
Quantum Tunneling of the Magnetization in High Spin Molecules

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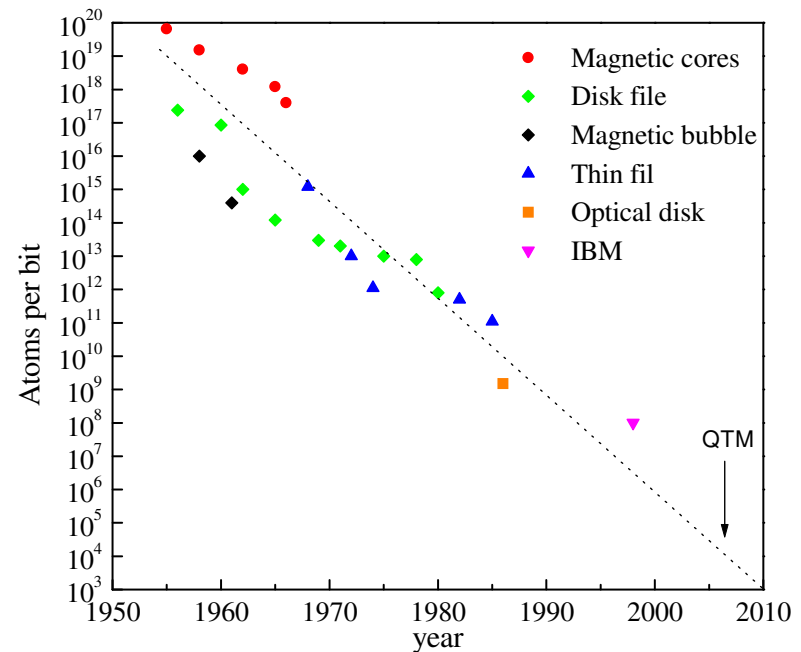
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Schuillier

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Introduction

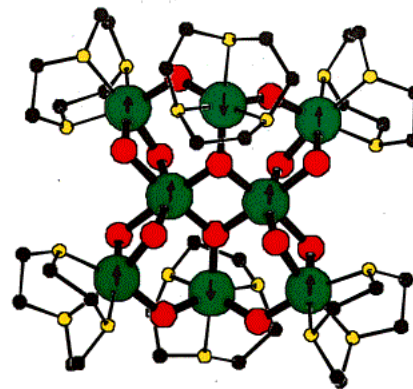
- **High Spin Molecules (HSM)** consist of coupled magnetic ions.
- At low temperatures HSM behave like giant spins.
- They crystallize in a lattice where they are magnetically separated.
- HSM can become the smallest magnetic writing unit.

Harris, *Physics World* (1999)

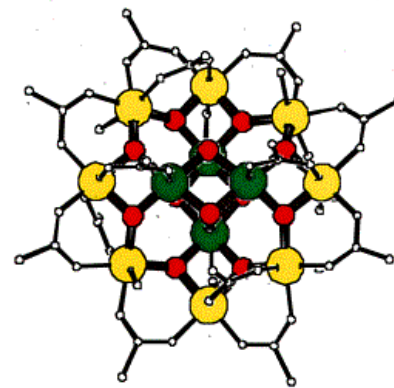


Most Studied HSM

- Fe_8 with ground spin state $S = 10$.
- 6 Fe ($S = 5/2$) ions coupled anti-ferromagnetically to 2 Fe ions.
- Mn_{12} with ground spin state $S = 10$.
- 4 Mn^{4+} ($S = 3/2$) ions coupled anti-ferromagnetically to 8 Mn^{3+} ($S = 2$) ions.



Fe_8

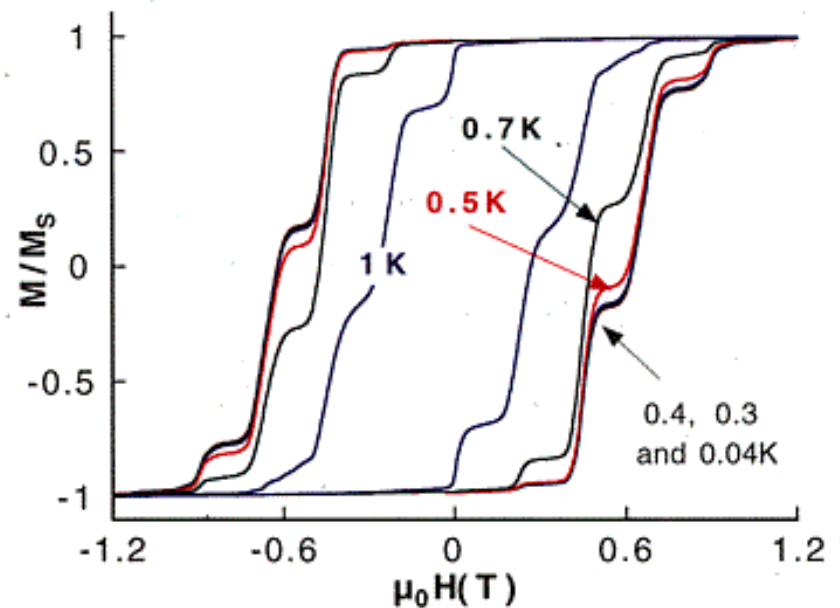


Mn_{12}

Quantum Tunneling of the Magnetization (QTM)

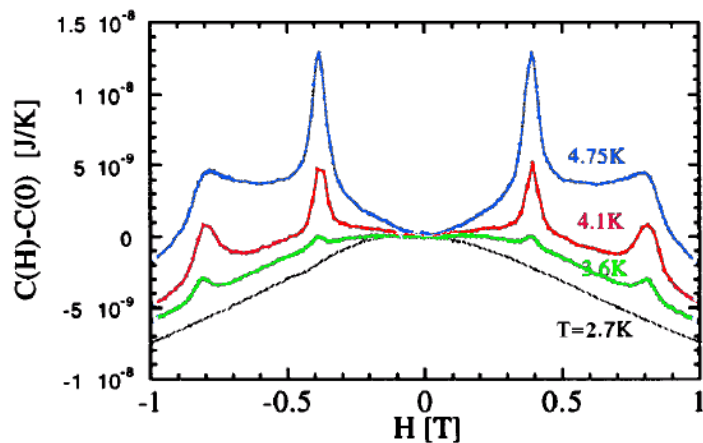
- QTM was first observed in Mn_{12} and then in Fe_8 , through **steps at regular intervals** of magnetic field in the hysteresis loop.
- QTM provides a signature quantum mechanical behavior in macroscopic systems.

