	$8.06 \times 10^{-8}$	$5.96 \times 10^{-6}$	[160]
-0.205	0.150	$1.4 \times 10^{-6}$	$8.06 \times 10^{-8}$	$5.96 \times 10^{-6}$	[162]

$$O_4^2 = \{[7S_z^2 - S(S+1) - 5](S_+^2 + S_-^2) + (S_+^2 + S_-^2)[7S_z^2 - S(S+1) - 5]\}/4$$

$$O_4^4 = (S_+^4 + S_-^4)/2$$

$$O_4^3 = [S_z(S_+^3 + S_-^3) + (S_+^3 + S_-^3)S_z]/4$$

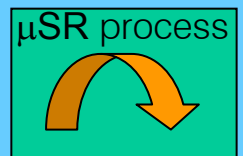
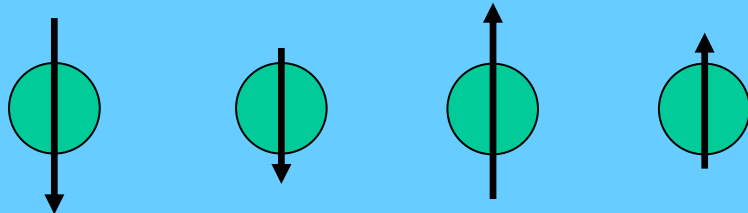
D. Gatteschi and R. Sessoli, *Angew. Chem. Int. Ed.* 42, No. 3 (2003), p. 268

# What do we mean by multi-bit memory?

- **Single-bit Memory** → using the same measurement one can distinguish between two different preparation processes.



- **Multi-bit Memory** → using the same measurement one can distinguish between more than two preparation processes.





# The concept of tunnel splitting: $S=1/2$

$$\mathcal{H} = DS_z^2 + g\mu_B(h_x S_x - h_z S_z) = \begin{pmatrix} -D/4 - g\mu_B h_z & g\mu_B h_x / 2 \\ g\mu_B h_x / 2 & D/4 + g\mu_B h_z \end{pmatrix}$$

The eigenvectors and eigenvalues of  $\mathcal{H}_0$  are:

$$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix} \rightarrow E_s = -D/4 + g\mu_B \sqrt{h_x^2 + h_z^2},$$

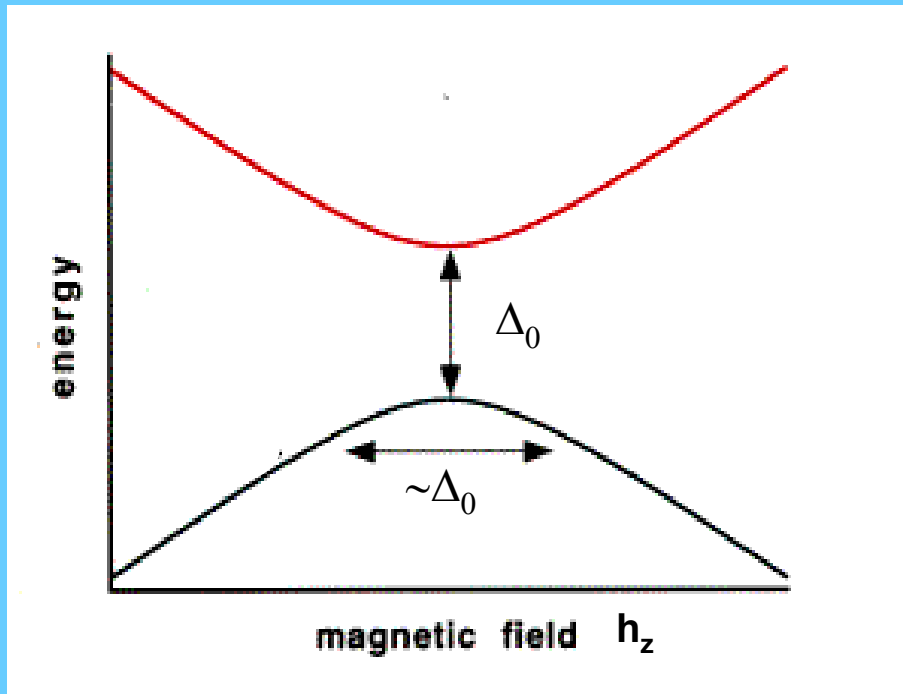
$$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -1 \end{pmatrix} \rightarrow E_{as} = -D/4 - g\mu_B \sqrt{h_x^2 + h_z^2}$$

$\Delta_0 = g\mu_B h_x$  known as tunnel splitting

$$\left| \left\langle \begin{pmatrix} 1 & 0 \end{pmatrix} e^{-\frac{i\mathcal{H}t}{\hbar}} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \right\rangle \right|^2 = \frac{h_x^2}{h_x^2 + h_z^2} \left[ \frac{1}{2} - \frac{1}{2} \cos \left( \frac{g\mu_B \sqrt{h_x^2 + h_z^2} \cdot t}{\hbar} \right) \right]$$

