



Entanglement on demand: Time reordering



Bisker, Gershoni, Lindner,
Meirom, Warburton

Bell states

$$|0\rangle_A \otimes |1\rangle_B \pm |1\rangle_A \otimes |0\rangle_B$$

$$|0\rangle_A \otimes |0\rangle_B \pm |1\rangle_A \otimes |1\rangle_B$$

Maximally entangled
Good for Quantum information



@ B. Bellamy 02



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Qubits

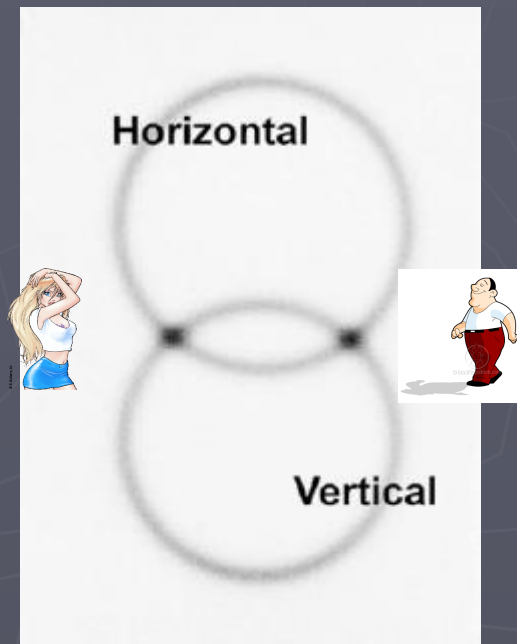
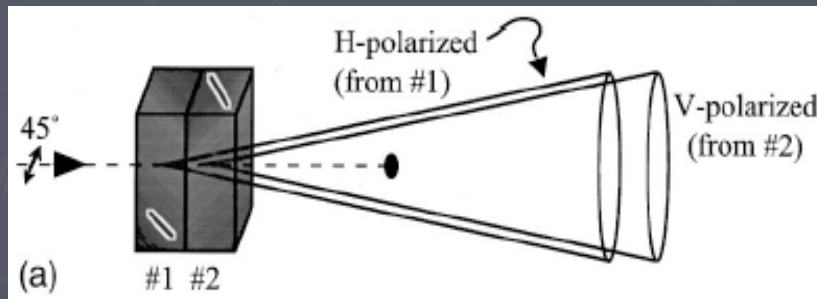
Flying quabits: Photons
Storage qubits: Nuclear spin
Working qubits: Electronic states

Photons: encode qubit in polarization

$$|0\rangle = |H\rangle, \quad |1\rangle = |V\rangle$$

Down conversion

Nonlinear optics: $a_{2k,D}^\dagger |0\rangle \longrightarrow a_{k,H}^\dagger a_{k,V}^\dagger |0\rangle$



$$|V\rangle_A \otimes |H\rangle_B + |H\rangle_A \otimes |V\rangle_B$$

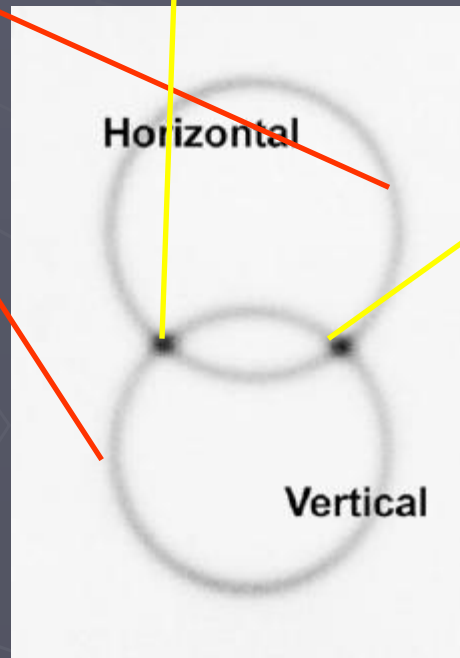
Which path ambiguity

On demand

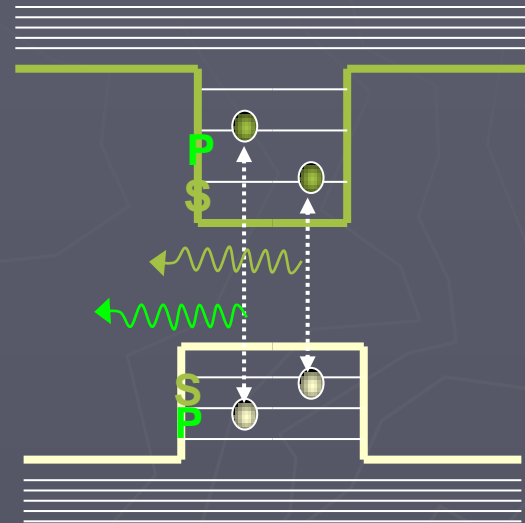
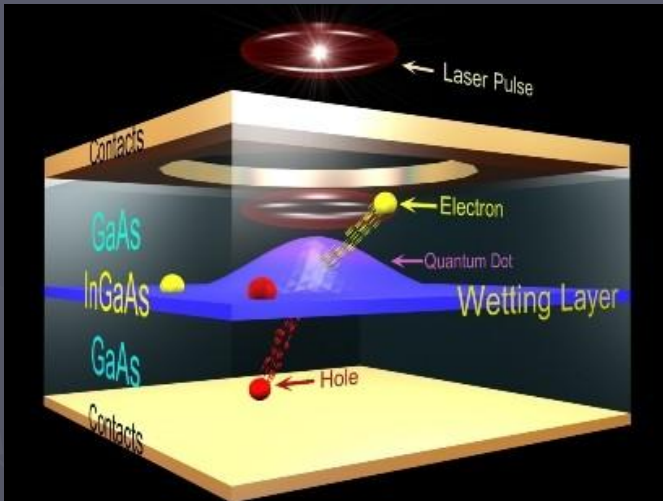
$$|0\rangle \otimes |0\rangle + \varepsilon(|V\rangle \otimes |H\rangle + |H\rangle \otimes |V\rangle)$$

