

Proximity, magnetoresistance & gating effects
in **bilayers** (BL) of
doped topological Bi_2Se_3 & superconducting NbN

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- **Part I** compares bilayers to bare NbN films
[Supercond. Sci. Technol. **28** 025003 \(2015\)](#) & <http://arxiv.org/pdf/1409.2975v1.pdf> (2014)
- **Part II** Magnetoresistance & gating effects on these bilayers & films
<http://arxiv.org/pdf/1506.08584v1.pdf> (2015)

Outline

- Some background
- Ultra-thin bilayers of Bi_2Se_3 -NbN for studying topological superconductivity

Part I

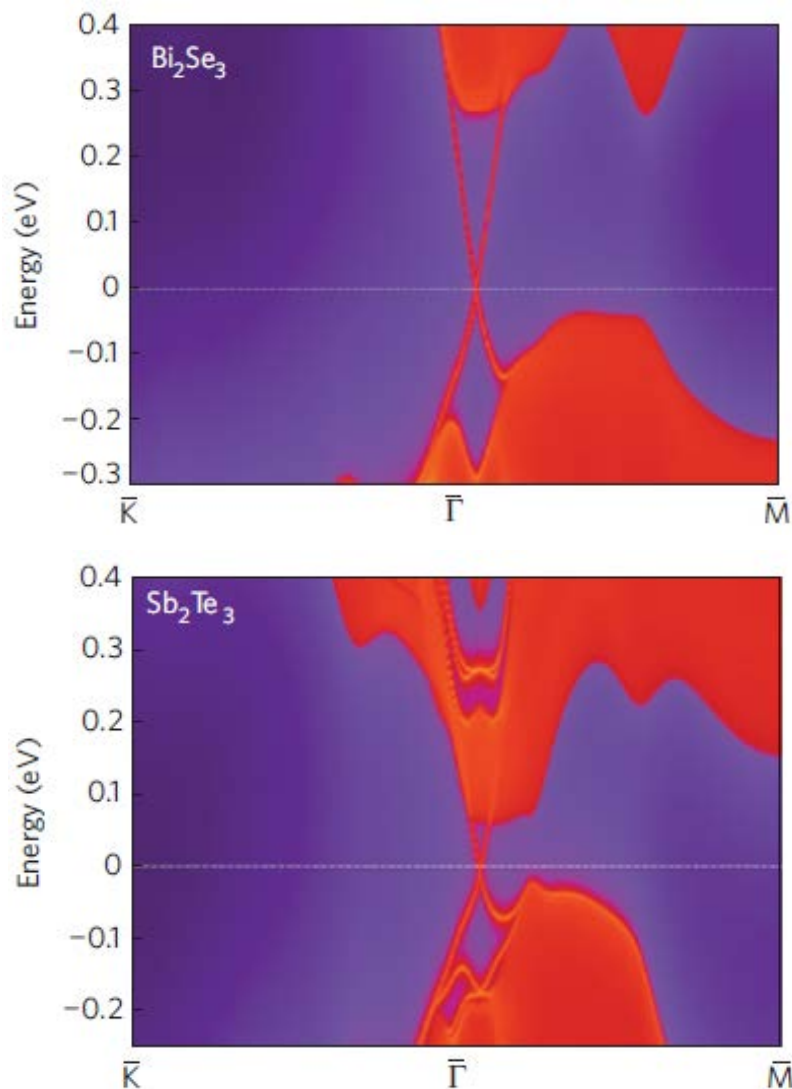
- Proximity effects in these bilayers

Part II

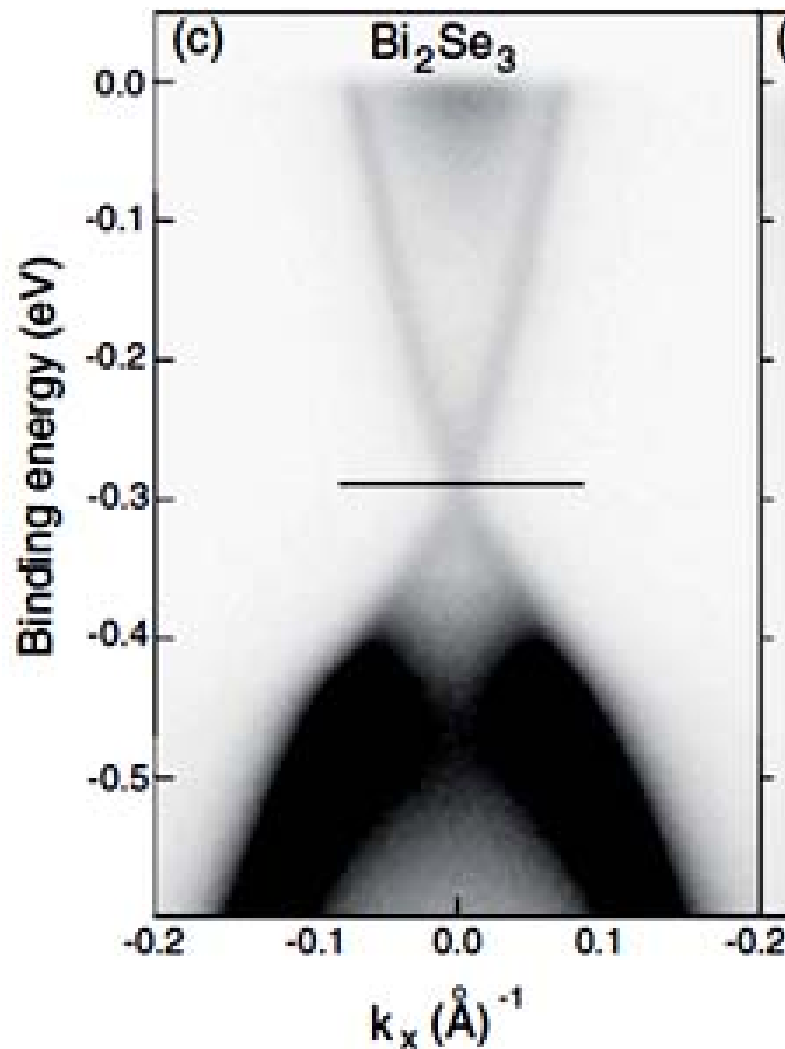
- Magnetoresistance & gating effects in Bi_2Se_3 films
- Magnetoresistance & gating effects in the bilayers
- Interpretation of the results in terms of vortex physics & pinning
- Alternative interpretations

Topological insulators are bulk insulators with surface conductance & a single Dirac cone of the surface states

Zhang... & S. C. Zhang, calc. bands
[NATURE PHYSICS, 5, 438 \(2009\)](#)



T. Kirzhner &... A. Kanigel, meas.
ARPES, [PRB 86, 064517 \(2012\)](#)



Motivation for studying topological superconductors (TSC)

- It is predicted that Majorana fermions (MFs) exist in the vortex cores of topological superconductors (TSC)
- These MFs will appear as zero energy modes (or ZBCP) in conductance spectra of TSC/N junctions (N is a normal metal)
- They should be **robust against disorder & decoherence**
- & thus might be useful in quantum computing (*)

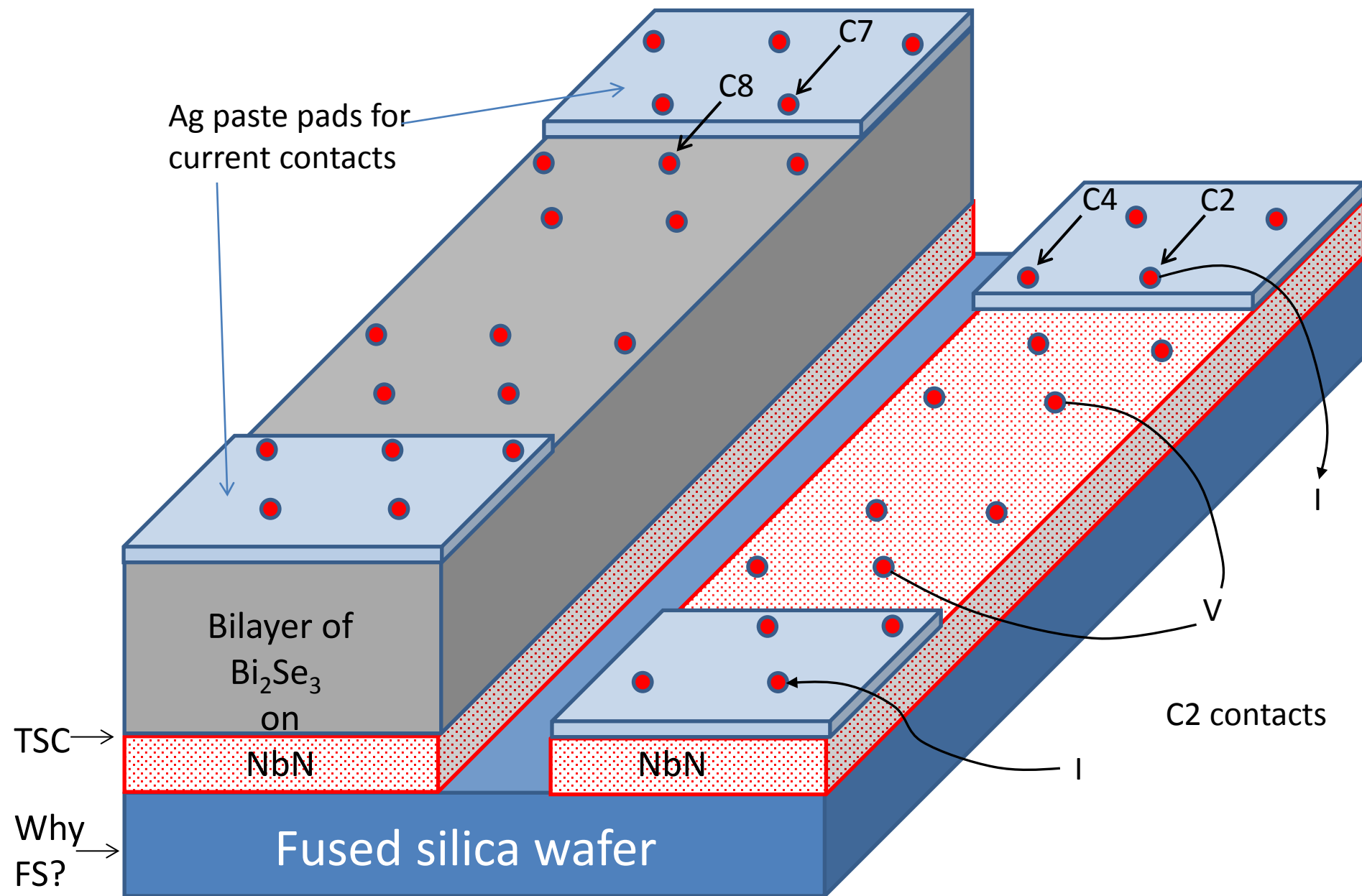
(*) Fermionic Quantum Computation

Sergey B. Bravyi and Alexei Yu. **Kitaev**, Annals of Physics **298**, 210–226 (2002)