The spin will tunnel at a rate given by:  $\Delta/\hbar = g\mu_B \sqrt{h_x^2 + h_z^2} / \hbar$

# Zener time



$$\Delta_0 / \tau_{\text{tunnel}} > g\mu_B \frac{dh_z}{dt}$$

$$\tau_{\text{tunnel}} = \frac{\pi}{2\Delta_0}$$



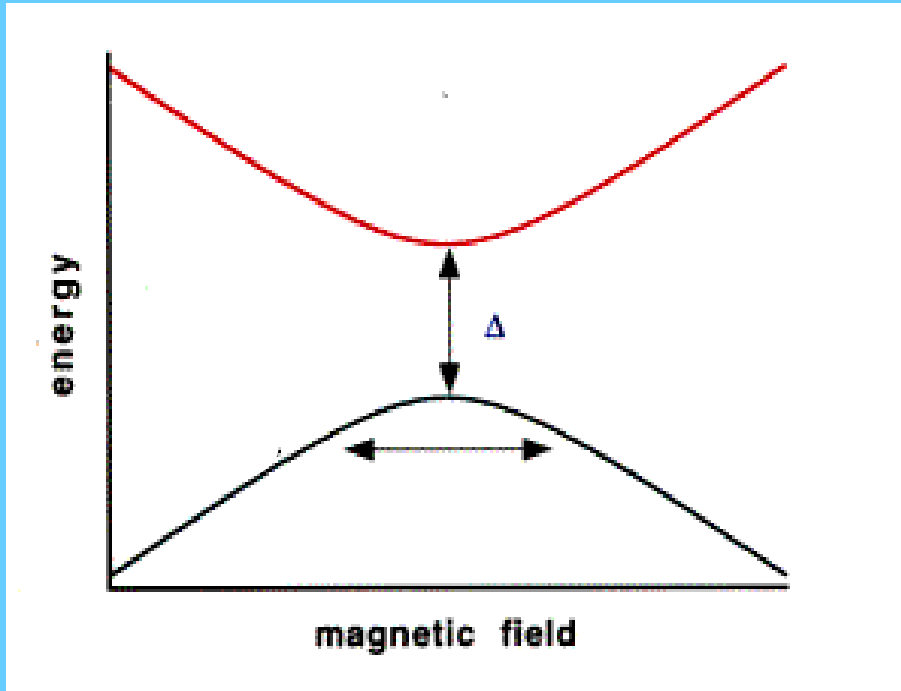
$$\Delta_0 / \left( \frac{\pi\hbar}{2\Delta_0} \right) > g\mu_B \frac{dh_z}{dt}$$



$$\Delta_0^2 / \hbar g\mu_B \frac{dh_z}{dt} > 1$$

$$P_{m,m'} = 1 - \exp \left[ - \frac{\pi \Delta_{m,m'}^2}{2\hbar g\mu_B |m - m'| dH/dt} \right]$$