junk

Entangled piece



Quantum dots

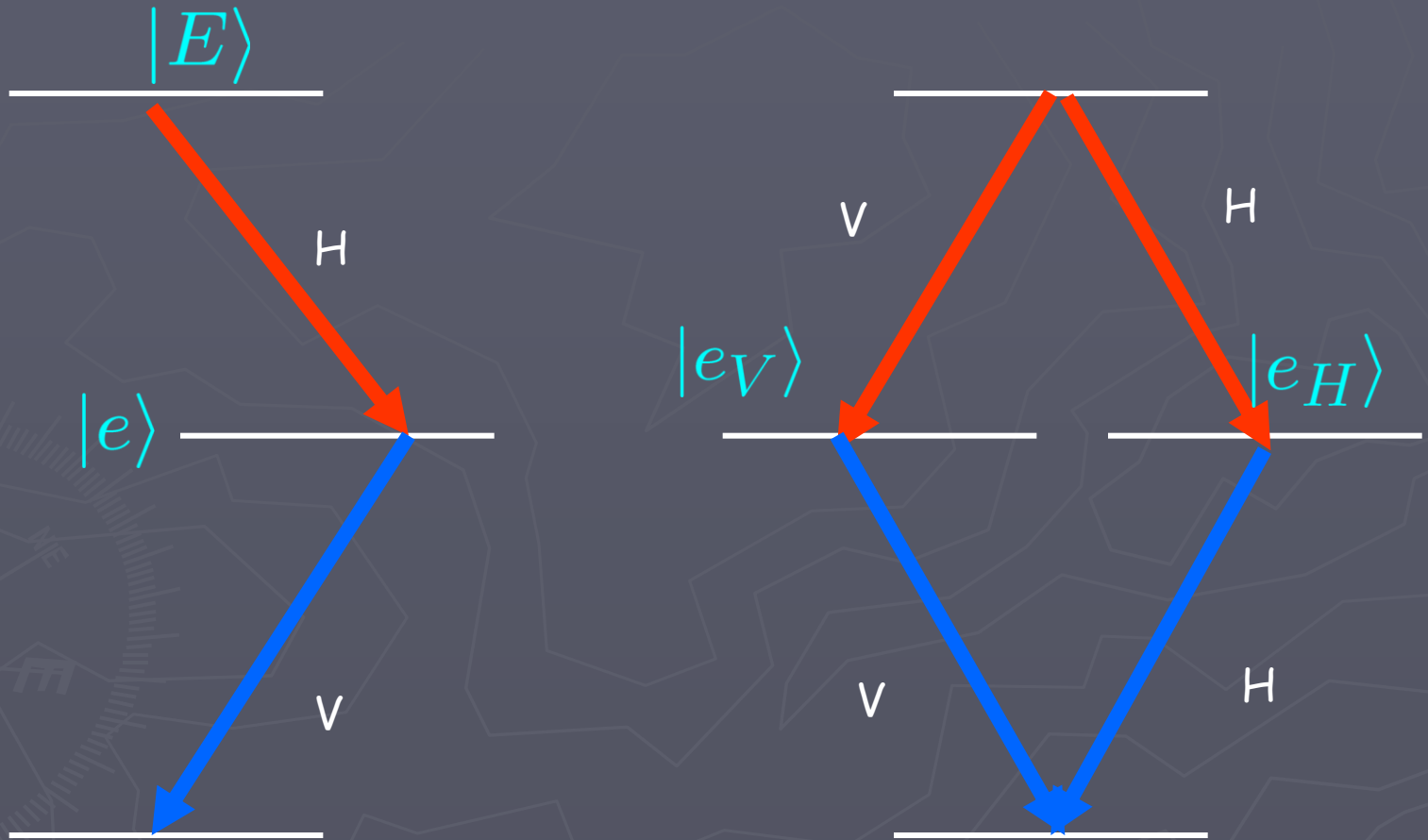


$$|e\rangle = |eh\rangle, \quad |E\rangle = |(eh)^2\rangle$$

photon zap $\rightarrow |(eh)^2\rangle \rightarrow |photon\ pair\rangle$

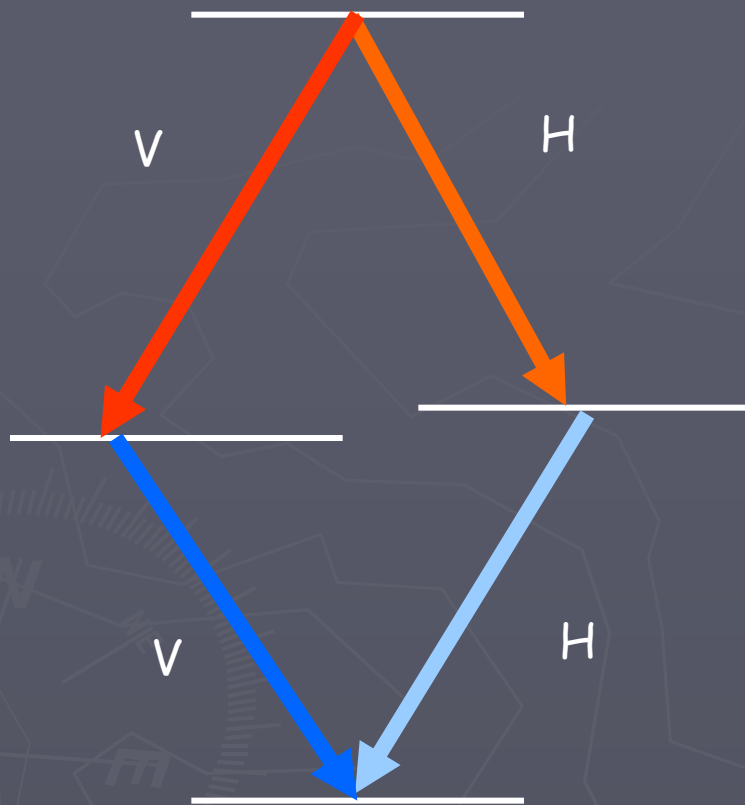
Can one entangle the pair?