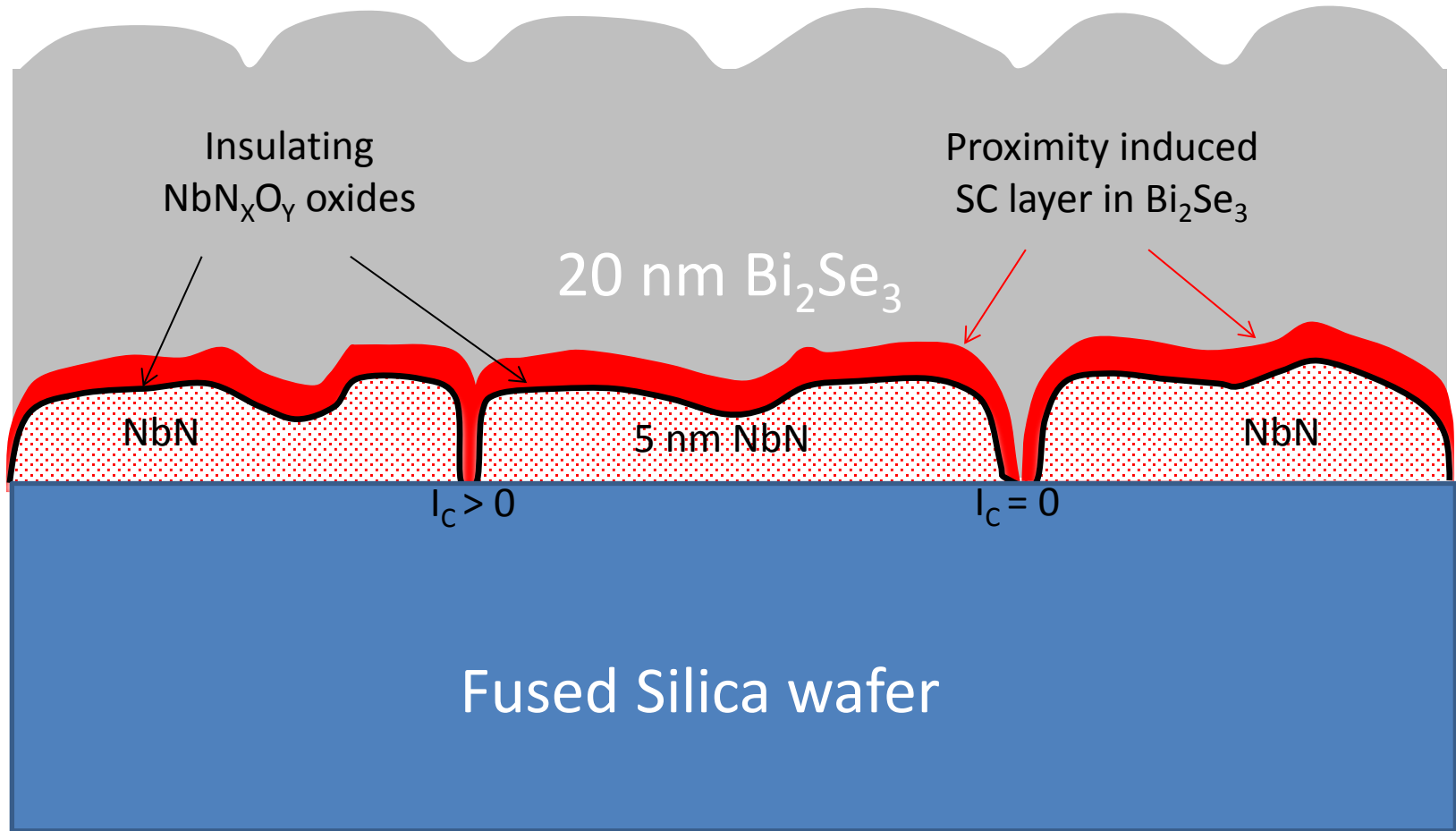
Why studying transport in **ultra-thin** bilayers of Bi_2Se_3 -NbN?

- If the NbN film is too thick ($>10\text{nm}$) & $T < T_c$, it will short all the effects of the Bi_2Se_3 cap-layer \rightarrow no TSC at the interface could be investigated.
- Thus a thin NbN islands layer (~ 3 to 5nm) is needed, that behaves as a network of weak-links when bridged by the Bi_2Se_3 cap-layer
- \rightarrow current will have to flow via the interface with the Bi_2Se_3 layer, allowing for the TSC to be studied
- Percolation paths of weak-links will constitutes 1D TSC, and their geometry relative to the voltage contacts will determine the TSC transport properties in the bilayers
- **In the following slides, this will be explained in details**
- Some relevant parameters for 3-5nm thick NbN films:
 $T_c \sim 5\text{-}8\text{ K}$, $\xi \sim 5\text{ nm}$, $\lambda \sim 500\text{ nm}$, $\Delta \sim 1.5\text{ meV}$
[A. Kamlapure et al. Appl. Phys. Lett. **96**, 072509 \(2010\)](#)

A scheme of the film, bilayer & contacts geometry on the wafer

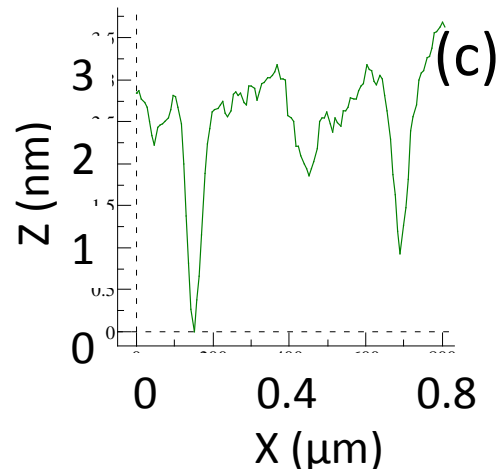
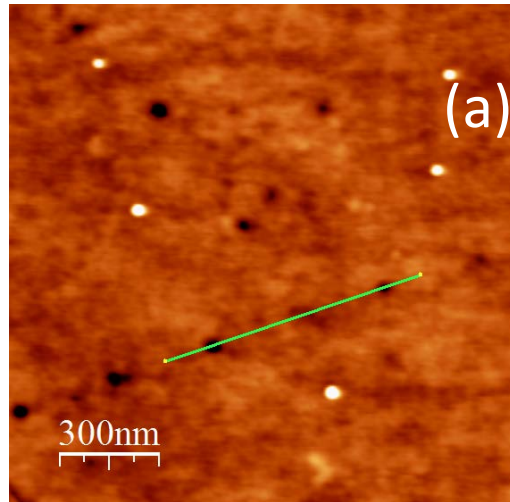


A model for the transport in the bilayer



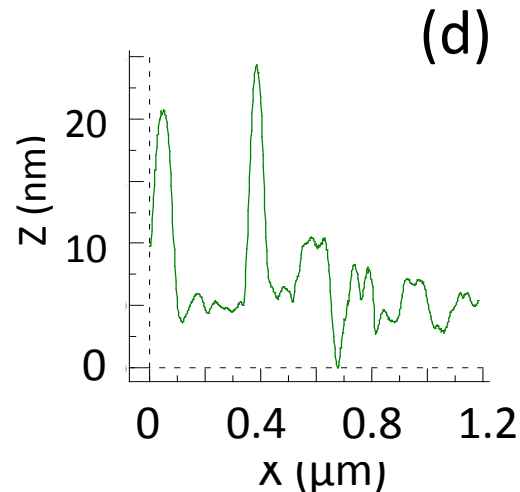
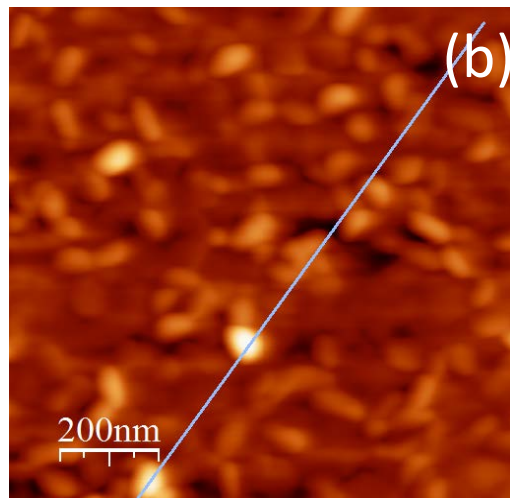
- Weak-links between the NbN grains (I_c with serial resistance)
- Proximity induced superconductivity in Bi_2Se_3 cap layer (at interface)

Topography of: (a) a 5nm thick NbN film, and of a bilayer (b) of 20nm Bi₂Se₃ on 5nm NbN on FS & typical line profiles



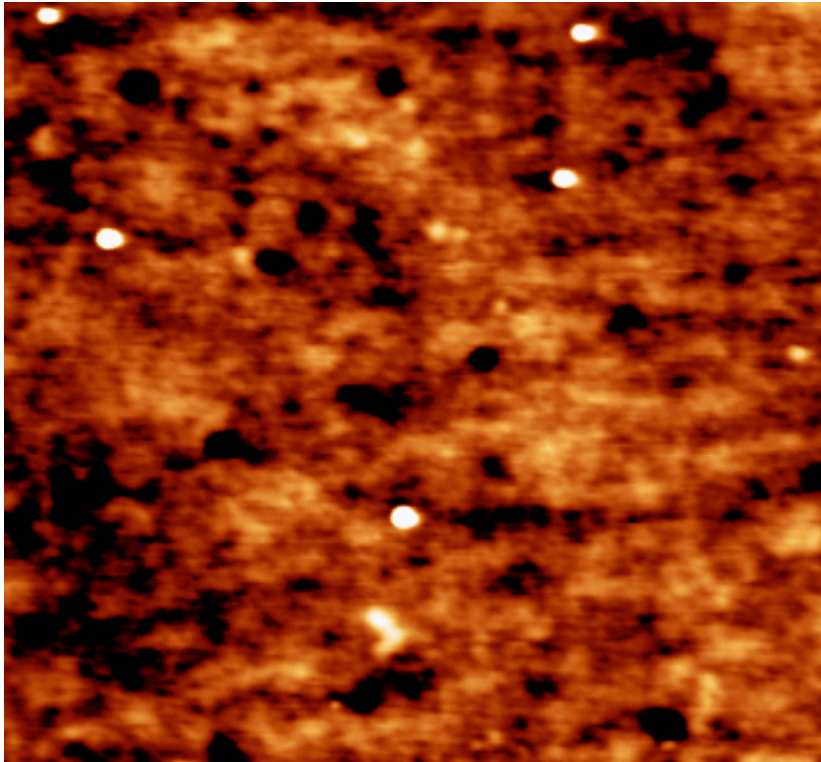
Holes:
~2-3 nm deep
r ~ 30 nm

Outgrowth:
~5-7 nm high
& similar r



On SrTiO₃ the NbN films are so smooth, that there are no weak-links.