# Zener Time – Mullen et al



$$\frac{\hbar\alpha}{\Delta^2} \gg 1 \quad \text{Adiabatic limit:}$$

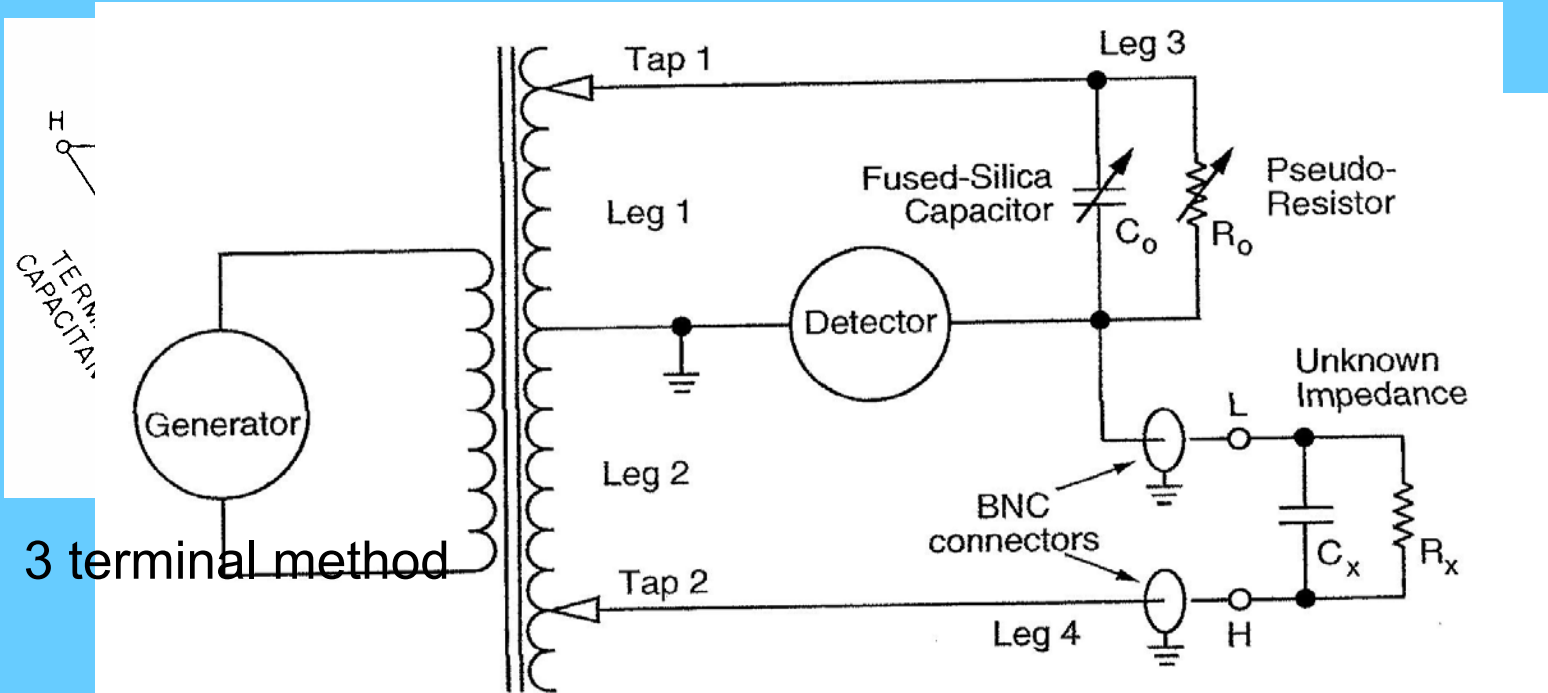
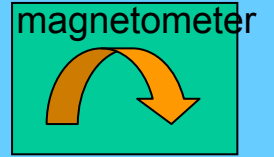
$$\rightarrow \tau_z \approx \sqrt{\hbar / \alpha}$$

$$\frac{\hbar\alpha}{\Delta^2} \ll 1 \quad \text{sudden limit:}$$

$$\rightarrow \tau_z \approx \Delta / \alpha$$

$$\alpha = \lim_{\Delta \rightarrow 0} \frac{dE}{dt} = g\mu_B \frac{dh_z}{dt}$$

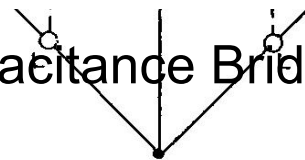
# Capacitance bridge



3 terminal method

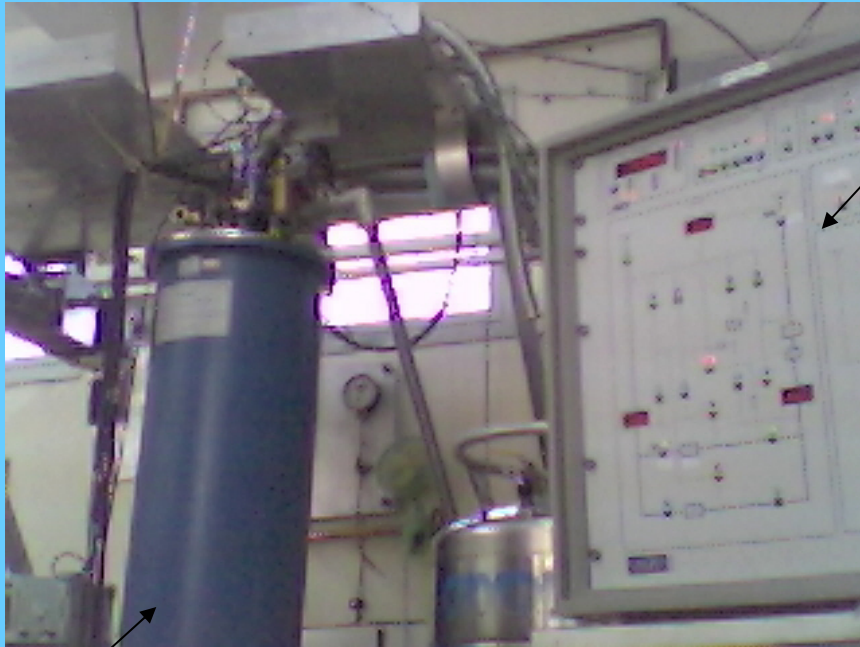
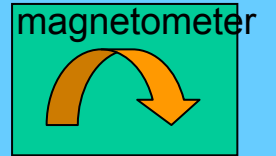
$$V_N C_N = V_X C_X \rightarrow \frac{C_X}{C_N} = \frac{V_N}{V_X} \frac{N_X}{N_N} = \text{Transformer Ratio}$$