Wernsdorfer, QMAG (1999)

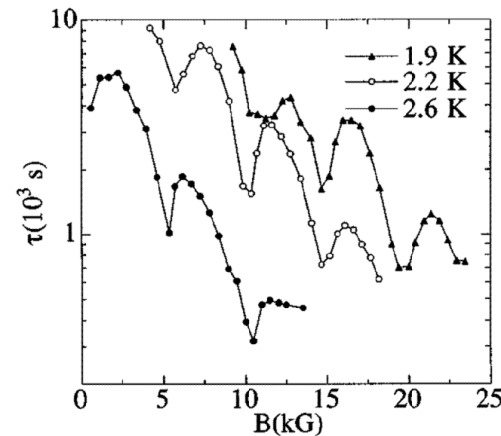


More QTM Experiments

Fominaya, *PRL* **79**, 1126 (1997)



Tejada, *Europhys. Lett.* **35**, 301 (1996)



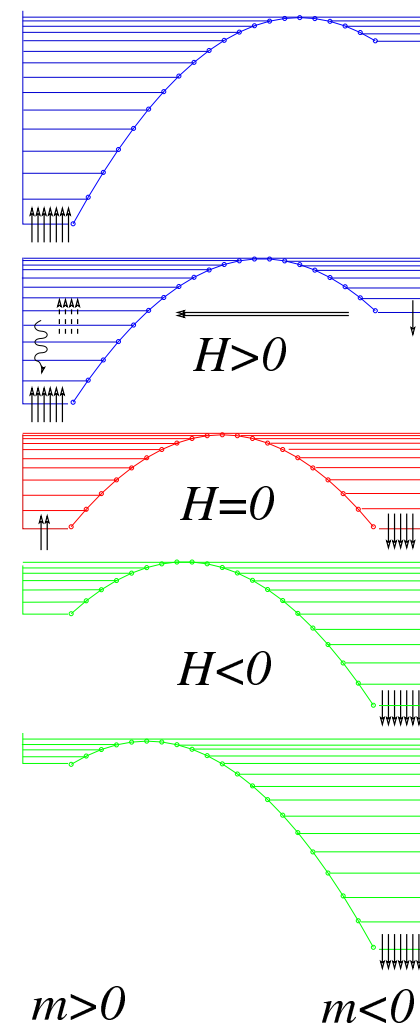
- The heat capacity of Mn_{12} single crystal shows **peaks at regular intervals** of magnetic field.
- The relaxation rate of the magnetization decreases drastically at regular intervals of magnetic field.

A Simple Model for QTM

- At low T the Hamiltonian for a single molecule is

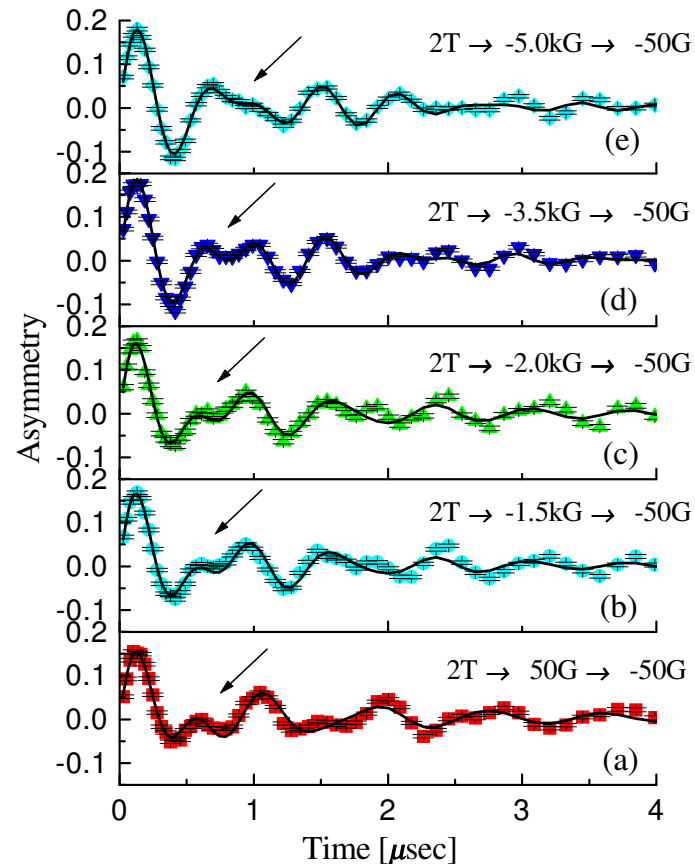
$$\mathcal{H} = -DS_z^2 - g\mu_B H_z S_z$$

- Transition is due to quantum tunneling only.
- Tunneling occurs when two states on both sides have **the same energy**.
- Matching of energy levels is achieved when $H_z = \frac{nD}{g\mu_B}$



μ SR in Fe₈

- All measurements were performed at **40 mK**.
- We apply $H = 2$ T for 30 minutes.
- We sweep the field $H \rightarrow H_i \rightarrow -50$ Gauss.
- All measurements are performed at $H = -50$ Gauss.
- The asymmetry is different only if different matching fields $H_{\text{match}} = 0, 2.1, 4.2, \dots$ kG are crossed.



Problem

- The Hamiltonian of HSM is

$$\mathcal{H} = -DS_z^2 - g\mu_B H_z S_z$$

- \mathcal{H} commutes with S_z

$$[\mathcal{H}, S_z] = 0$$

therefore S_z should be **conserved**.

What induces tunneling ??

Theory of QTM

- In order to have tunneling **additional terms** \mathcal{H}_\perp should be added to the spin Hamiltonian.
- Possibilities are:
 1. High order spin terms and crystal field.
 2. Transverse field.
 3. Spin-phonon interaction.
 4. Dynamic nuclear spins and dipolar interaction.
- We are interested in the **dependence of tunneling on the spin value S .**

Proposed Mechanisms

- Crystal Field: $\mathcal{H}_\perp = -\frac{g\mu_B}{2} \sum_{n=1}^N h_n (S_+^n + S_-^n)$

$$\tau^{-1} = \frac{DS\hbar}{\pi} \left(\frac{g\mu_B h_N (S\hbar)^{N-2}}{2D} \right)^{2S/N}$$

van Hemmen, *Europhys. Lett.* **1**, 481 (1986).

- Transverse Field: $\mathcal{H}_\perp = -g\mu_B H_x S_x$

$$\tau^{-1} = \frac{2D}{\pi[(2m-1)!]^2 \hbar} \frac{(S+m)!}{(S-m)!} \left(\frac{g\mu_B H_x}{2D} \right)^{2m}$$

Chudnovsky, *PRL* **79**, 4469 (1997).

- Spin-Phonon: $\mathcal{H}_\perp \propto (S_k S_l + S_l S_k)$

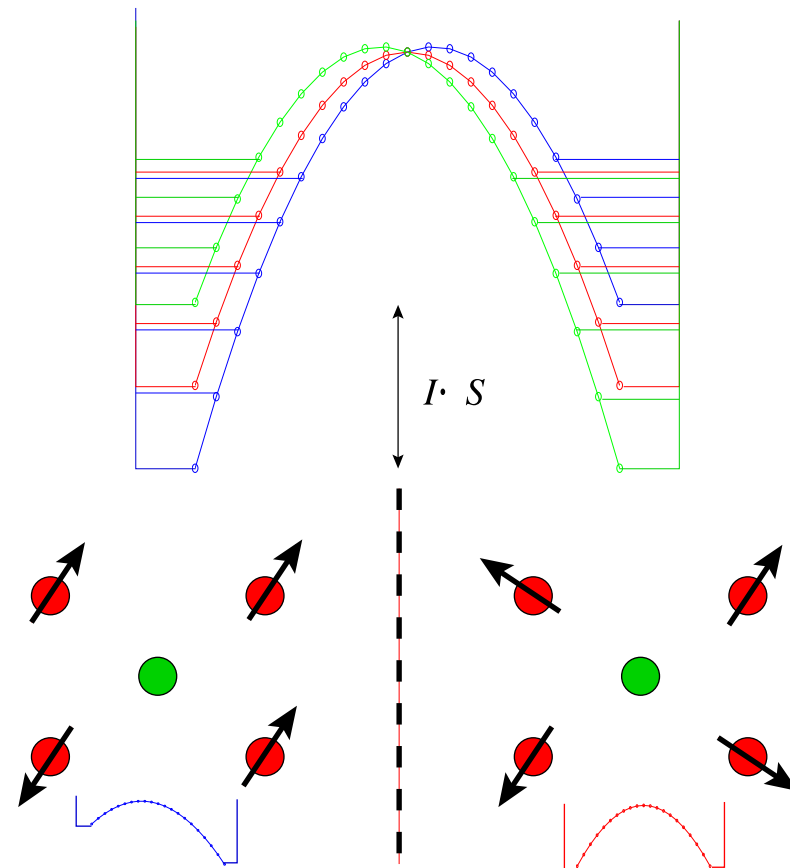
$$\tau^{-1} = \frac{12}{\pi^2 \hbar^4 c^5 \rho} | \langle S | \mathcal{H}_\perp | -S \rangle |^2 (H_z S)^3$$

Hartmann Boutron, *PRL* **75**, 537 (1995).