RT & contrast-topo of a 5nm thick NbN film on FS

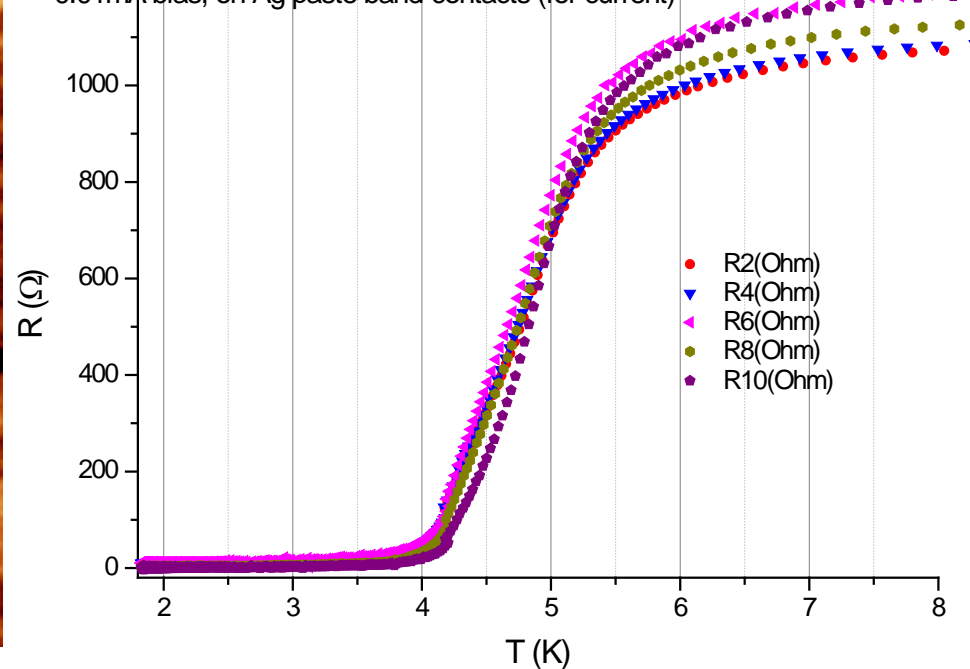


1.6 x 1.5 μm^2

LAF-334, Aug 11, 2014, 70min in air

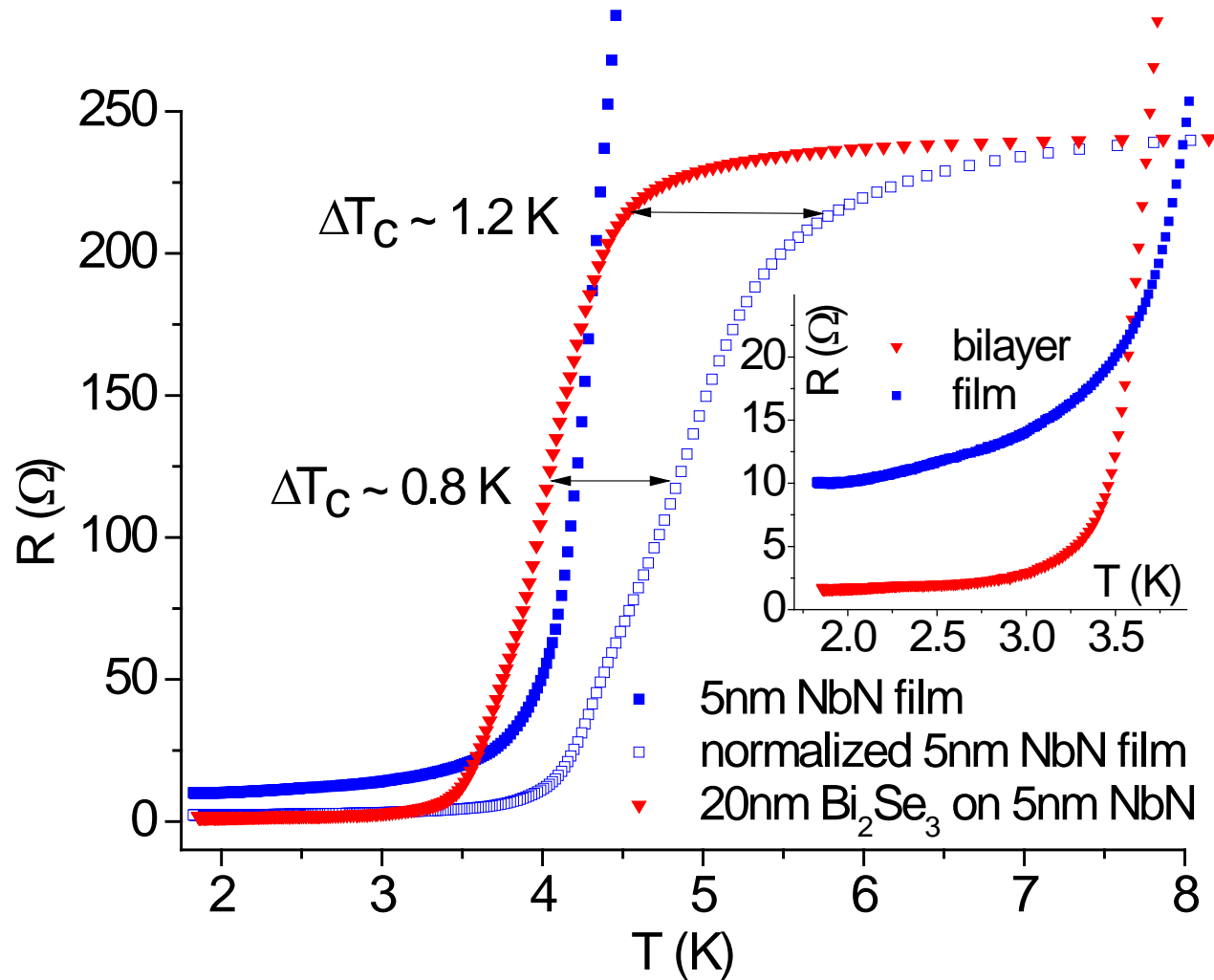
5nm NbN film on whole wafer on fused silica (FS)

0.1mA bias, on Ag paste band-contacts (for current)



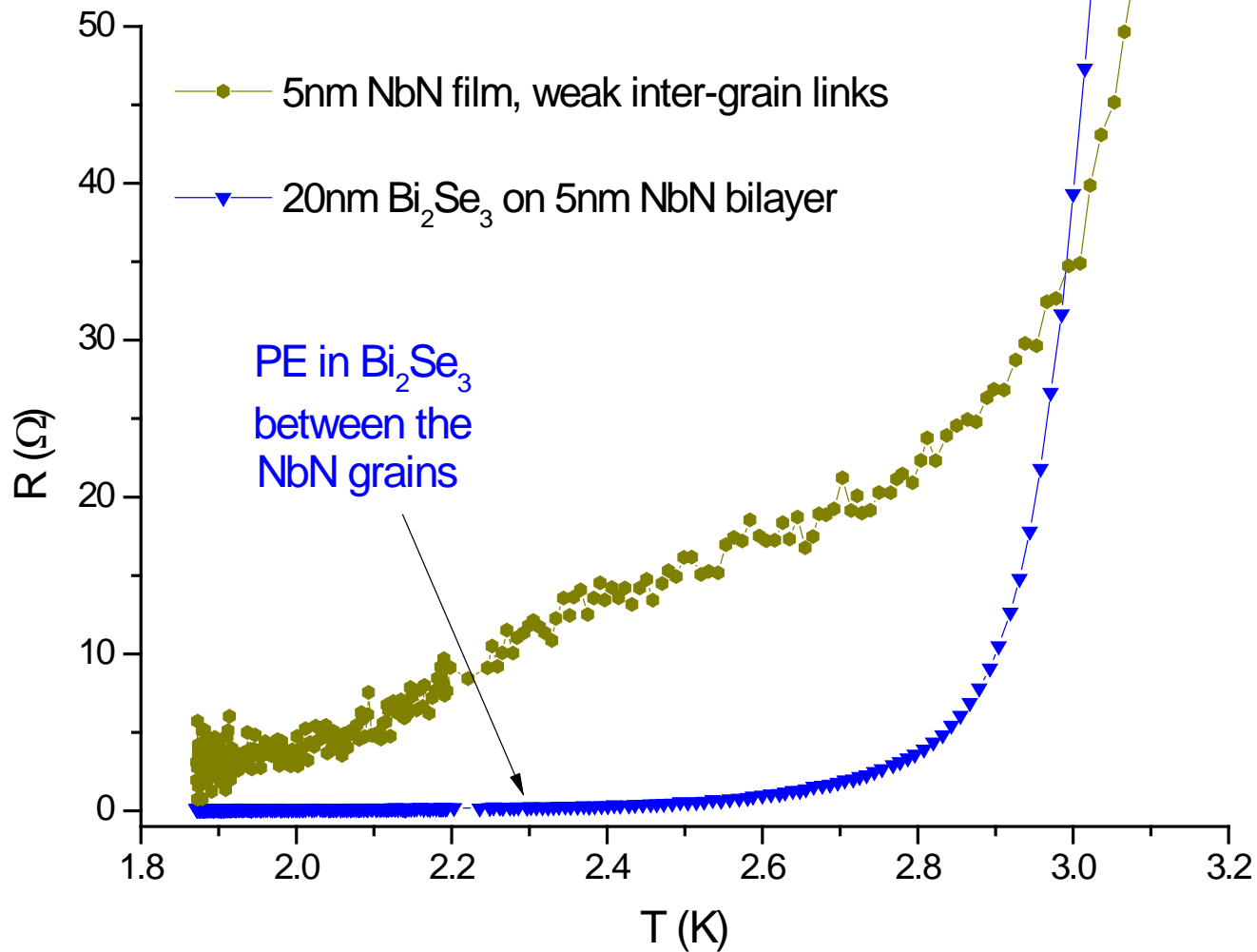
- NbN islands (bright areas) connected by weak-links (dark areas)
- rms – roughness: $\sim 0.5\text{nm}$ (0.1nm on STO – not shown)