Basic bridge circuit of AH2550A Capacitance Bridge



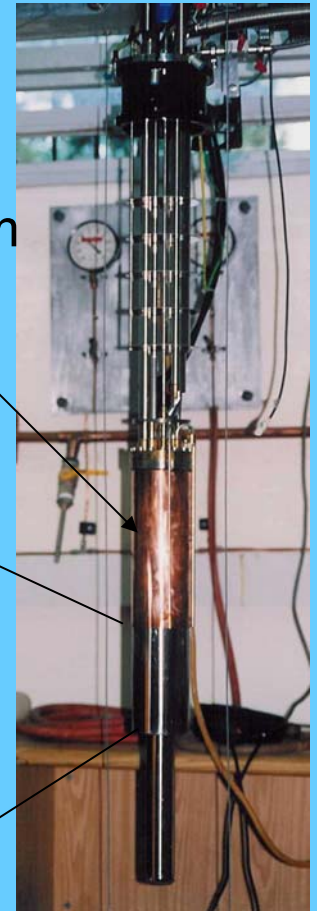
A capacitance bridge with transformer ratio arms.

# Dilution refrigerator

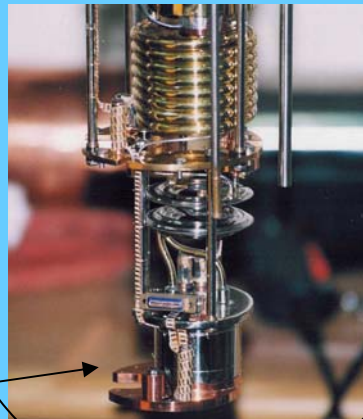


Control unit

outer Vacuum chamber

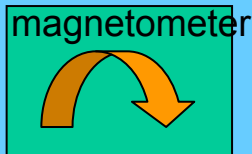
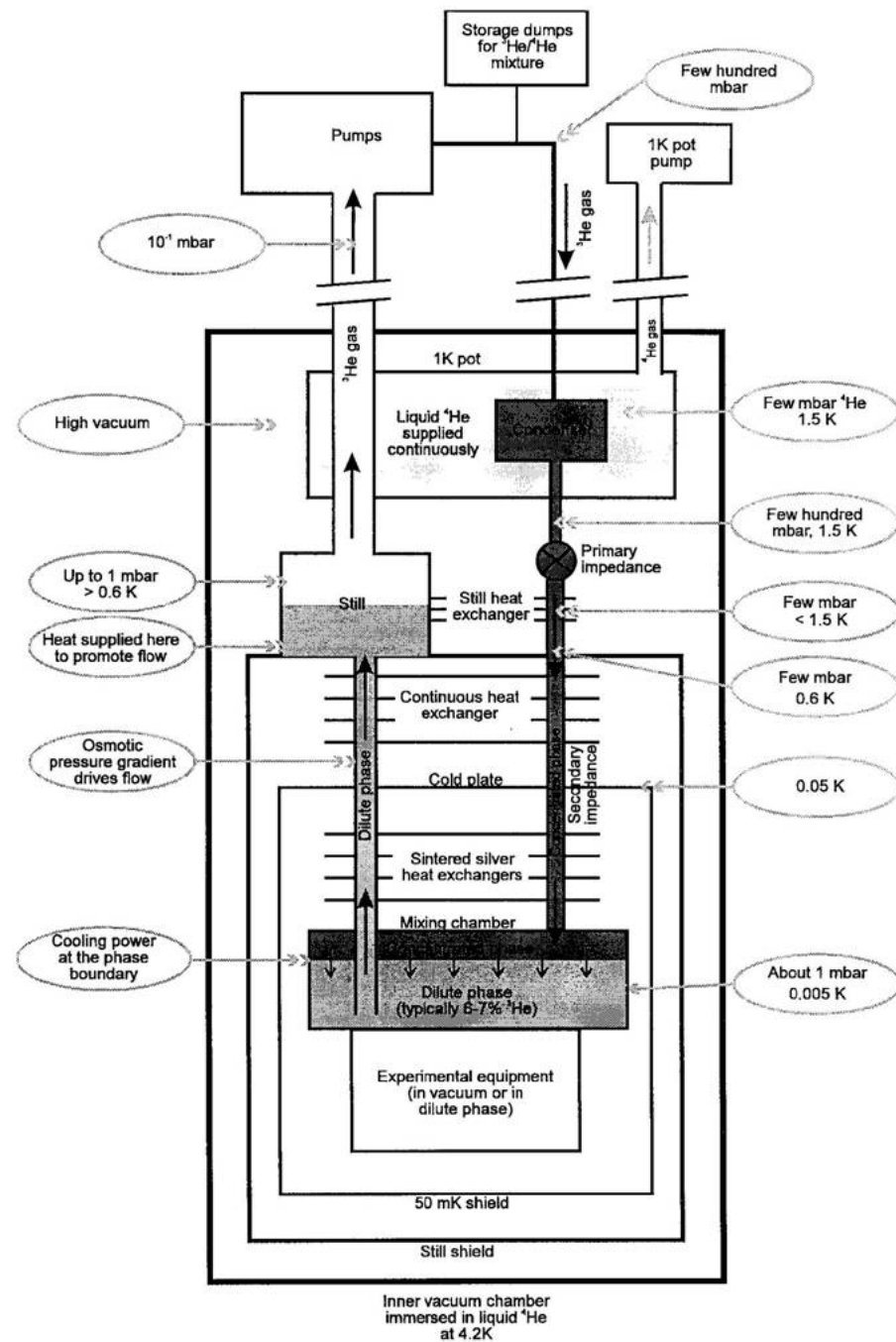
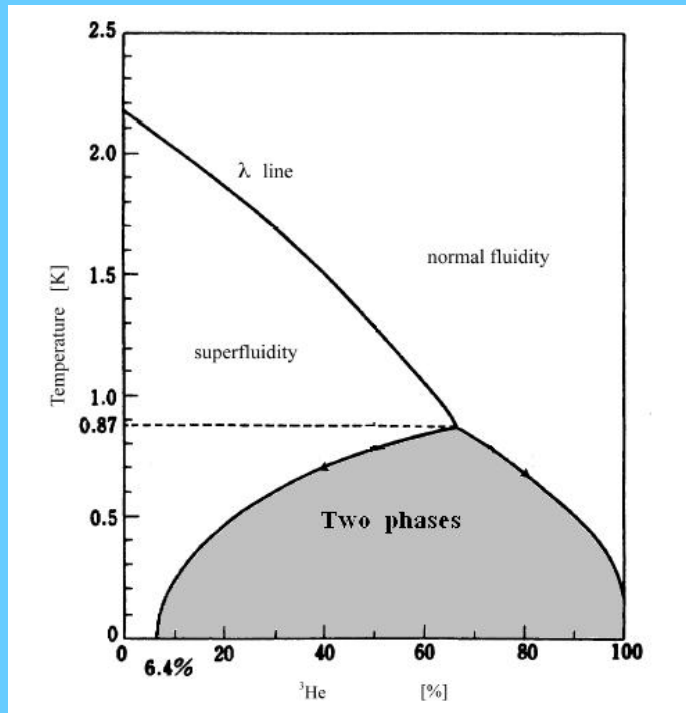