Which path and entanglement

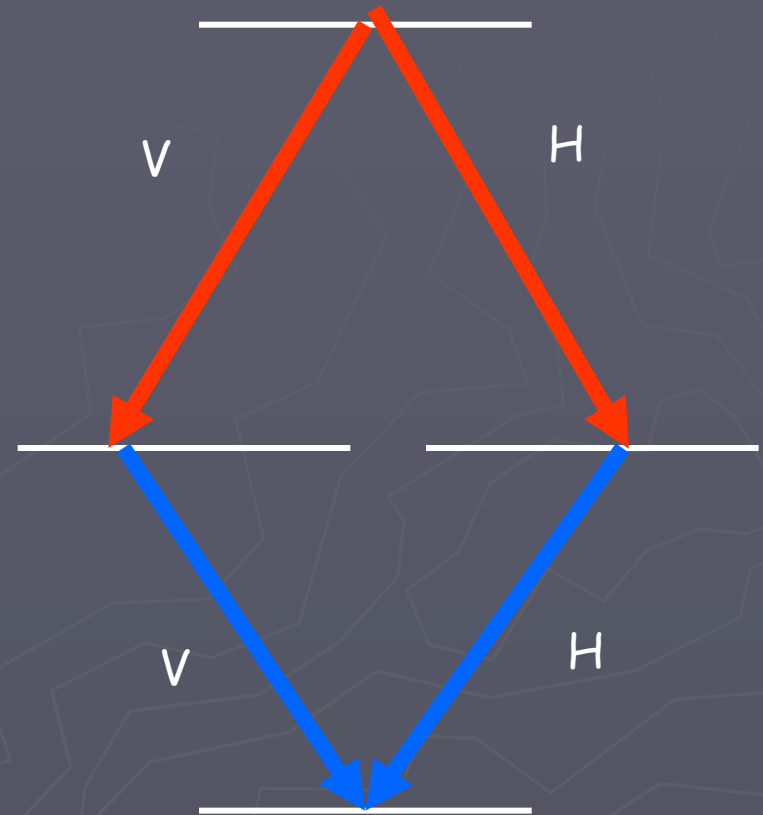


Entanglement: A 2 photon analog of interference

Color monitors the cascade



Monitored by color



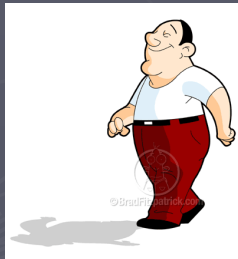
Un-monitored

Monitoring: Kills ambiguity and entanglement

What is entanglement?

Classical vs quantum probabilities

independence $P_{ab}(j, k) = P_a(j)P_b(k)$



Correlations due to common preparation

$$P_{ab}(j, k) = \sum_{\alpha} p_{\alpha} P_a^{\alpha}(j) P_b^{\alpha}(k)$$

Classical probabilities

Any probability distribution is a weighted sum of independent

$$P(j, k) = \sum_{\alpha\beta} P(\alpha, \beta) \delta_{j,\alpha} \delta_{k,\beta}, \quad P(\alpha, \beta) > 0$$

Independent (sure) events

Common preparation

Quantum probabilities

Quantum independence

$$\rho_A \otimes \rho_B \longrightarrow \text{Prob}(j, k) = \text{Tr}_A(\rho_A P_j) \text{Tr}_B(\rho_B P_k)$$

Correlations due to common preparation

$$\rho = \sum_i p_i \rho_A^i \otimes \rho_B^i, \quad p_i > 0$$

Separable states

States that are not separable are entangled

Entangled states

Separable states

$$\rho = \sum_i p_i \rho_A^i \otimes \rho_B^i, \quad p_i > 0$$

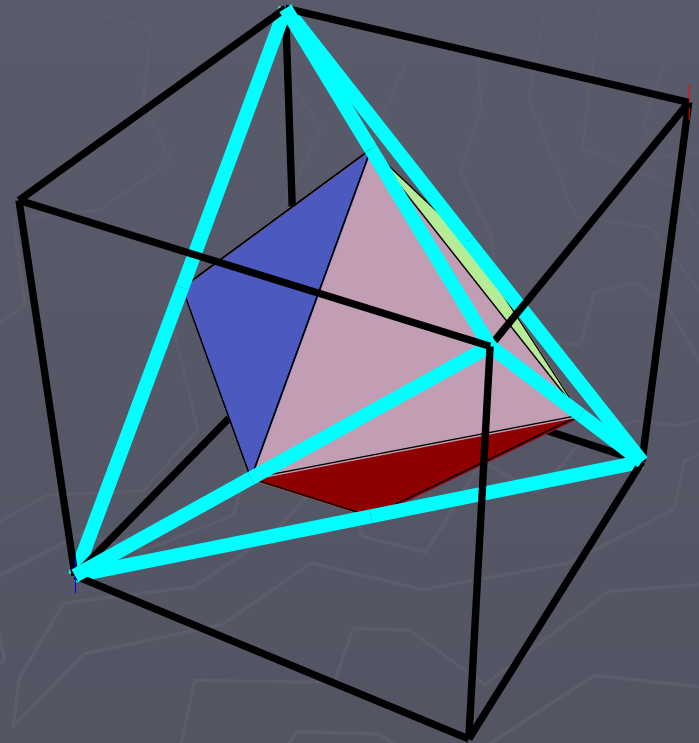
Independent up to common preparation

There are states, $\rho > 0$, that are not separable!

Definition: States that are not separable are entangled

Separable and entangled states

Octahedron=separable
Tetrahedron=all states



Horodecki's, Leinaas Myrheim Uvrom, Kenneth Avron, Bisker

Entanglement (Peres) test



$$\rho = \begin{pmatrix} A & B \\ D & C \end{pmatrix}, \quad \rho^P = \begin{pmatrix} A & D \\ B & C \end{pmatrix}$$

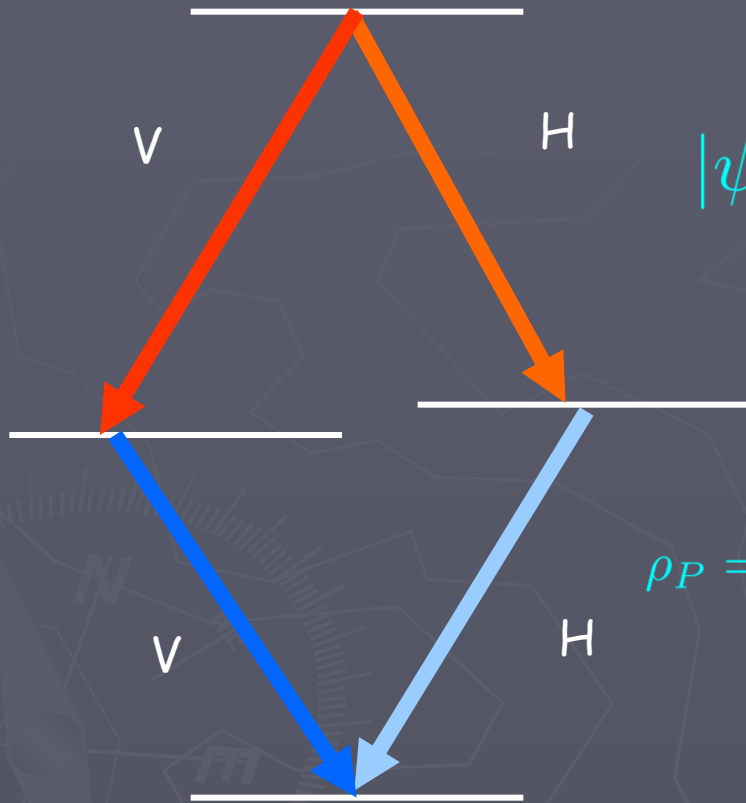
If transform has negative eigenvalue state is entangled

Example: Bell state

$$\rho = \frac{1}{2} \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \quad \rho^P = \frac{1}{2} \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{pmatrix}$$