Dynamic Nuclear Spins and Dipolar Interaction

- Dipolar fields bring the spin states of the molecules **out of resonance**.
- Rapidly fluctuating hyperfine fields bring molecules initially **to resonance**.
- Tunneling changes the dipolar fields and **brings more molecules to resonance**.
- The tunneling rate in this case is

$$\tau^{-1} \propto \frac{\Delta_0^2 T_2 |E_S - E_{-S}|}{E_D}$$



Prokofév, *PRL* 80,5794 (1998).

Strategy

- The Hamiltonian of anisotropic HSM is

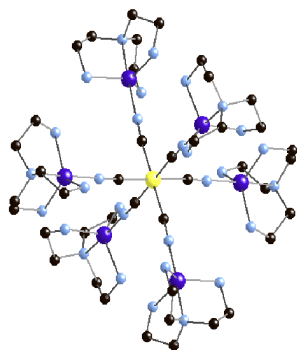
$$\mathcal{H} = -DS_z^2 - g\mu_B H_z S_z + \mathcal{H}_\perp$$

- For isotropic HSM $D \rightarrow 0$

$$\mathcal{H} = -g\mu_B H_z S_z + \mathcal{H}_\perp$$

We can probe \mathcal{H}_\perp directly!

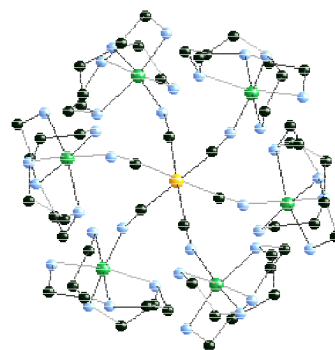
Isotropic High Spin Molecules



$$S = 9/2$$

$$J_{\text{Cr-Cu}} = 77\text{K}$$

$$S_{\text{Cu}} = 1/2$$

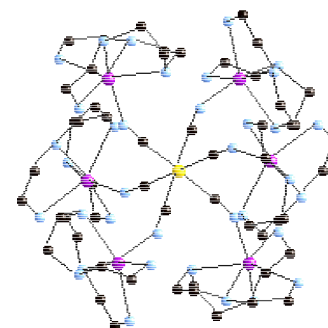


$$S = 15/2$$

$$J_{\text{Cr-Ni}} = 24\text{K}$$

$$S_{\text{Ni}} = 1$$

$$S_{\text{Cr}} = 3/2$$



$$S = 27/2$$

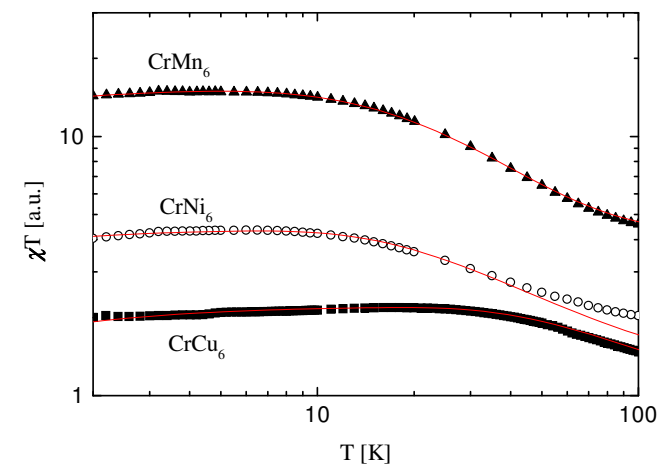
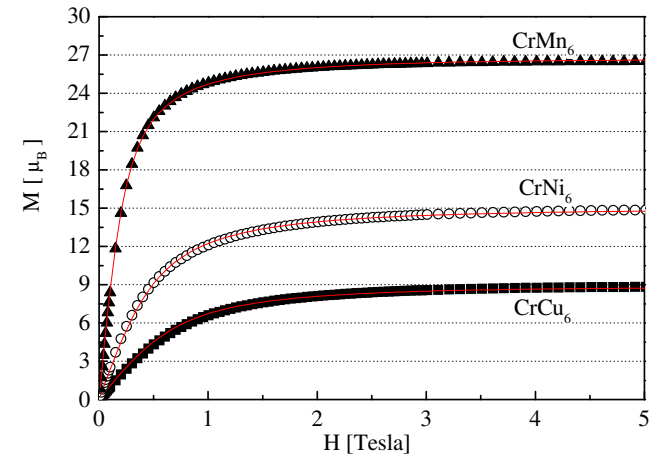
$$J_{\text{Cr-Mn}} = -11\text{K}$$

$$S_{\text{Mn}} = 5/2$$

Magnetic Properties

- At high H and $T = 2$ K the magnetization per molecule saturates giving the value of S .
- M vs. H follows the Brillouin function of the corresponding S .
- At low H and low T the susceptibility saturates and shows no anisotropy.
- The susceptibility follows that expected from the Hamiltonian

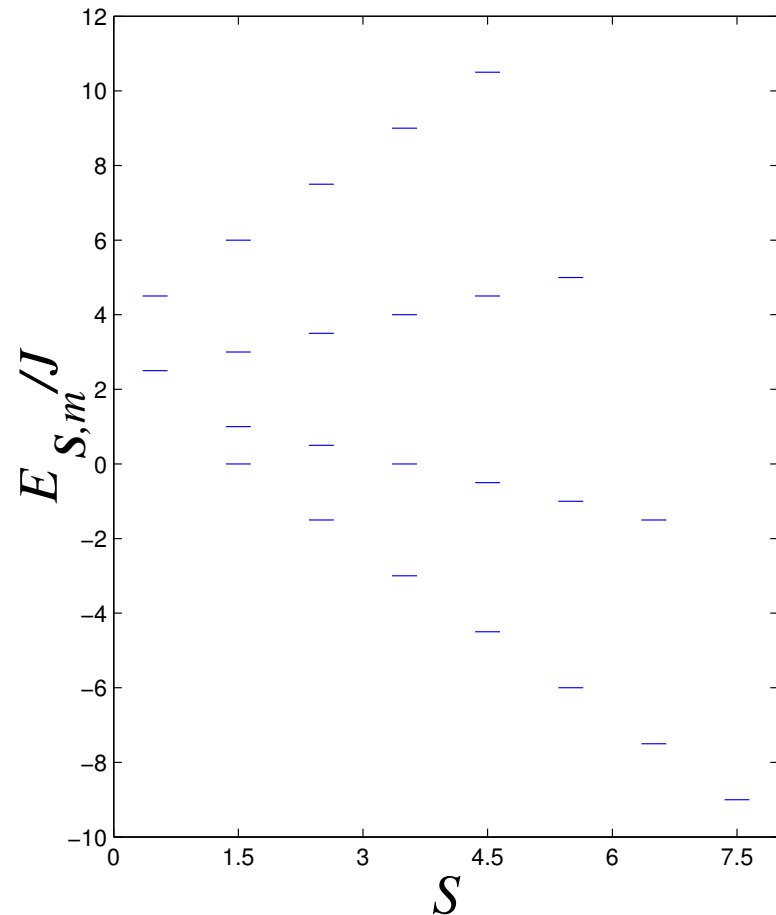
$$\mathcal{H} = -J \sum_{i=1}^6 \vec{S}_0 \cdot \vec{S}_i - g\mu_B \vec{H} \cdot \sum_{i=0}^6 \vec{S}_i$$