Inner Vacuum chamber

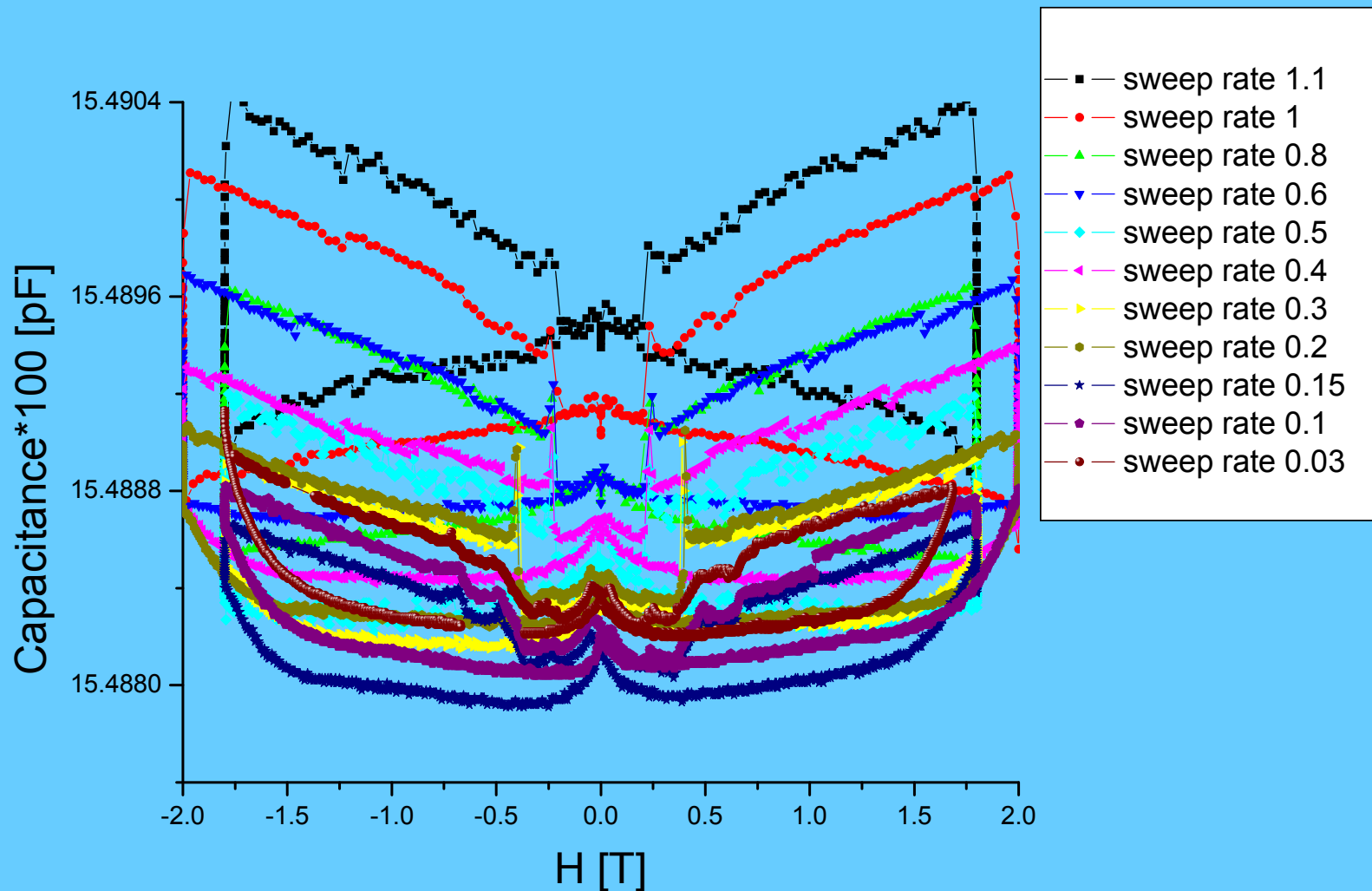


Mixing chamber

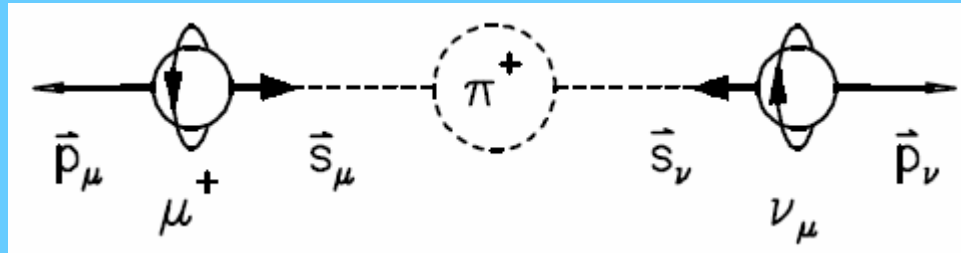
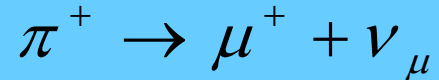
# Dilution refrigerator – schematic view



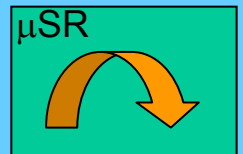
# Changes due to eddy currents



# Pion decay