R vs T of a 5nm thick NbN film after 10min in air, compared to an *in-situ* deposited bilayer of 20nm Bi₂Se₃ on 5nm NbN (LAF-BL-334)



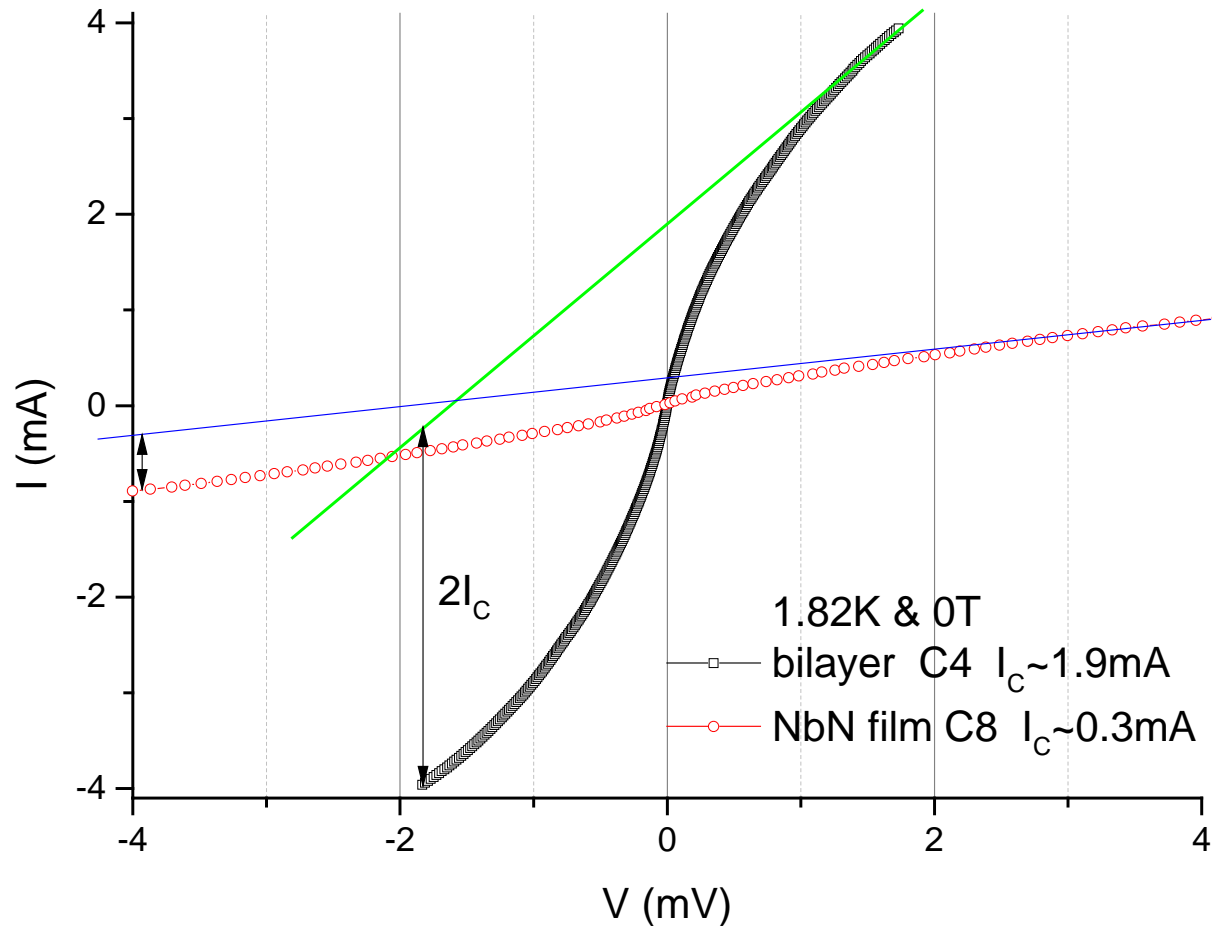
- Proximity effect (PE) in BL suppresses superconductivity in NbN grains (lower T_C)

Similar wafer (LAF-BL-333): Below 3K & without normalization of R



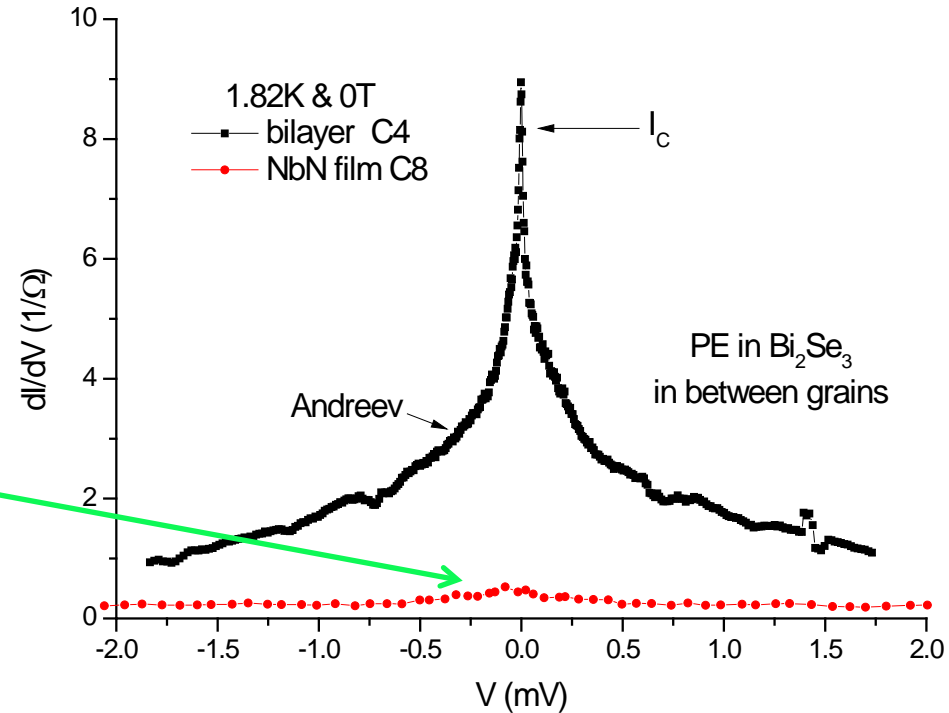
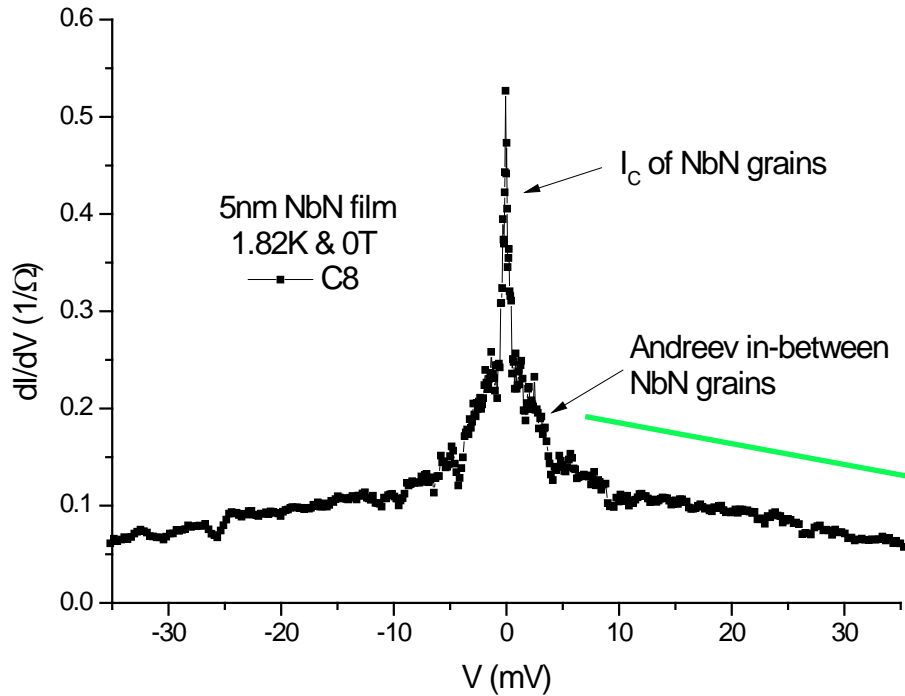
- Induced SC in Bi_2Se_3 at the interface with NbN with **no serial resistance**
- $T_c(\text{bilayer at } R=0) \sim 2.3\text{K}$, No $T_c(\text{film})$ down to 1.9K \rightarrow inverse PE in BL...