Calculation of the Susceptibility

- We diagonalize the Hamiltonian \mathcal{H}
- We find the eigenstates $|S, m\rangle$ and eigenvalues $E_{S,m}$.
- The susceptibility is

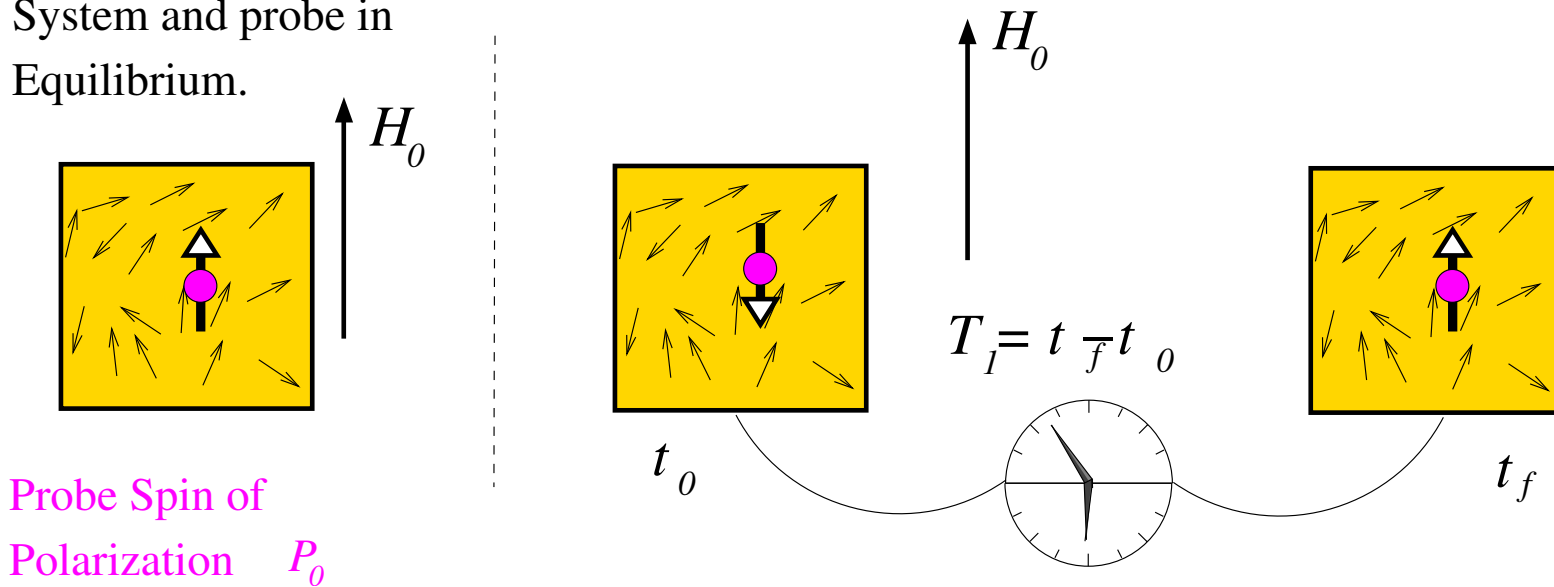
$$\chi = \sum_{|S,m\rangle} \frac{m e^{-\frac{E_{S,m}}{T}}}{Z H}$$



Spin Lattice Relaxation Time

- It is the time that takes a probing spin to reach equilibrium

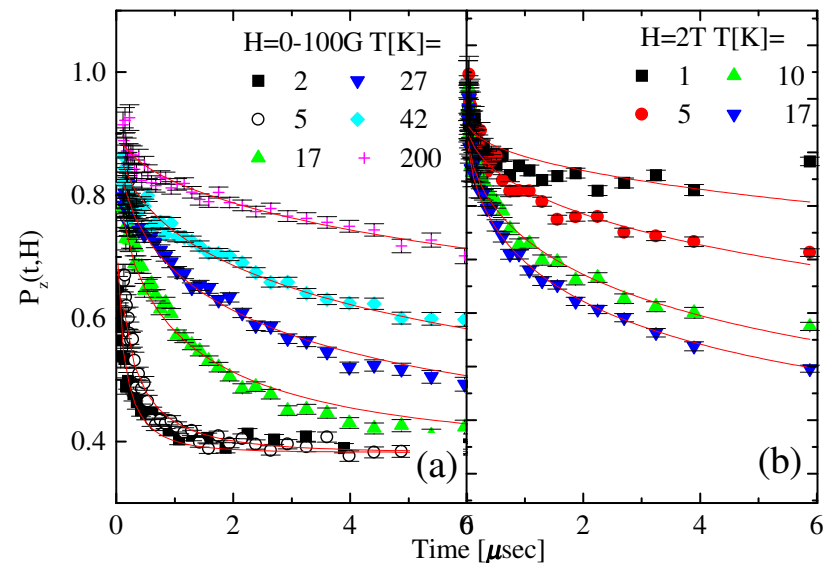
System and probe in
Equilibrium.