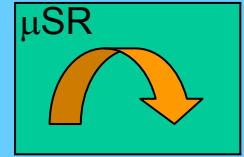


- Only left-handed neutrinos exist
- Pions have zero spin
- Pions at rest ( $p_p = 0$ )  $\rightarrow$  Muons have a spin which is anti-parallel to their momentum

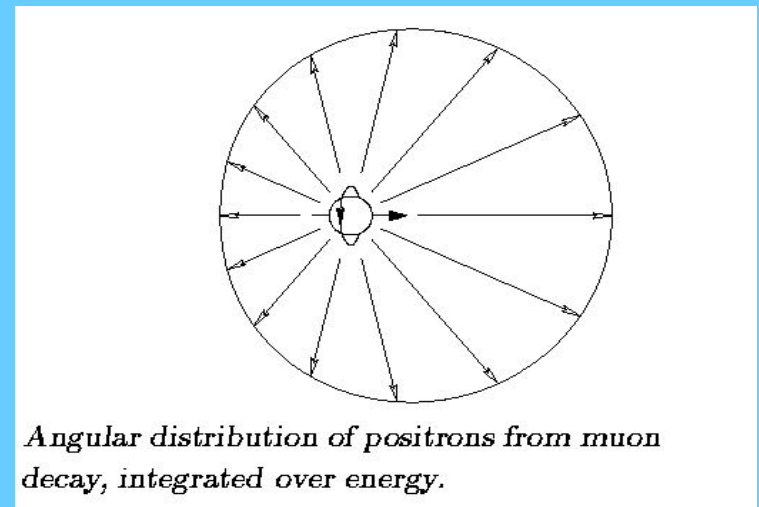
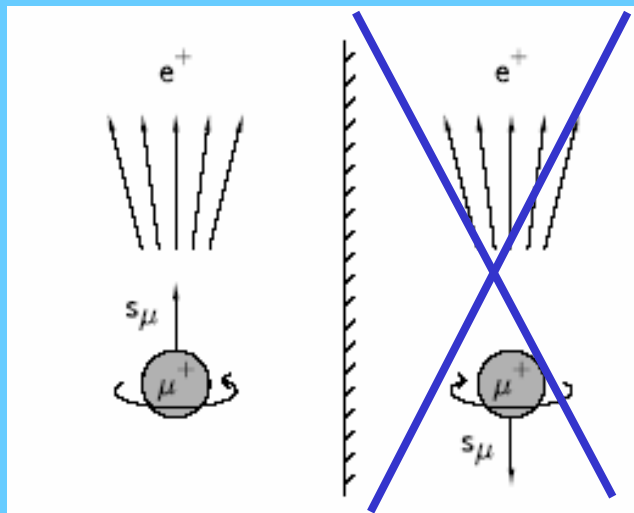