Negative eigenvalue is a measure of entanglement

How monitoring kills entanglement



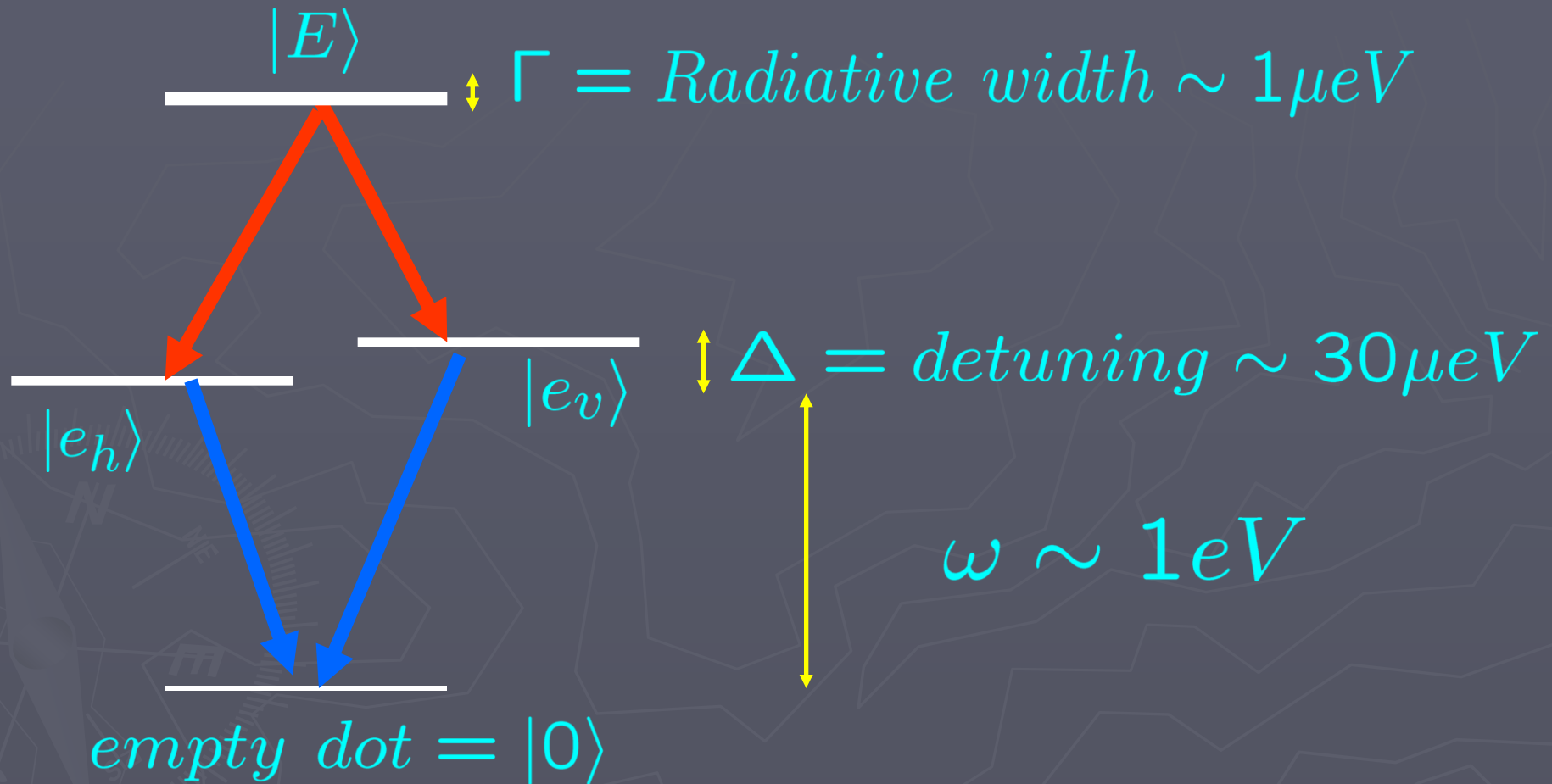
$$|\psi\rangle = |f\rangle_C |HH\rangle_P + |g\rangle_C |VV\rangle_P$$

$$\rho_P = \text{Tr}_C(|\psi\rangle\langle\psi|) = \frac{1}{2} \begin{pmatrix} 1 & 0 & 0 & \langle f|g\rangle \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ \langle g|f\rangle & 0 & 0 & 1 \end{pmatrix}$$

$|\langle f|g\rangle|$ is a measure of entanglement



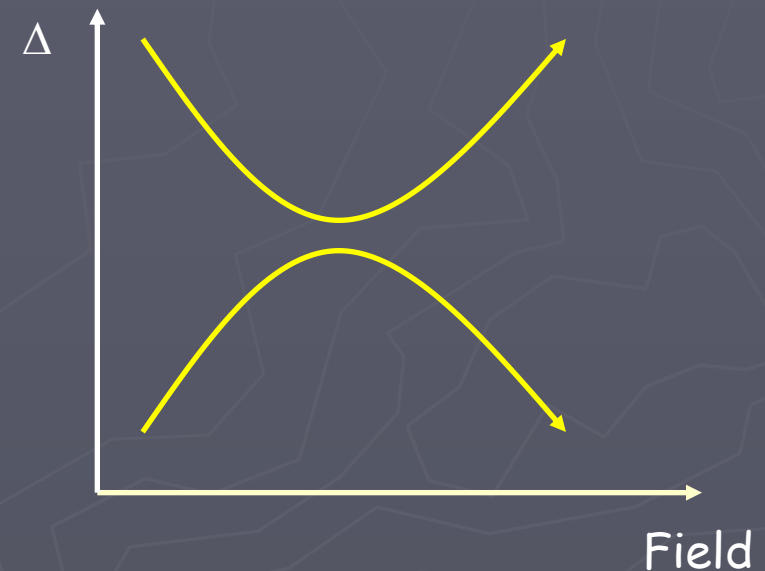
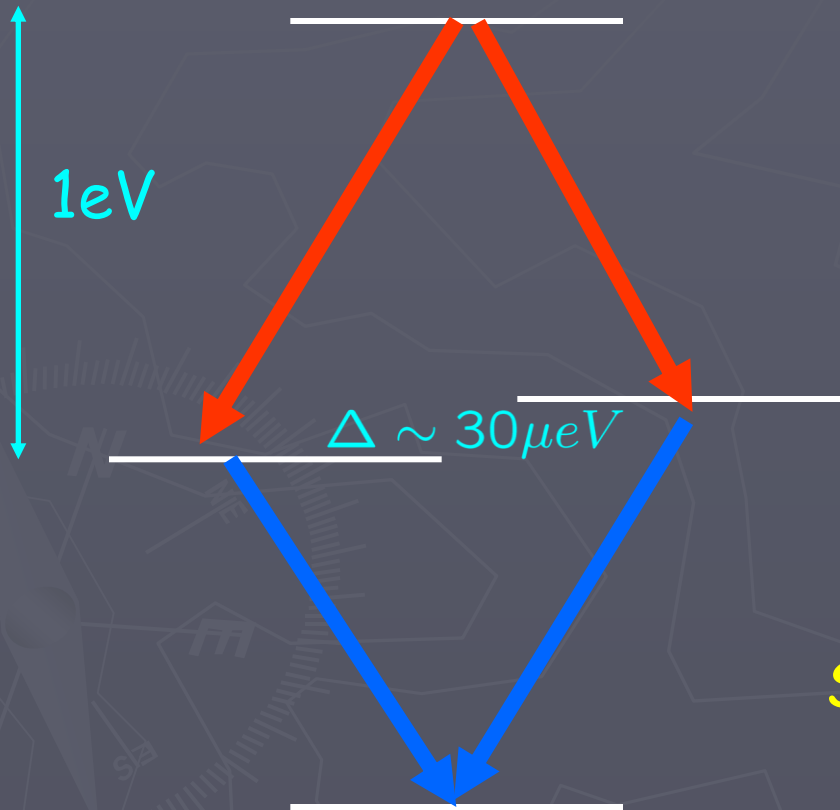
Monitoring: Energy scales