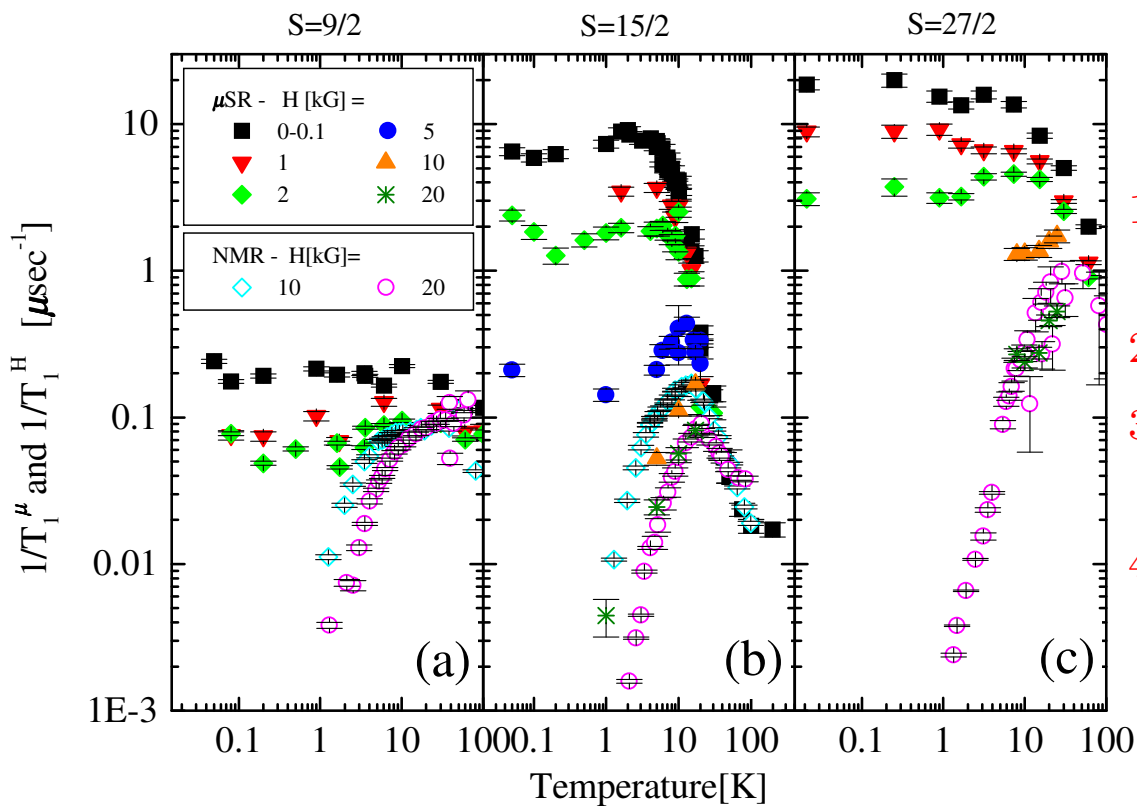
- In μ SR $P_0 = 1$ and $P_f = 0$ while in NMR $P_0 = 0$ and $P_f = 1$.
- Only fluctuating fields $\vec{B}(t)$ contribute.
- Only transverse fluctuations B_{\perp} contribute.

T Dependence of the μ^+ Polarization

- At $H = 0$ the muon polarization relaxation increases with decreasing temperature down to 5 K and then saturates.
- At $H = 2$ T and temperatures lower than ~ 17 K the relaxation decreases with decreasing T .



μ SR and NMR Results



1. No T dependence at $H \rightarrow 0, T \rightarrow 0$.
2. Scale of T varies.
3. H dependence varies.
4. Different behavior in different H .

- The spin lattice relaxation rate measured by μ SR and NMR at the same external field can be scaled.

The Spin Lattice Relaxation

- In spin lattice relaxation theory one assumes a fluctuating local field $\vec{B}(t)$ experienced by a local probe (muon or nucleus) of spin \vec{I} .
- The spin lattice relaxation time T_1 in this case follows

$$\frac{1}{T_1} = \frac{\gamma^2}{2} \int_{-\infty}^{\infty} dt \langle B_{\perp}(0) B_{\perp}(t) \rangle \exp(i\gamma H t).$$

- The correlation time τ and mean square of the transverse field distribution at the probe site in frequency units Δ^2 are defined by

$$\gamma^2 \langle \mathbf{B}_{\perp}(t) \mathbf{B}_{\perp}(0) \rangle = \Delta^2 \exp(-t/\tau).$$

Field-Field Correlation Time

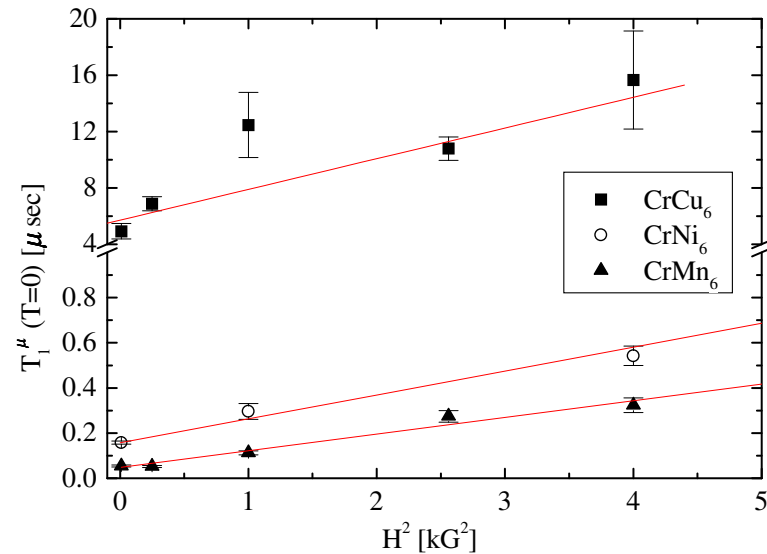
- The spin lattice relaxation rate is

$$\frac{1}{T_1} = \frac{\Delta\tau}{\omega^2\tau^2 + 1}$$

where in our system $\omega = g\mu_B H$.

$$T_1 = \frac{\omega^2\tau^2 + 1}{\Delta\tau}$$

- The value of $T_1(T \rightarrow 0)$ depend linearly on H^2 .



Field-Field Correlation Time

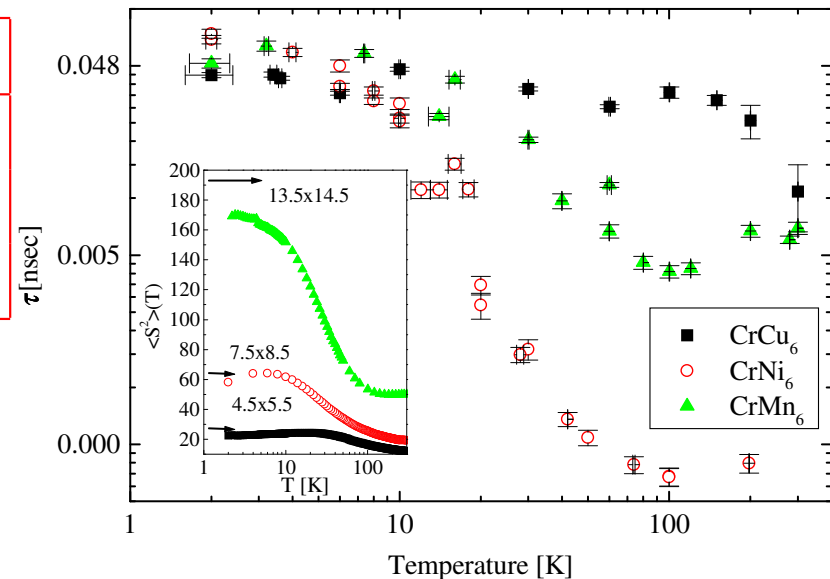
- From the linear fit of $T_1(T \rightarrow 0)$ vs. H^2 we have

	τ_{int} [nsec]	Δ [MHz]
CrCu ₆	0.034(4)	4.9(9)
CrNi ₆	0.053(4)	26(2)
CrMn ₆	0.044(4)	38(2)

- The correlation time at all temperatures follows

$$\tau(T) = \frac{(g\mu_B)^2}{3k_B} \frac{S(S+1)}{T_1(T)T\chi(T)\Delta^2}.$$

- The correlation time depends weakly on S at $T \rightarrow 0$.