# Muon decay

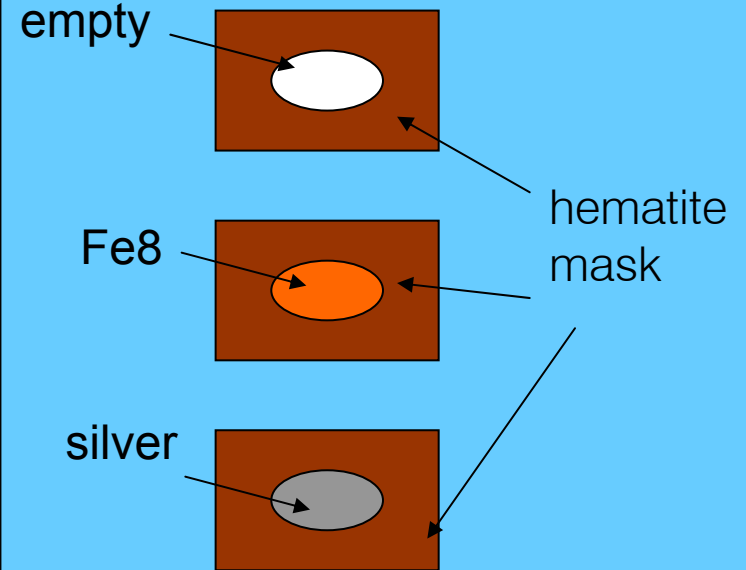
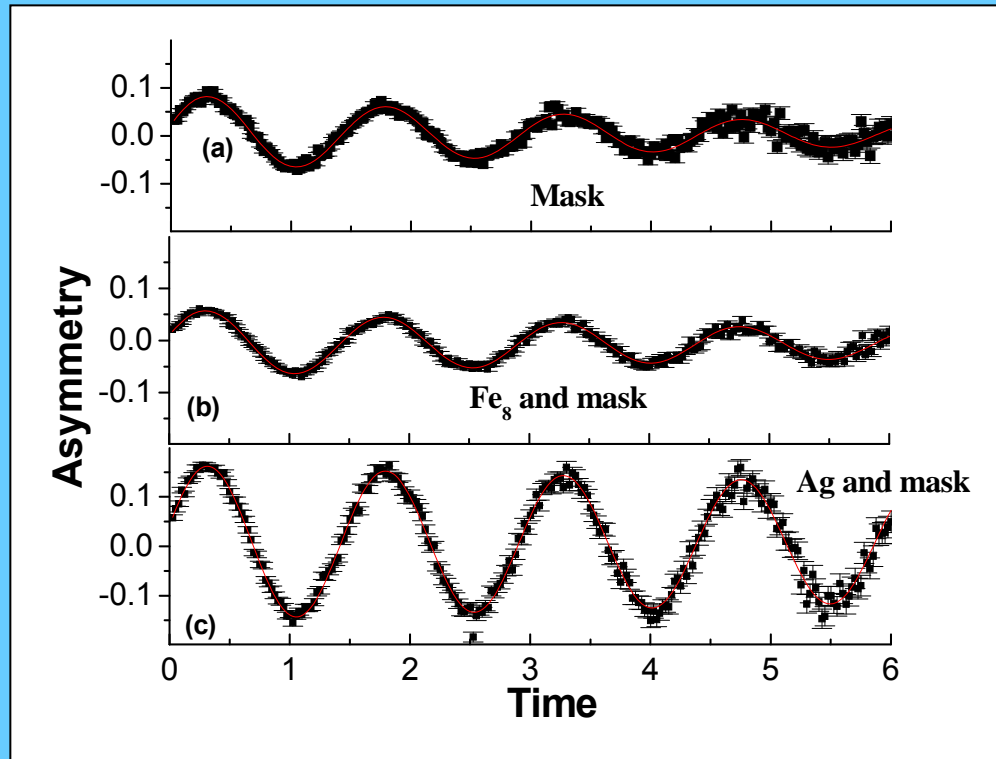
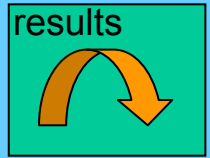


- The muon decays according to:  $\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$
- The positron is usually energetic enough to travel a substantial distance before annihilating.