Same wafer (LAF-BL-333): IVC at 1.82K



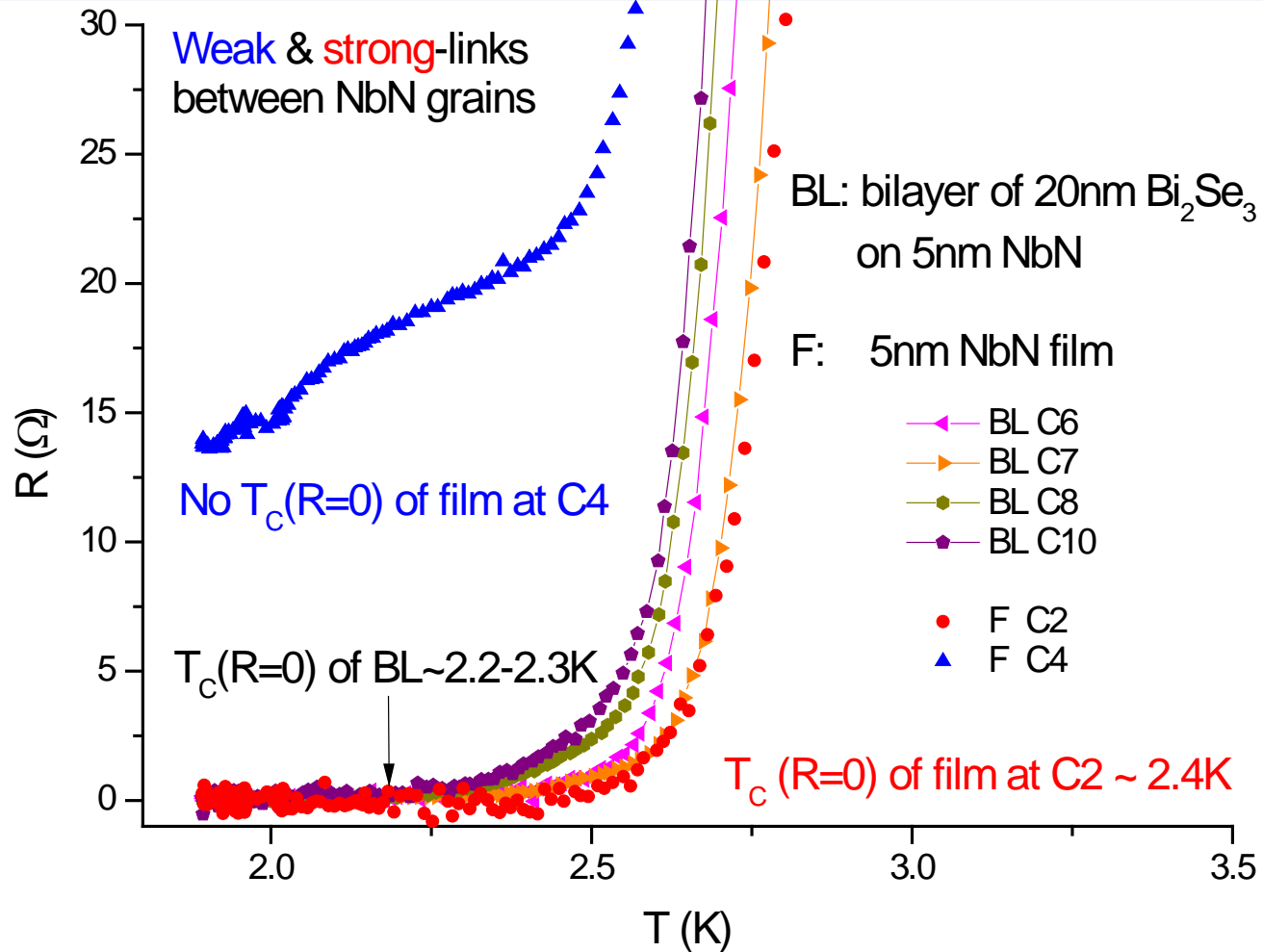
- Both have I_C at 1.82K, but $I_C(\text{bilayer})$ is about 6.3 times larger than $I_C(\text{film})$
- I_C enhancement in BL at low T indicates (inverse) PE in the TI

Conductance spectra of in-situ prepared bilayer and film (LAF-BL-333)



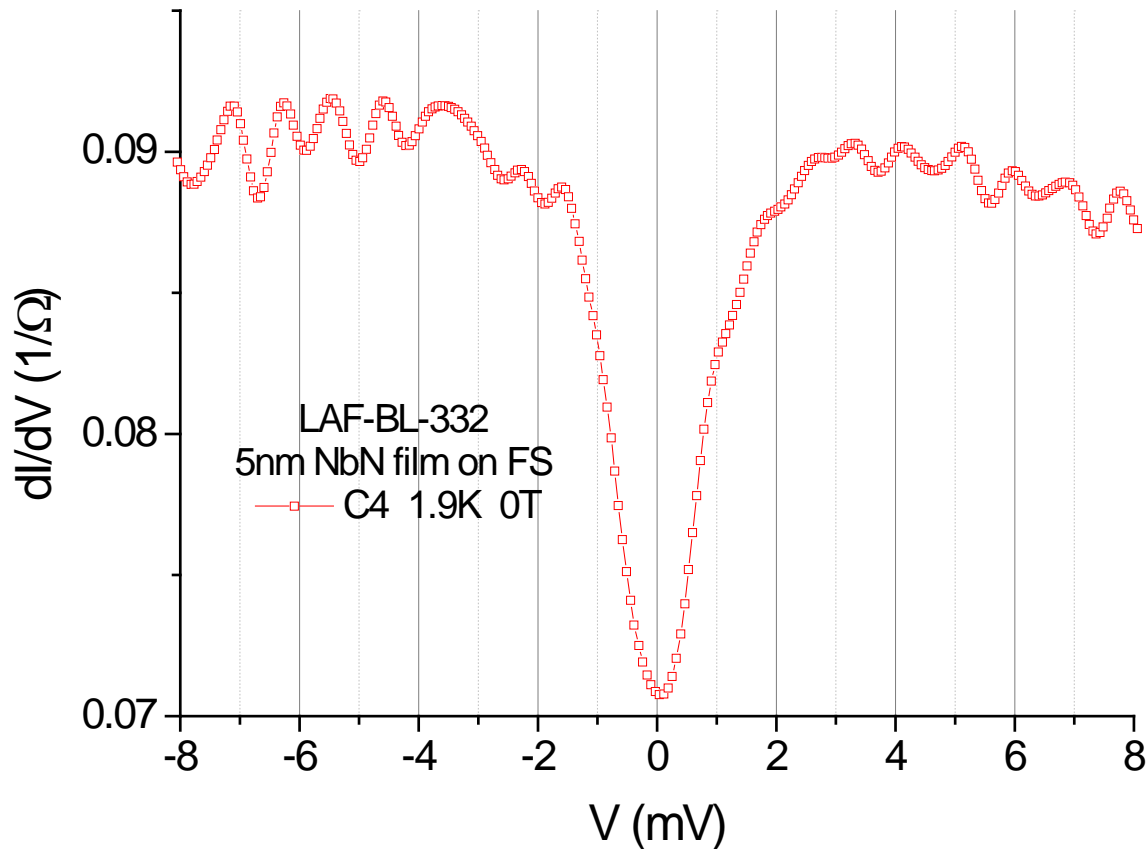
- I_C and Andreev peaks
- Andreev enhancement in BL at low T indicates (inverse) PE in the TI
- ZBC ($1/R$) of BL is about 20 times higher than that of the NbN film
[$R(\text{normal of NbN film}) \sim 6 \times R(\text{normal bilayer})$]

Scattering of the data (LAF-BL-332) after 17min exposure to ambient air: two extreme cases for the 5nm NbN film



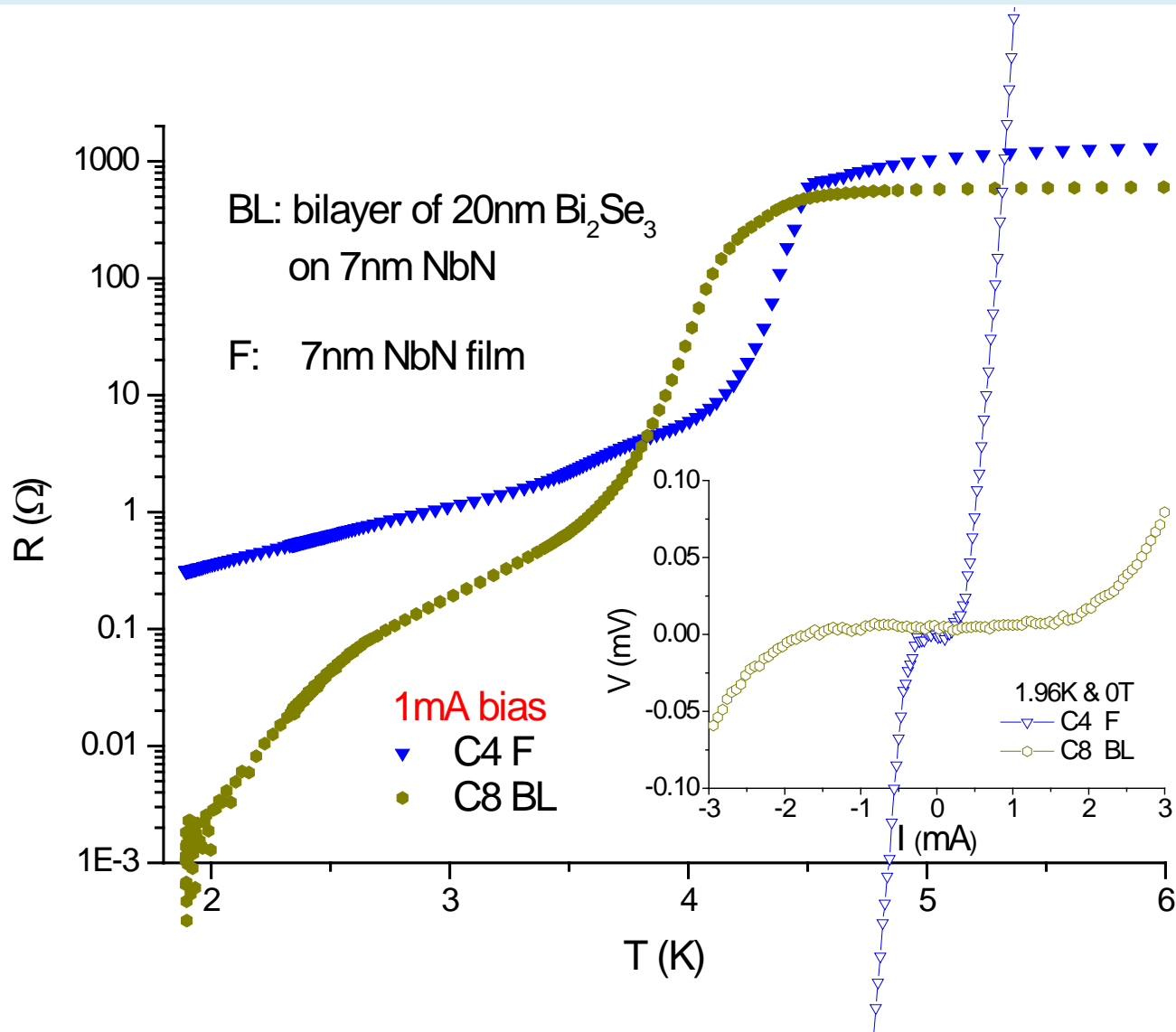
- Percolation of **strong-links** between the SC grains that connects the V-contacts of **C2**
- Percolation of **weak-links** between the SC grains that cuts the V-contacts of **C4**
- PE in Bi_2Se_3 in the BL, T_c of 2.2-2.3K, low scattering of the data (thick cap layer)

Tunneling conductance of the C4 contact of LAF-BL-332



- Gap-like feature at $2\Delta \sim 2$ mV $\rightarrow \Delta$ of the NbN grains ~ 1 mV (assuming 1 SNS junction)
- The weak-link here could originate in stronger defects like nm scratches etc.