Calculation of T_1

- Assuming a coupling $A\vec{I} \cdot \vec{S}$ between the probe \vec{I} and the molecular spin \vec{S} , the spin lattice relaxation rate is

$$\frac{1}{T_1} = \frac{A^2}{2} \int_{-\infty}^{\infty} \langle S_-(t)S_+(0) \rangle e^{i\omega t} dt$$

- For the spin states of \mathcal{H} we obtain

$$\frac{1}{T_1} = \frac{A^2}{2\mathcal{Z}} \sum_{|S,m\rangle} (S(S+1) - m(m+1)) \left(\frac{\tau_{S,m} e^{-\frac{E_{S,m}}{T}}}{1 + \omega'^2 \tau_{S,m}^2} \right)$$

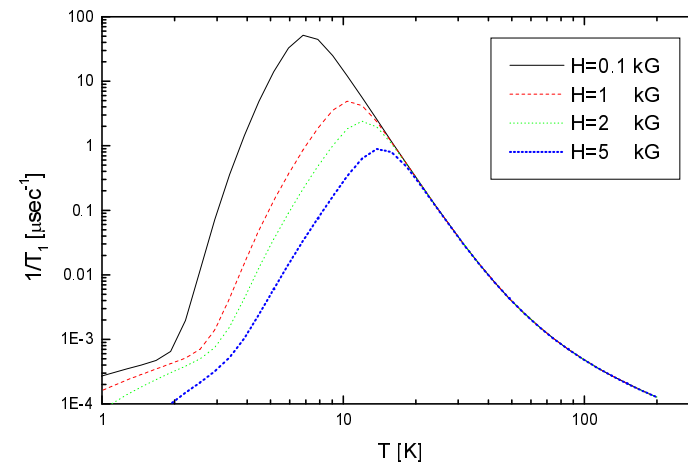
where $\tau_{S,m}$ is the lifetime of the level $|S, m\rangle$ and $\omega' = (\gamma - g\mu_B/\hbar)H \simeq -g\mu_B H/\hbar$.

1/T₁ Due to Spin-Phonon Interaction

- Assuming that the finite lifetime of the levels is due to **spin-phonon** interaction

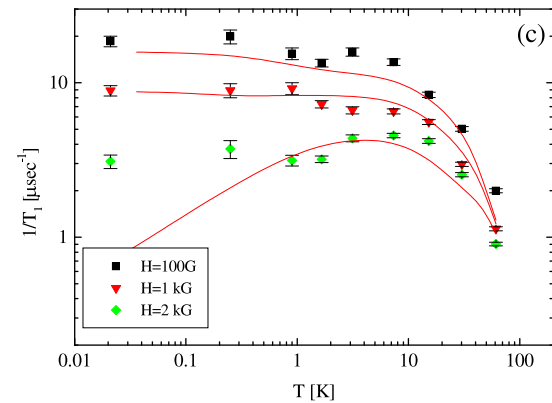
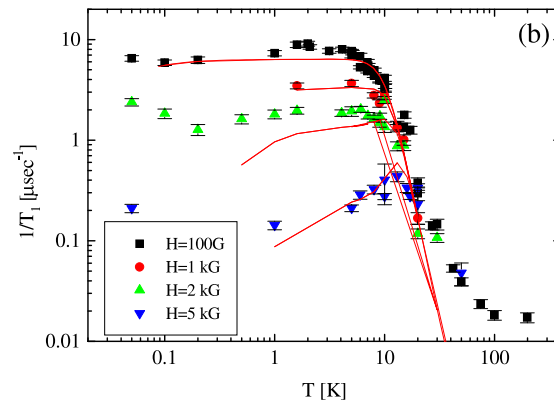
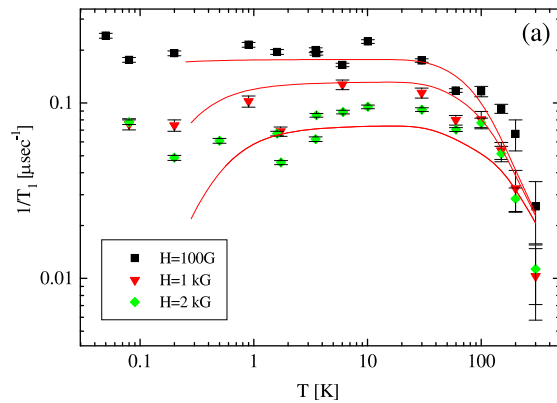
$$\tau_{sp}^{-1} = \frac{C(E_{S,m} - E_{S',m'})^3}{\exp[(E_{S,m} - E_{S',m'})/T] - 1}$$

- The behavior is similar to the experimental data at high T but differs at $T \rightarrow 0$.



Additional Constant Fluctuations

- To reproduce $1/T_1$ at low temperatures and low fields we assume $\frac{1}{\tau_{S,m}} = \frac{1}{\tau_{sp}} + \frac{1}{\tau_{int}}$ where τ_{int} is constant.



- With this we improve the agreement.

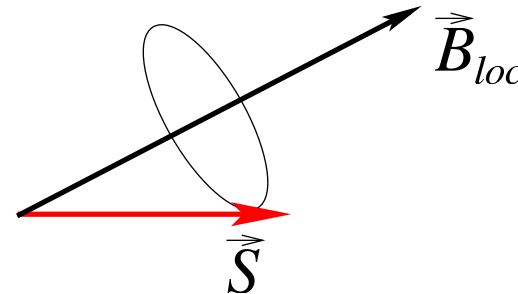
Discussion

- The correlation time τ_{int} depends weakly on S , ruling out crystal field and dipolar interactions.
- We have seen that spin-phonon interaction cannot account for the finite $1/T_1$ at low T .
- We are left with fluctuating hyperfine interaction
 $\vec{B}_{mol} = a\vec{i}(t) \cdot \vec{S}$.

Consider the Bloch equation

$$\frac{d\vec{S}}{dt} = g\mu_B [a\vec{i}(t) \times \vec{S}]$$

which is independent of S .



Conclusion

- The spin lattice relaxation in HSM is temperature independent at low temperatures.
- The spin-spin correlation time at low temperatures depends weakly on the molecular spin S .
- The molecular spin dynamics at high temperature is driven by spin phonon interaction, while dynamically fluctuating hyperfine fields induce the molecular spin dynamics at very low temperatures.

$$\mathcal{H}_{\perp} \propto \vec{i} \cdot \vec{S}$$

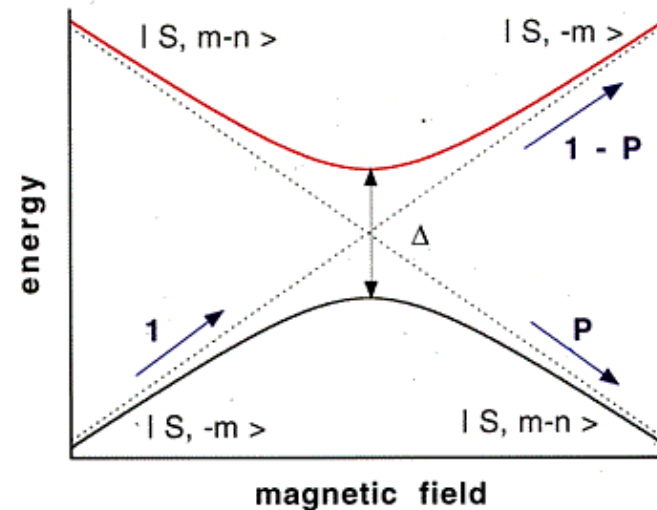
Landau-Zener Tunneling

- Landau-Zener model is used for experiments with swept external magnetic field.