Entanglement needs $\Gamma > \Delta$

Why making Δ small is hard

Principle of level repulsion

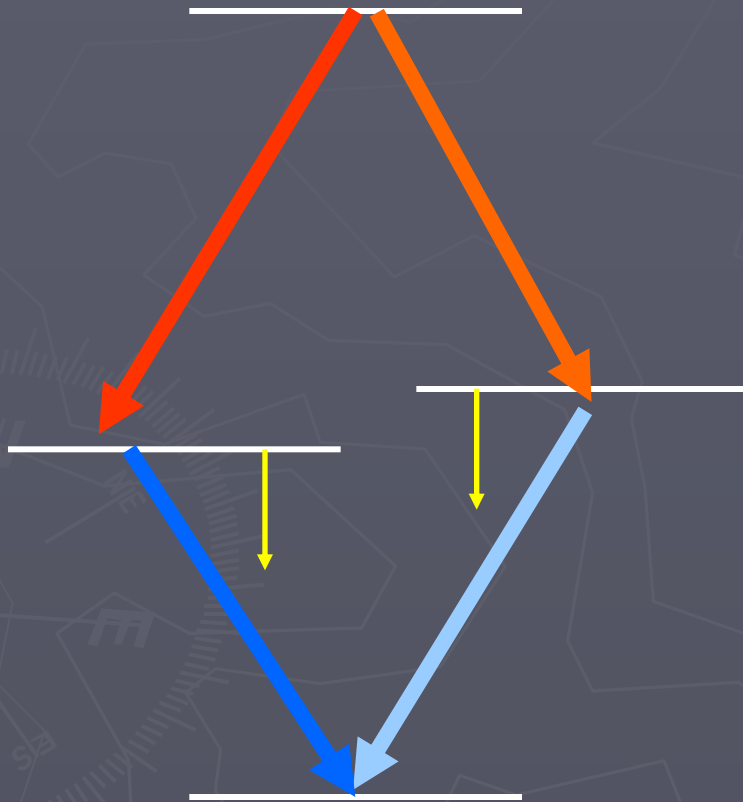


Spin-Orbit: Protected subspace

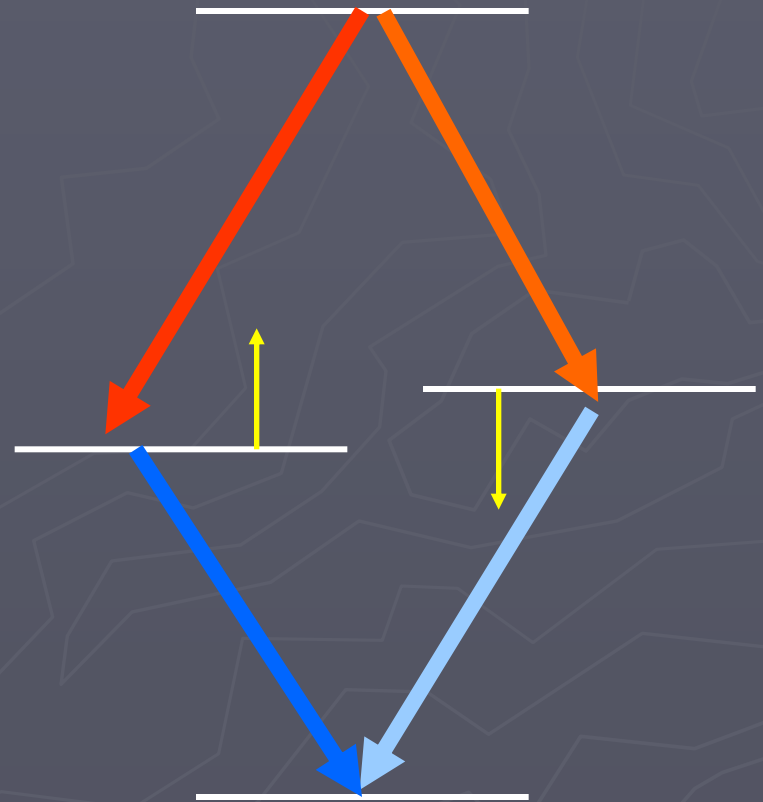
Forcing degeneracy: Stevenson et. al. , Hafenbrak et. al.