7nm NbN film and bilayer with 20nm Bi₂Se₃: R vs T & IVC

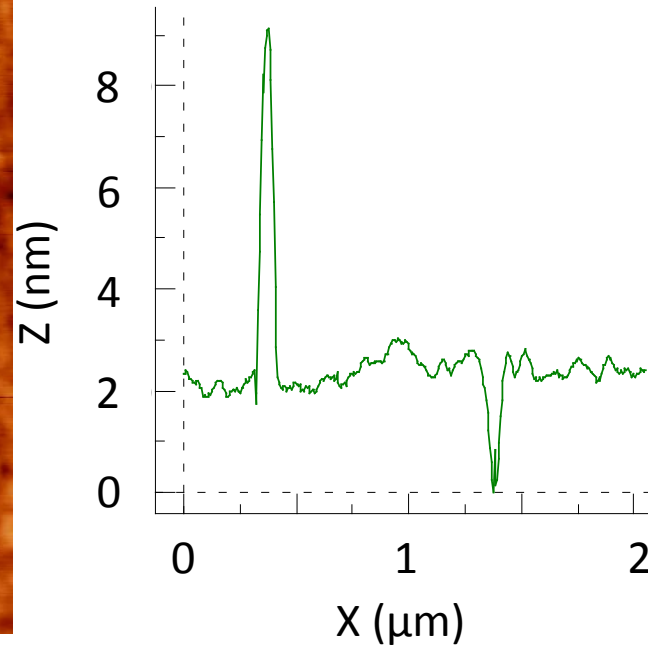
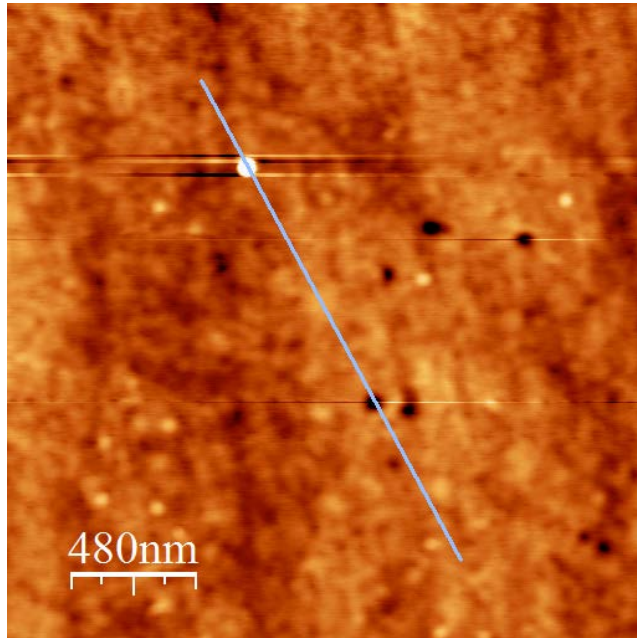


- Stronger links in thicker film which is less resistive at low T
- Need a higher bias to see PE in Bi₂Se₃ below 3.5K, see IVC at low T.

Conclusions I

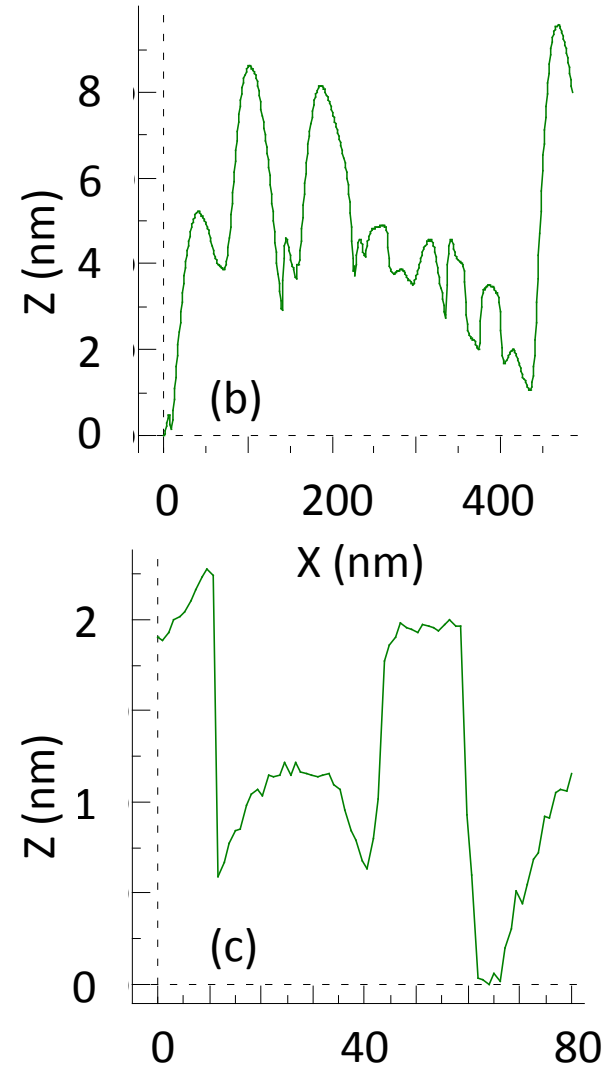
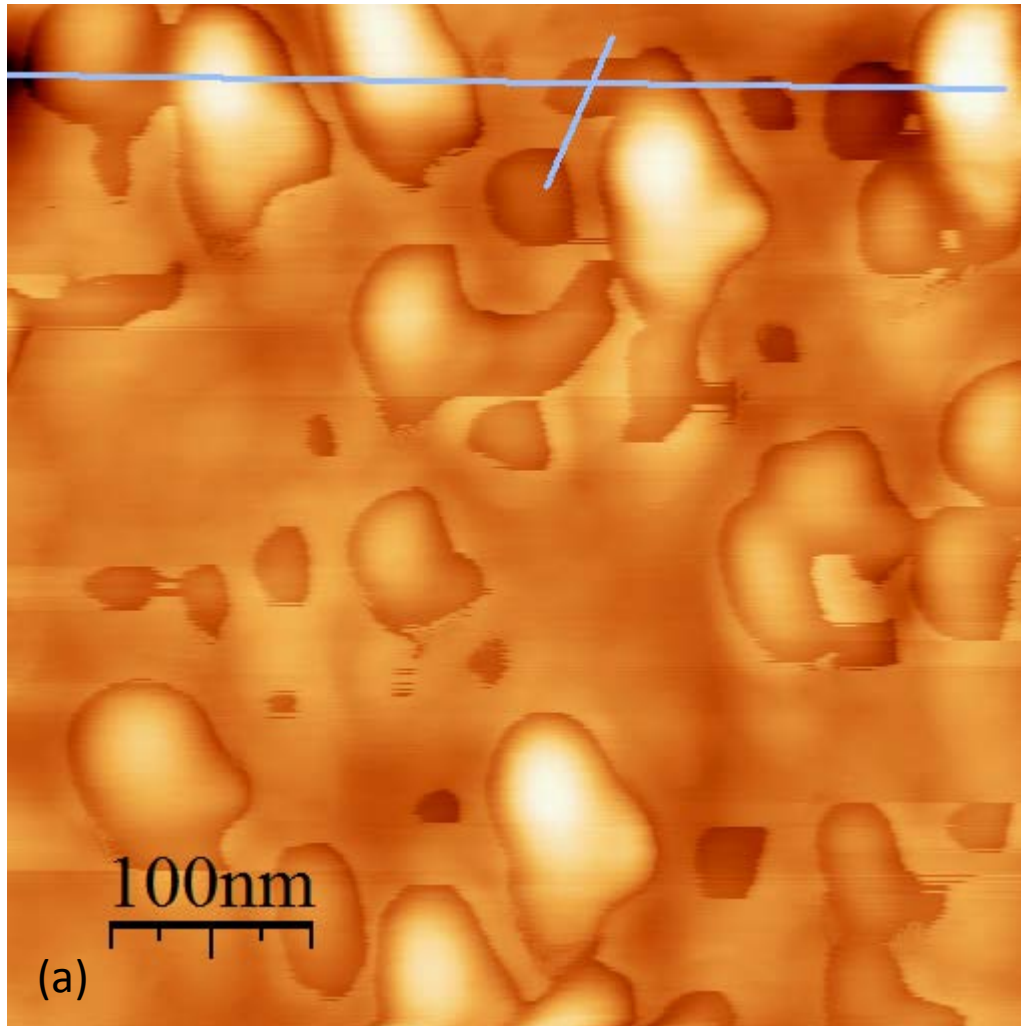
- Transport properties of *in-situ* prepared **bilayers** of a TI (Bi_2Se_3) & a SC (NbN) were compared to the bare SC **film**
- **Standard proximity effect** (PE) was observed in all bilayers in the main part of the SC transition (high T), where the TI layer (N) **suppressed** T_c of the SC layer
- At low T, an **inverse PE** in the TI of the bilayers was observed, as indicated by **enhancement** of I_c & Andreev conductance in the bilayer compared to the SC film
- Next we shall present **part II** which deals with **gating** effects on the magnetoresistance of even thinner bilayers and films.