- The tunneling probability is

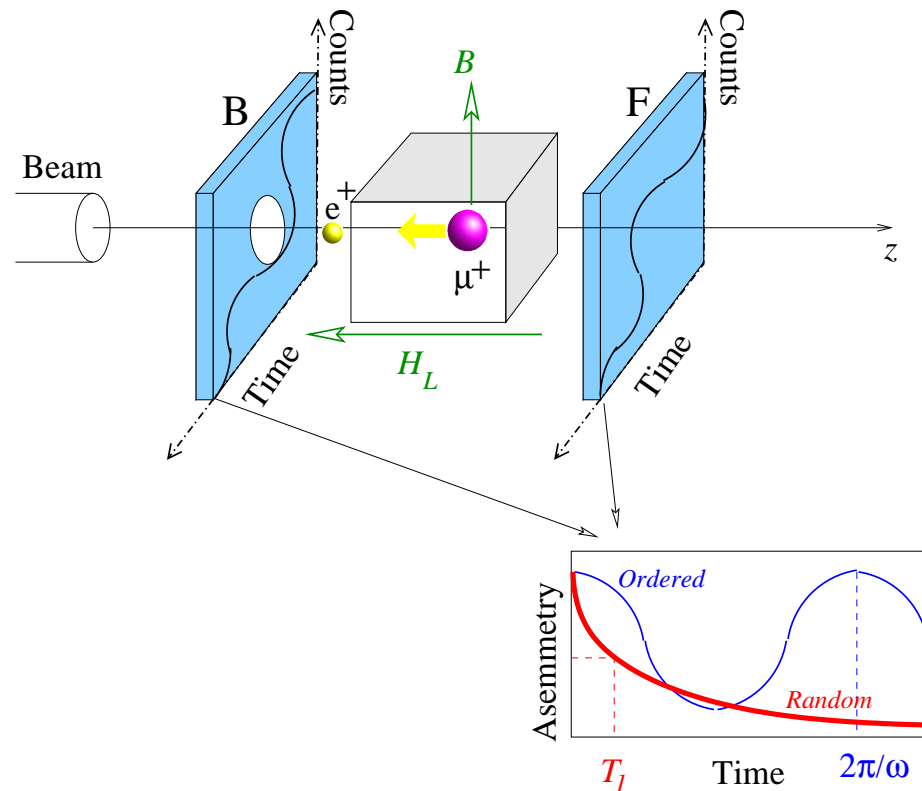
$$P = 1 - \exp \left[-\frac{\pi \Delta}{4 \hbar g \mu_B S (dH/dT)} \right]$$

where Δ is the gap at the level crossing (tunnel splitting).



The μ SR Technique

- The muons are **100% polarized**.
- The **positrons** are emitted parallel to the muons polarization.
- Histograms of positron counts vs. time are collected in the F/B counters.
- The **Asymmetry** $= \frac{F-B}{F+B}$ is proportional to the **polarization**.
- Zero field, Longitudinal or transverse field can be applied.



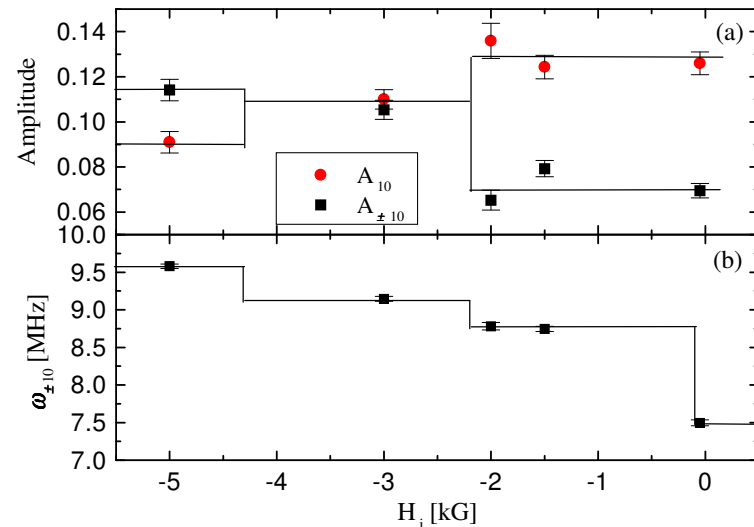
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μ SR in Fe₈

- We fit the asymmetry to

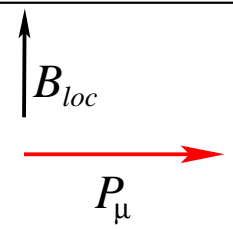
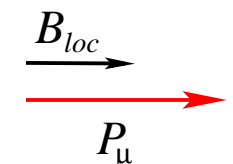
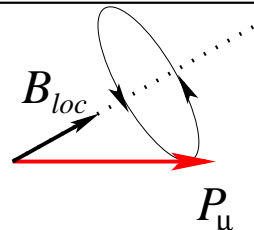
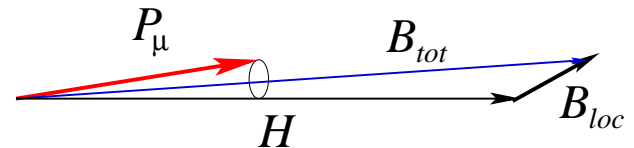
$$A(t) = A_{10} \sin(\omega_{10}t)e^{-\lambda_{10}t} + A_{\pm 10} \sin(\omega_{\pm 10}t)e^{-\lambda_{\pm 10}t}$$

- A_{10} , ω_{10} and λ_{10} represents the fraction of μ^+ near $m = +10$ state.
- $A_{\pm 10}$, $\omega_{\pm 10}$ and $\lambda_{\pm 10}$ represent the fraction of μ^+ near $m = \pm 10$ state.
- **Steps** in the value of $\omega_{\pm 10}$, A_{10} and $A_{\pm 10}$ coincide with the matching field values.



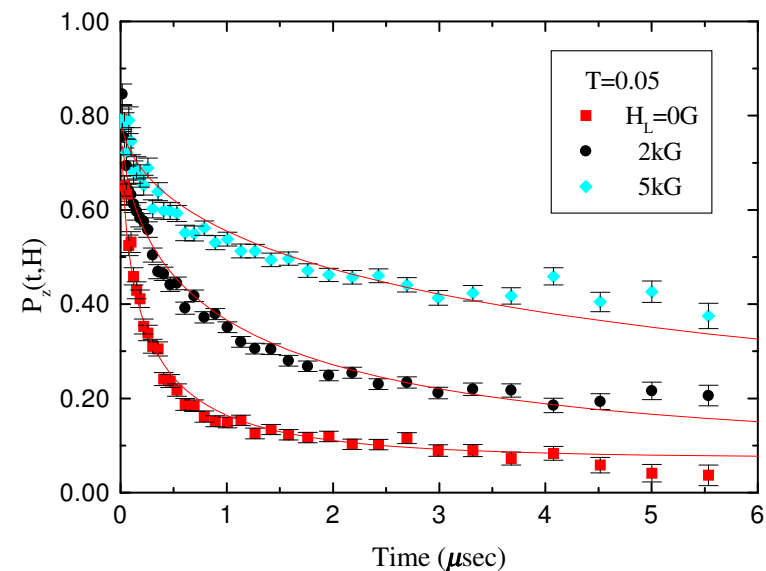
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Muon Spin Relaxation in a Static Field