Life in protected subspace

Δ is due to spin orbit interaction - Relativistic effect



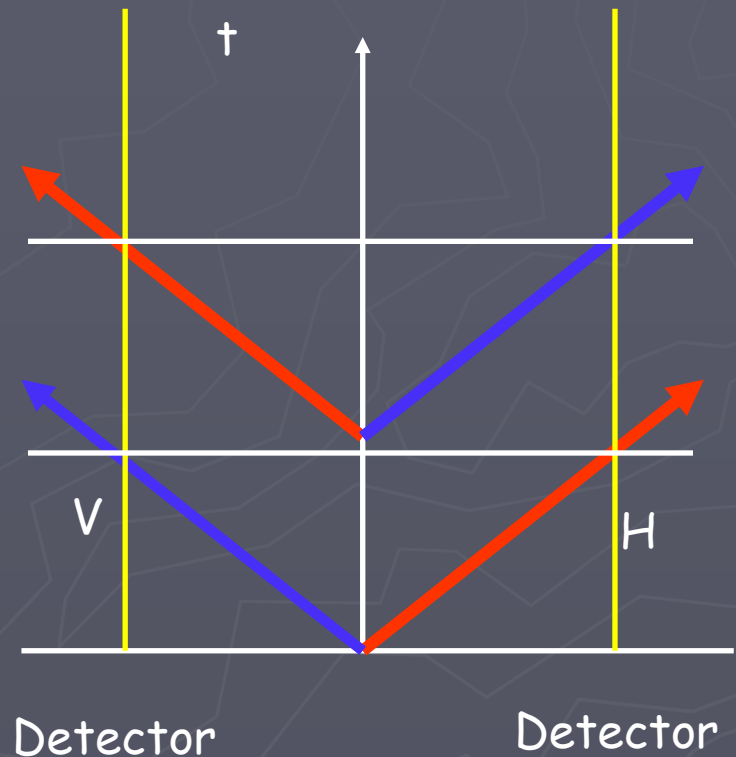
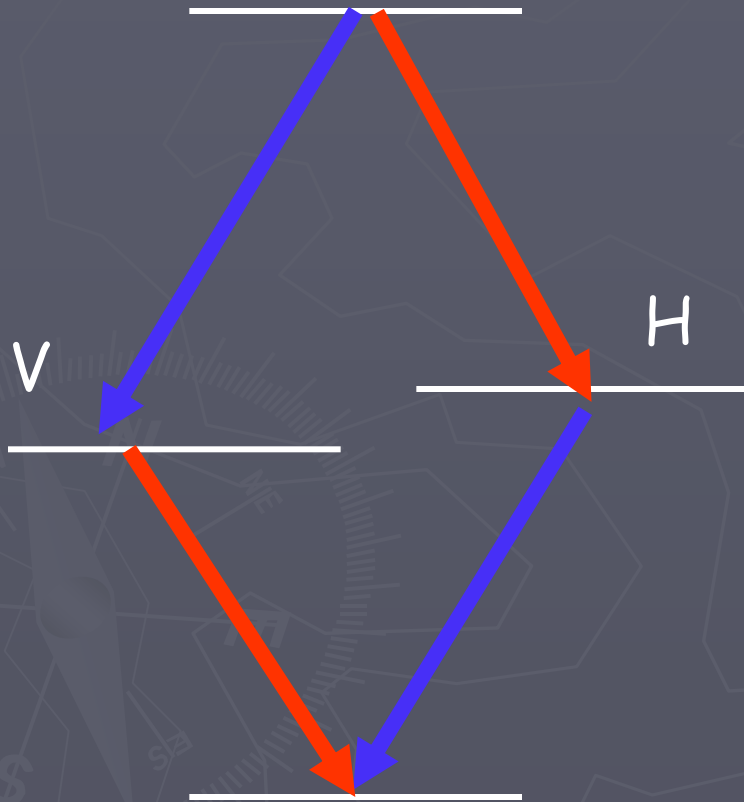
In principle easy



In principle hard

Ambiguity up to order

Space time diagrams: Lindenr

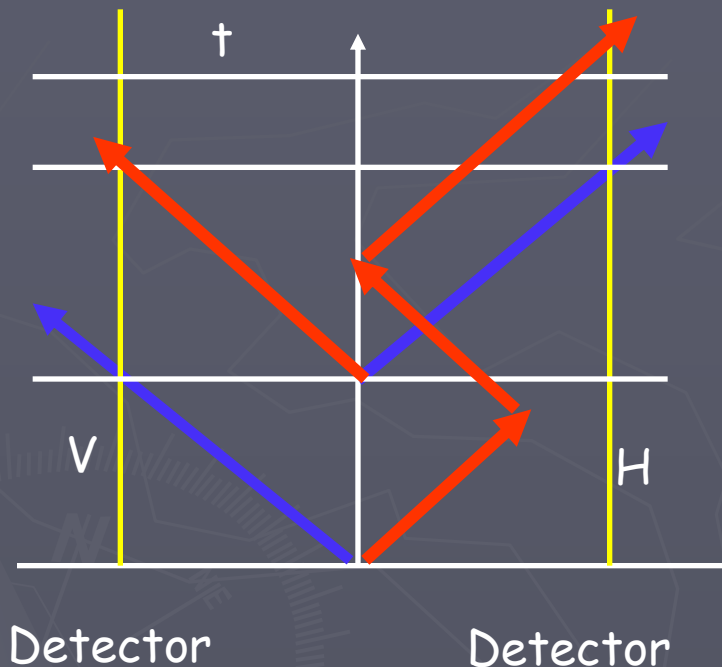


J. Finley

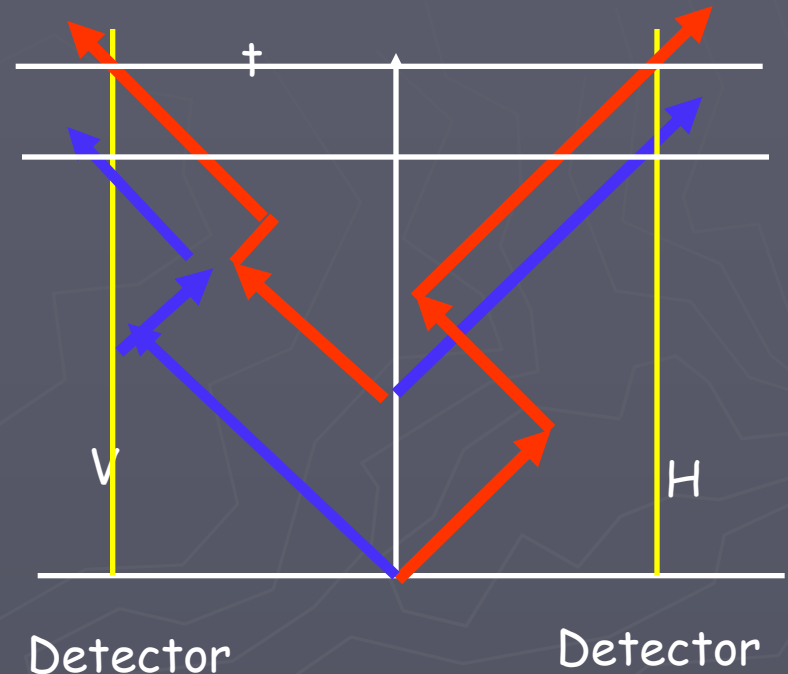
Order Monitors the path

Reordering

Reimer et. al.