AFM image of a 3nm thick NbN layer on FS



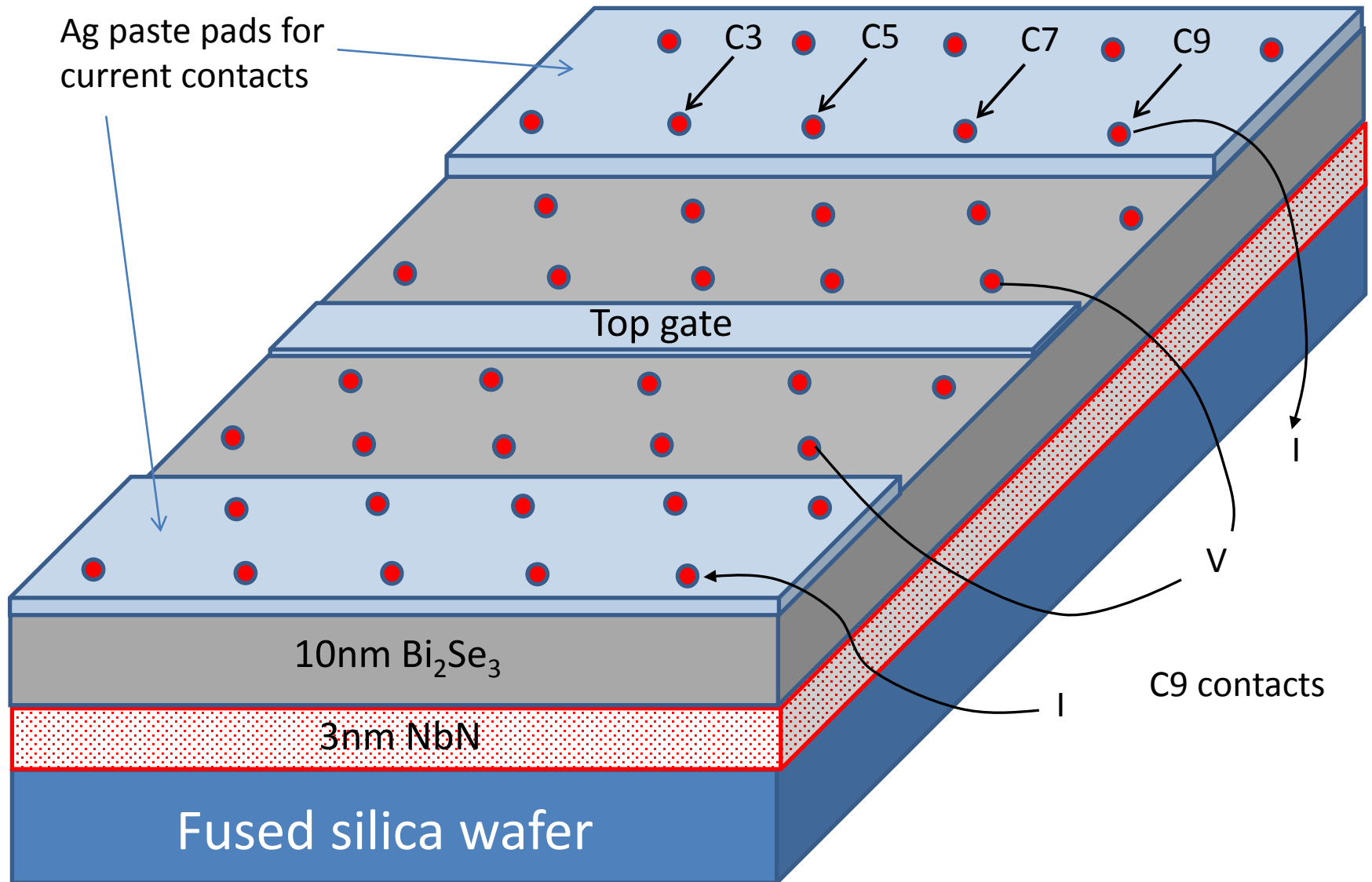
- Nano holes of ~ 70 nm diameter
- ~ 0.35 nm rms roughness

AFM image of a 10nm Bi_2Se_3 on 3nm NbN bilayer on FS & the corresponding line profiles in (b) & (c)

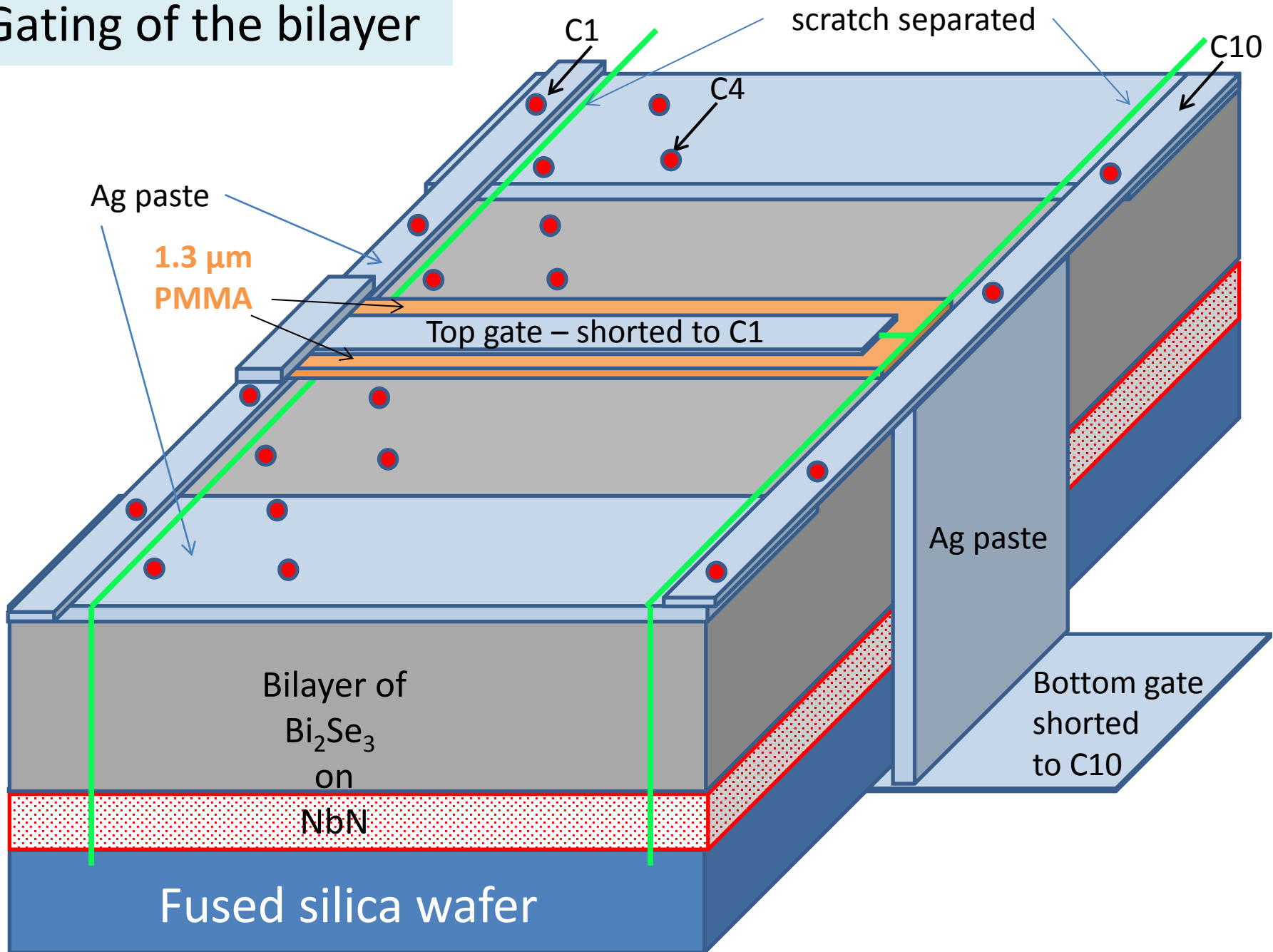


~1.1 nm rms roughness & Quintuple steps of 1 and 2 nm can be seen in (c)