Time scale of relaxation	Recovery in zero field	Decoupling in high longitudinal field
$t^{-1} \simeq \gamma \sqrt{\langle B_{loc}^2 \rangle}$	<div style="text-align: center;">  </div> <div style="text-align: center; margin-top: 20px;">  </div> $\lim_{t \rightarrow \infty} P_z(t) = \frac{1}{3}$	<div style="text-align: center;">  </div> <div style="text-align: center; margin-top: 20px;">  </div> $\lim_{H \rightarrow \infty} P_z(t) = 1$

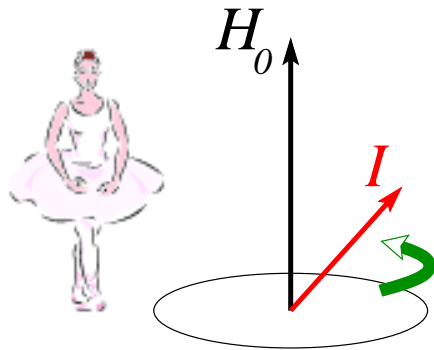
H Dependence of the μ^+ Polarization

- The μ SR results in CrNi_6 at $T = 50$ mK show that
 1. There is no recovery, unlike the static local field case.
 2. The relaxation time scale is $1 \mu\text{sec}$, and therefore $\sqrt{B_{loc}^2}$ should be ~ 10 G.
 3. Decoupling should occur at $H \sim 100$ G, but even at 5 kG there is no decoupling.

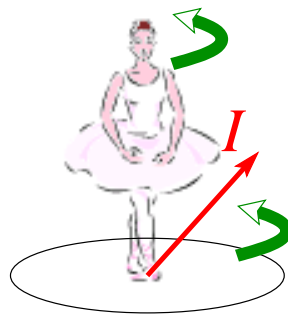


We conclude that even at 50 mK the CrNi_6 spins are dynamically fluctuating.

Principle of NMR

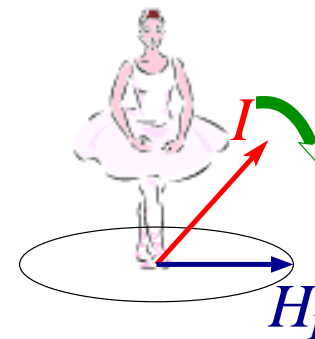


Ballerina watching spin rotating.



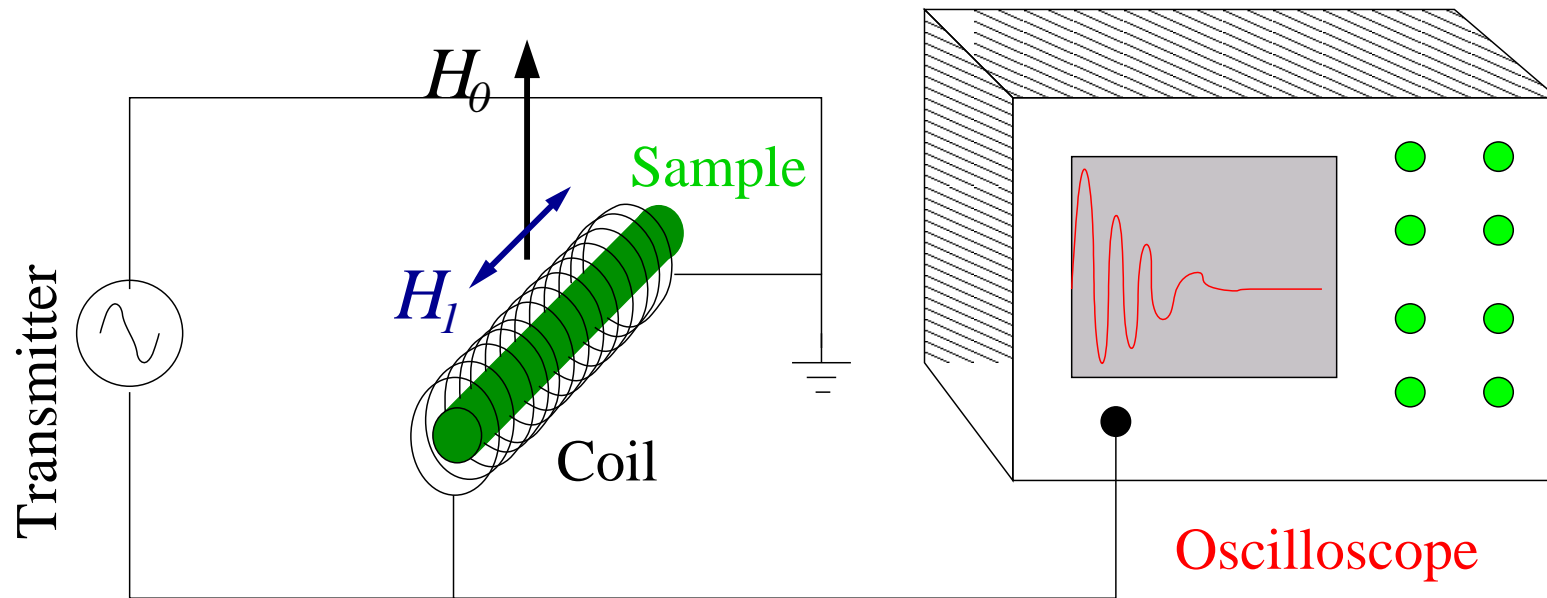
Ballerina and spin are rotating. From her point of view the spin is fixed so there is no field.

Back



A rotating field H_1 is applied. Ballerina sees a fixed field so the spin is rotating around it.

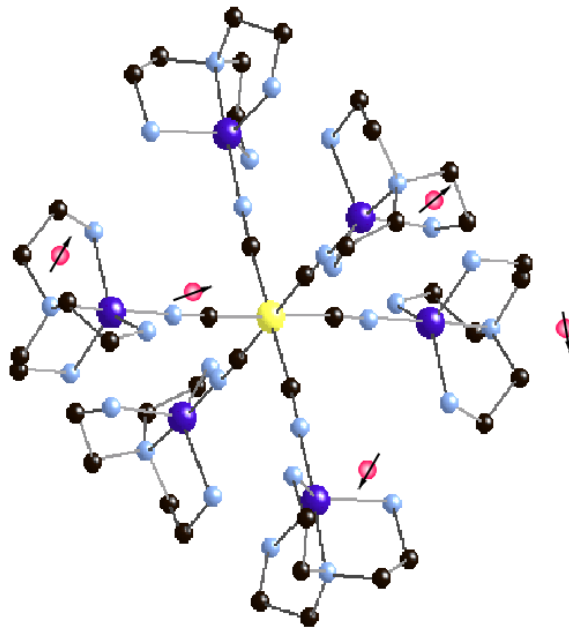
Principles of NMR



Back

The Polarization in Isotropic HSM

- In these HSM the muon could occupy many different sites in the sample as a result one must average over Δ .



- The polarization of a local probe, in the fast fluctuation $\tau\Delta \ll 1$, is given by

$$P(H, t) = (P_0 - P_\infty) e^{[-t/T_1]^\beta} + P_\infty$$

The Spin Dependence of the Tunneling Rate

<i>Interaction</i>	<i>Spin dependence of the tunneling rate τ^{-1}</i>
High order spin terms	S^2 or higher
Spin-phonon	S^3
Static transverse field	higher than S^2
Dynamic hyperfine and dipolar	$1/S$