Fixing the order

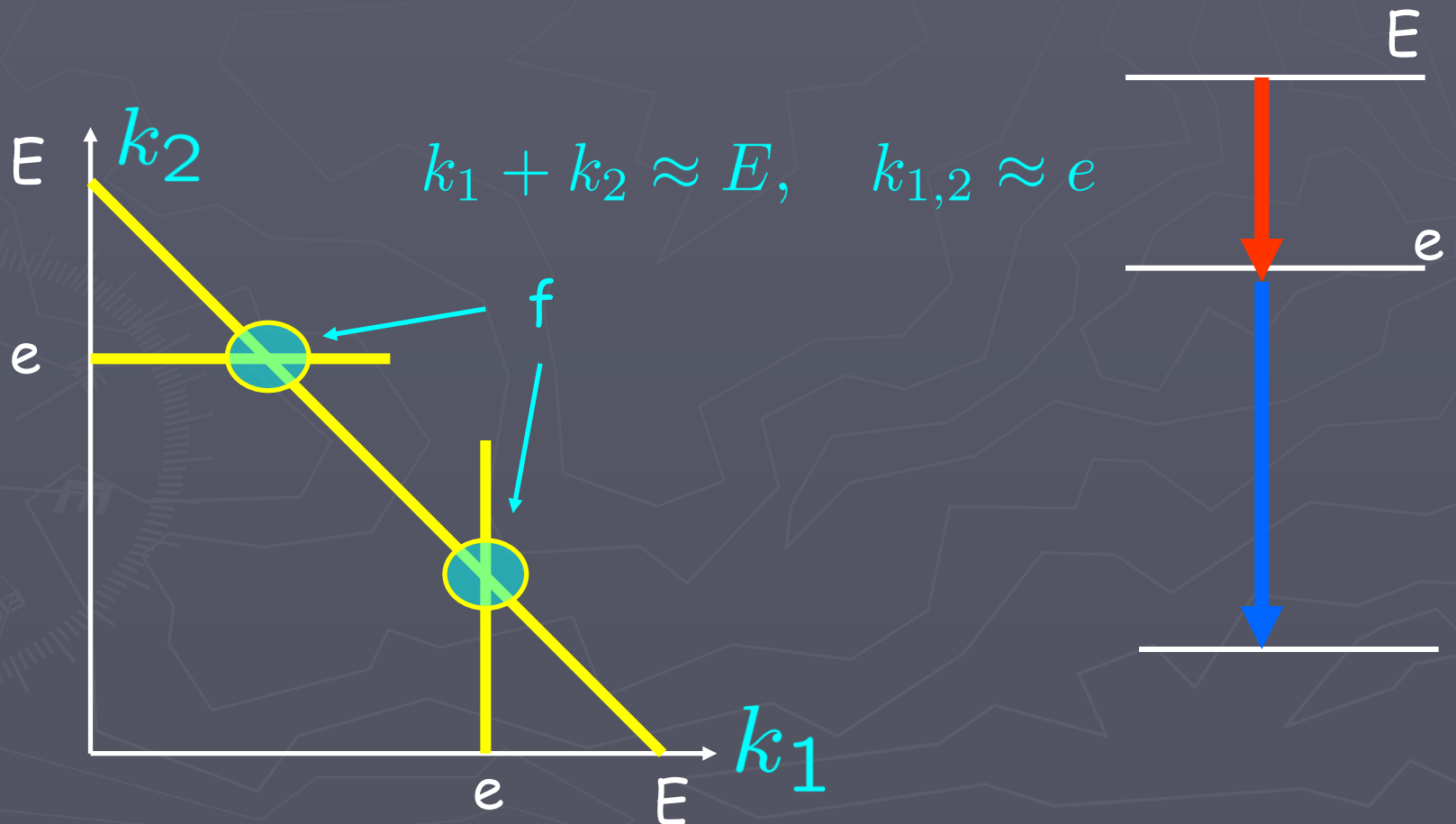


Forcing ambiguity

How much entanglement?
Can reordering be done on demand, i.e. unitary?

Photon field from cascade

$$|E, e\rangle = \sum f(k_1, k_2; E, e) a^\dagger(k_1) a^\dagger(k_2) |0\rangle$$



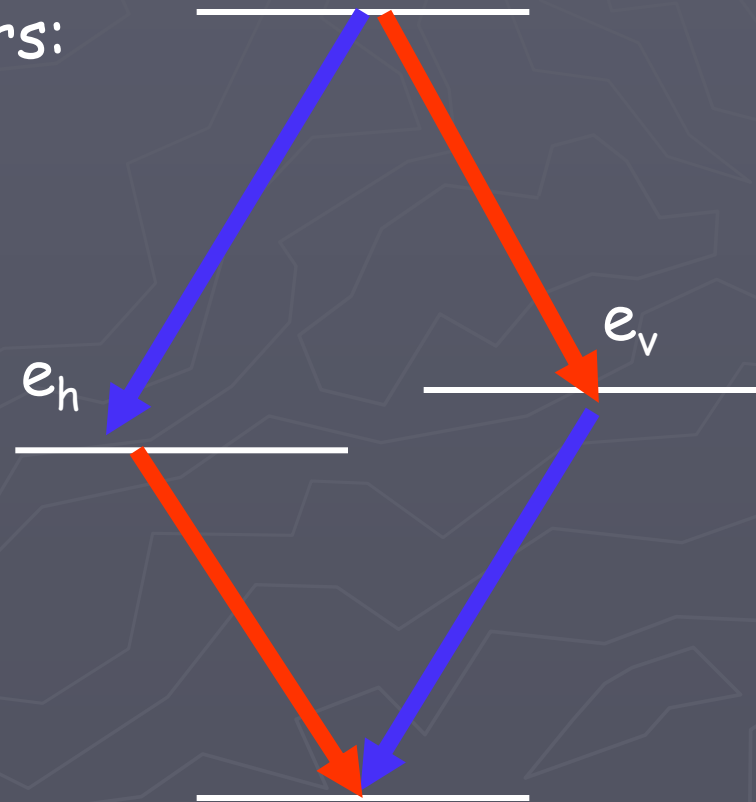
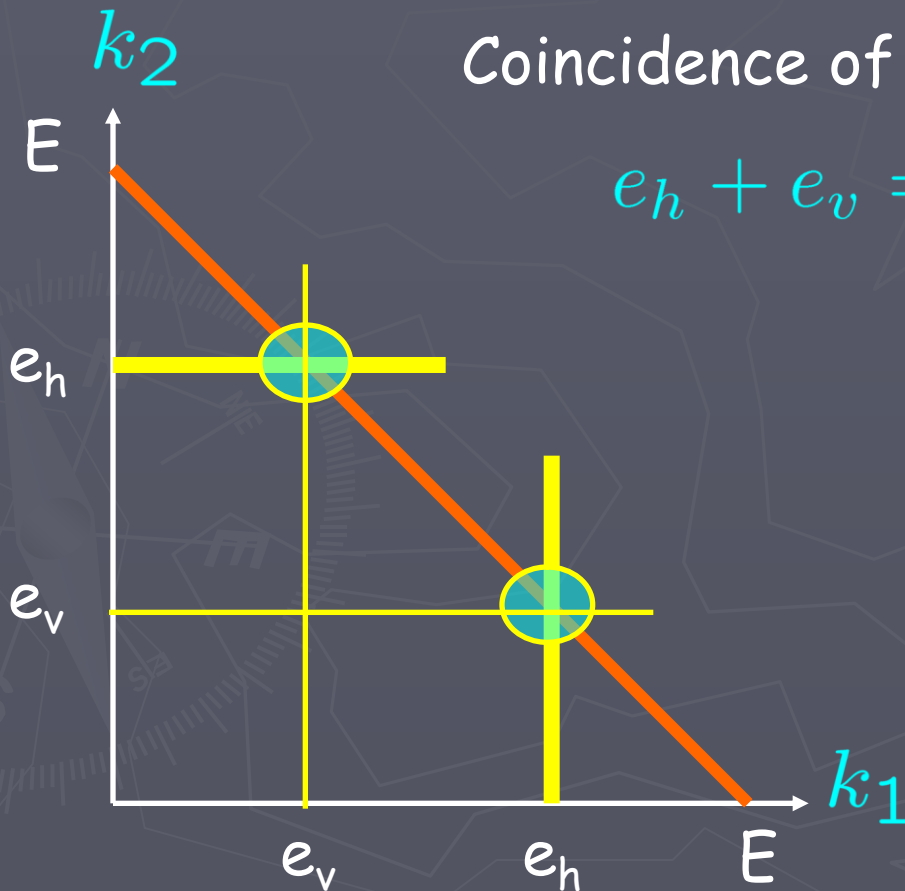
Photon field for 2 paths