The violation of parity

# Fe8 as hematite



The asymmetry of a hematite and glue mask (a) is very similar to mask and Fe<sub>8</sub> (b), but different from mask and silver (c). Therefore, muons in Fe<sub>8</sub> do not contribute to the asymmetry.

# Comparison to the Landau-Zener model

$$P = 1 - \exp\left[-\frac{\pi\Delta_{m,m'}^2}{2\hbar g\mu_B |m - m'| dH/dt}\right]$$

$$\hbar = 7.6328 \times 10^{-12} [K]/[s]$$

$$\mu_B = 0.67170099 [K]/[T]$$

$$dH / dt = 0.245 [T]/[\text{min}] = 4.083 \times 10^{-3} [T]/[s]$$

$$\text{For } \Delta_{-10,10} = 10^{-7} \text{ K} \rightarrow P_{-10,10} = 0.02$$

$$\text{For } \Delta_{-10,9} = 3 \times 10^{-7} \text{ K} \rightarrow P_{-10,9} = 0.16$$

$$\text{For } \Delta_{-10,8} = 20 \times 10^{-7} \text{ K} \rightarrow P_{-10,8} = 0.99$$

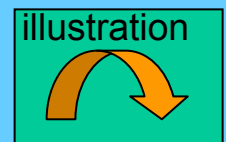
# Comparison to the Landau-Zener model

Starting point -  $N_{-10} : N_{10} = 1:0$

$H_i$ (intermediate field)	The probability <u>not</u> to tunnel	$N_{-10} : N_{10}$
$H_i < \sim 0.22T$	$1 - P_{-10,10}$	0.9776 : 0.0224
$\sim 0.22T < H_i < \sim 0.44T$	$(1 - P_{-10,10}) \times (1 - P_{-10,9})^2$	0.68 : 0.38
$\sim 0.44T < H_i < \sim 0.66T$	$(1 - P_{-10,10}) \times (1 - P_{-10,9})^2 \times (1 - P_{-10,8})^2$	0 : 1

$N_{-10}$  - the number of the molecules with spin up

$N_{10}$  - the number of the molecules with spin down

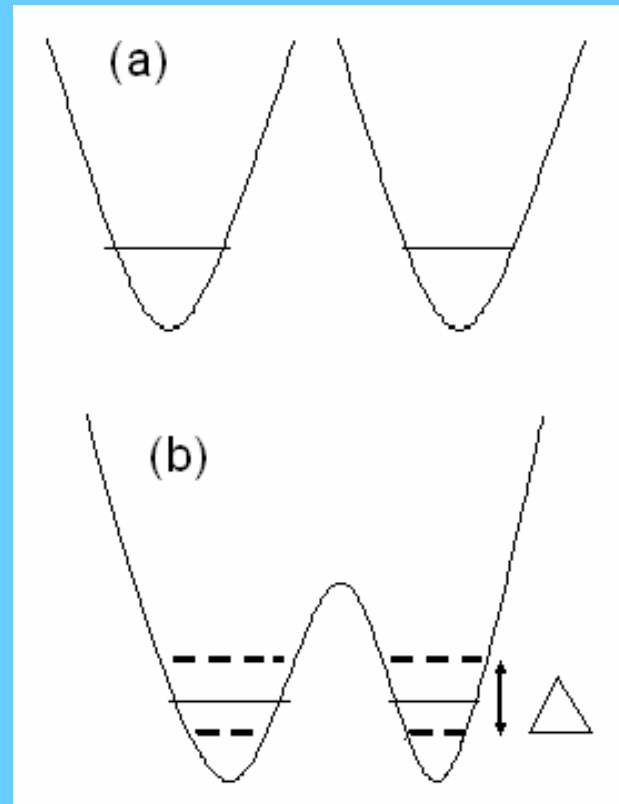


# The simplest model – double well potential

Tunneling in a double well system:

a) Non-coupling states.

b) Coupling states giving rise to tunnel splitting,  $\Delta$ .



# The prediction

## “The molecular approach to nanoscale magnetism”

A. Caneschi, D. Gatteschi, C. Sangregorio, R. Sessoli, L. Sorace, A. Cornia, M.A. Novak, C. Paulsen, W. Wernsdorfer

Journal of Magnetism and Magnetic Materials Vo. 200 (1999) p. 182-201

(referred to the result in Mn12)

“ These results...also make Mn12ac more appealing for technological applications as it represents a multi- rather than a bi-stable single molecule memory unit. ”

# Summary

- The experimental work:
  - Synthesizing Fe<sub>8</sub> crystals
  - Assembling a dilution refrigerator
  - Faraday force magnetometer experiments (Design a load sensing variable capacitor; operating DR, SC magnet, capacitance bridge)
  - $\mu$ SR experiments

end