$$|E, e_h\rangle \rightarrow h(k_1, k_2), \quad |E, e_v\rangle \rightarrow v(k_1, k_2)$$

E

Coincidence of colors:

$$e_h + e_v = E$$



How much entanglement?

Entanglement small $\langle h|v\rangle \approx 0$

By phase cancellation not by lack of overlap

$W = e^{i(\gamma_h - \gamma_v)}, \quad \gamma_{h,v}(k_1, k_2)$ manifestly unitary

$$h = |h|e^{i\gamma_h}, \quad v = |v|e^{i\gamma_v}$$

$$\langle E, e_h | W | E, e_v \rangle = \langle |h| | |v| \rangle \quad \text{Not small}$$

How much overlap ?

Little overlap



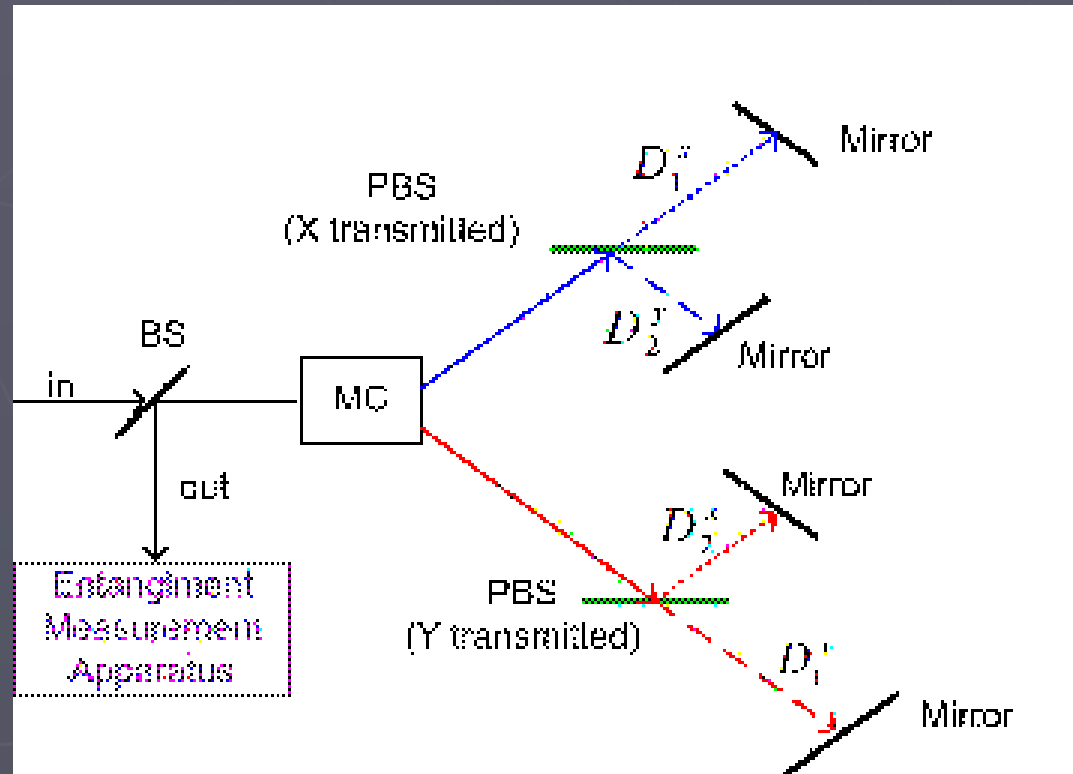
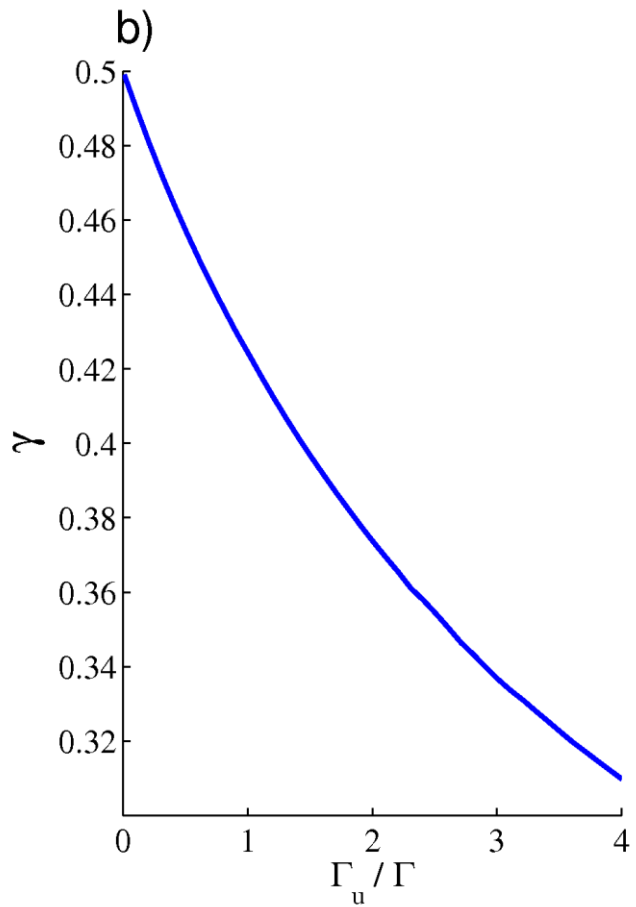
$$\Gamma_E > \Gamma_e$$

Large overlap



$$\Gamma_E < \Gamma_e$$

Setup



Concluding remarks

- ▶ Test: Make the experiment
- ▶ Dephasing
- ▶ Fight Wigner von Neuman

Special thanks to Jonathan Finely