A schematic drawing of the bilayer & contacts geometry now



Gating of the bilayer

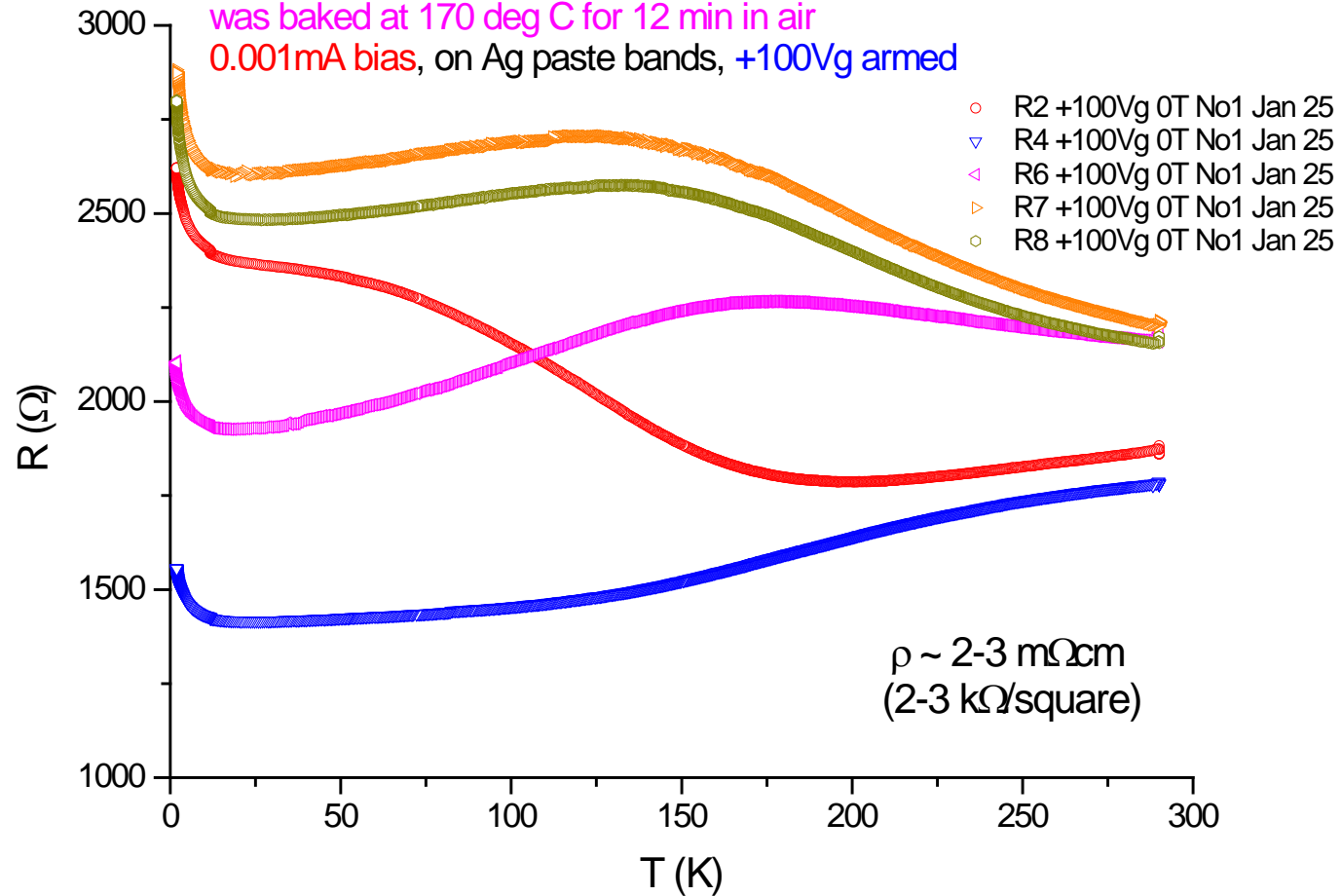


10 nm Bi_2Se_3 reference film on fused silica

(1) R vs T results

L438c, Jan 25 2015, **AGED!!**

10nm Bi_2Se_3 film on FS, while putting the top gate:
was baked at 170 deg C for 12 min in air
0.001mA bias, on Ag paste bands, +100Vg armed



For similar resistivity,
The electron densities
according to
[Butch *et al.* PRB](#)
[81, 241301R \(2010\)](#)
are:

- $4\text{-}6 \times 10^{17}$ elect./cc
From Hall measurements
- $3\text{-}4 \times 10^{17}$ elect./cc
From SdH oscillations

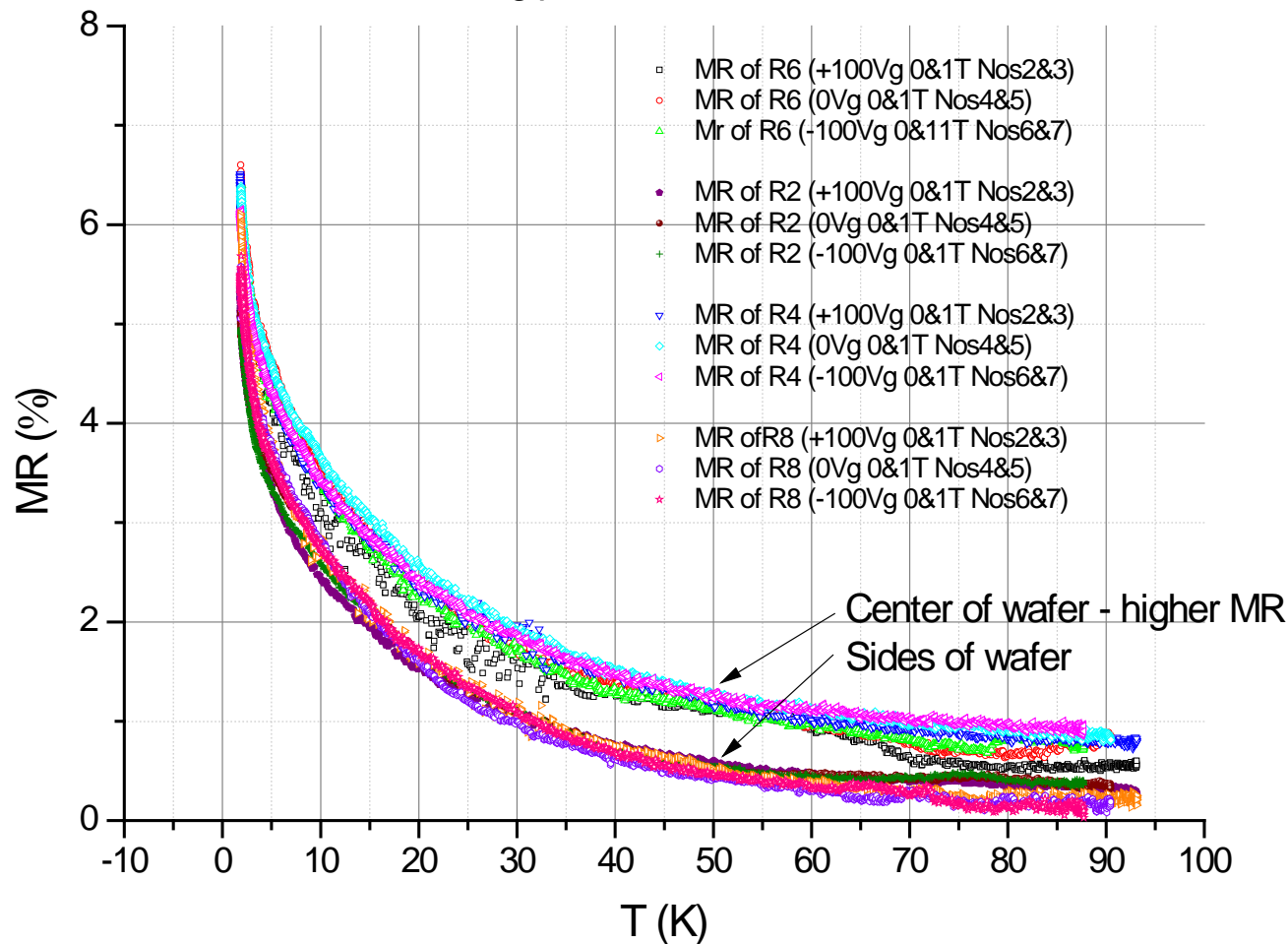
10 nm Bi₂Se₃ reference film on fused silica

(2) MR results

- Magnetoresistance $MR = [R(H)-R(0)] / [R(H)+R(0)]/2$ H is the magnetic field

L438c, Jan 25 2015, 10nm Bi₂Se₃ film on FS
0.001mA bias, on Ag paste bands

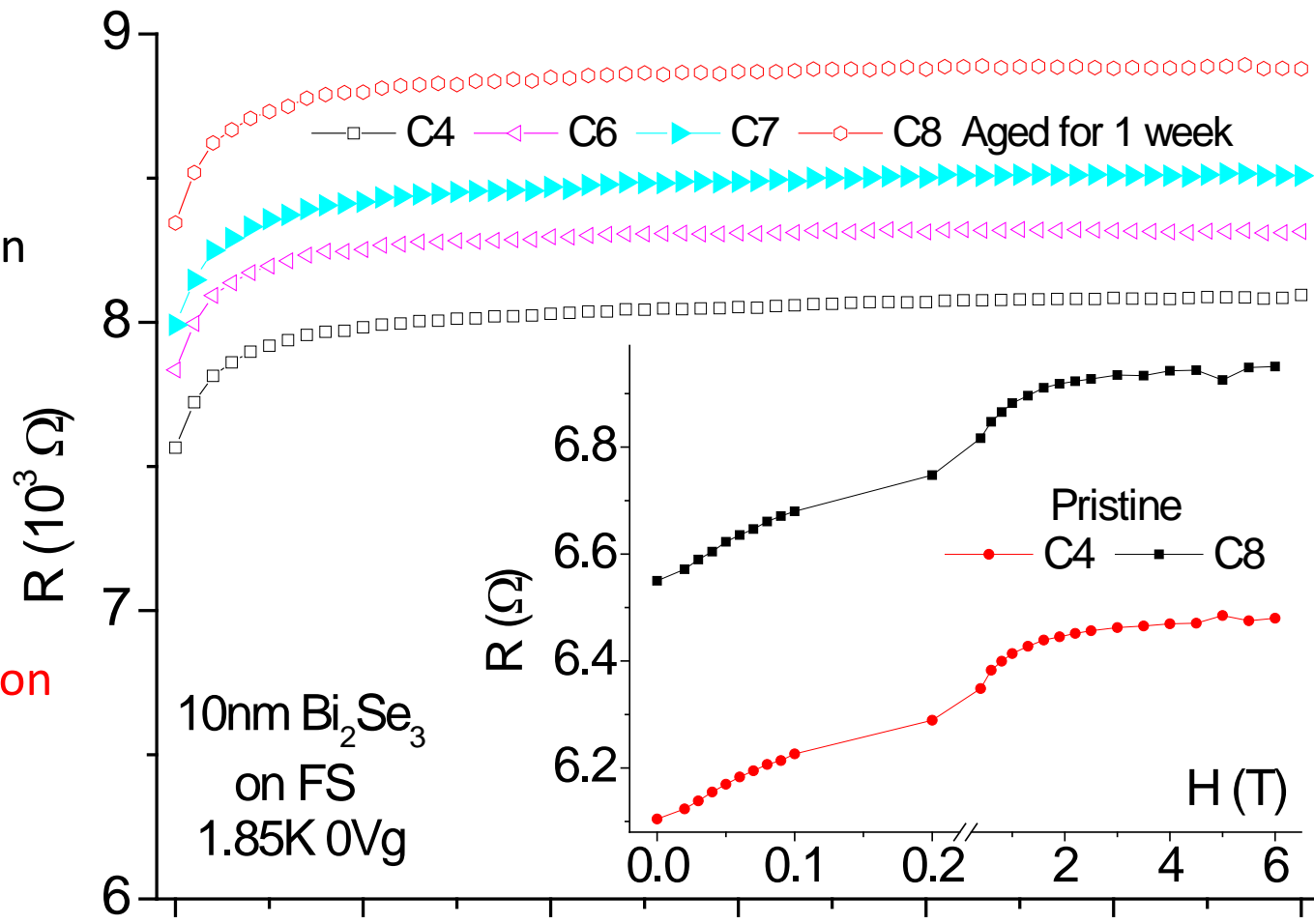
- H is 1T here
- Fit a double-exponential decay, but not $A/T^{0.5}$
- Almost insensitive to gate-voltage V_g , unlike Steinberg et al. PRB **84**, 233101 (2011)
- E_g -field of top gate for -100Vg & $\epsilon \sim 2.6$ is: $2.6 \times 100V / 0.00013cm = 2 \text{ MV/cm}$ (vs x 40 higher of Steinberg)



(3) R versus H of another 10nm Bi_2Se_3 film on FS

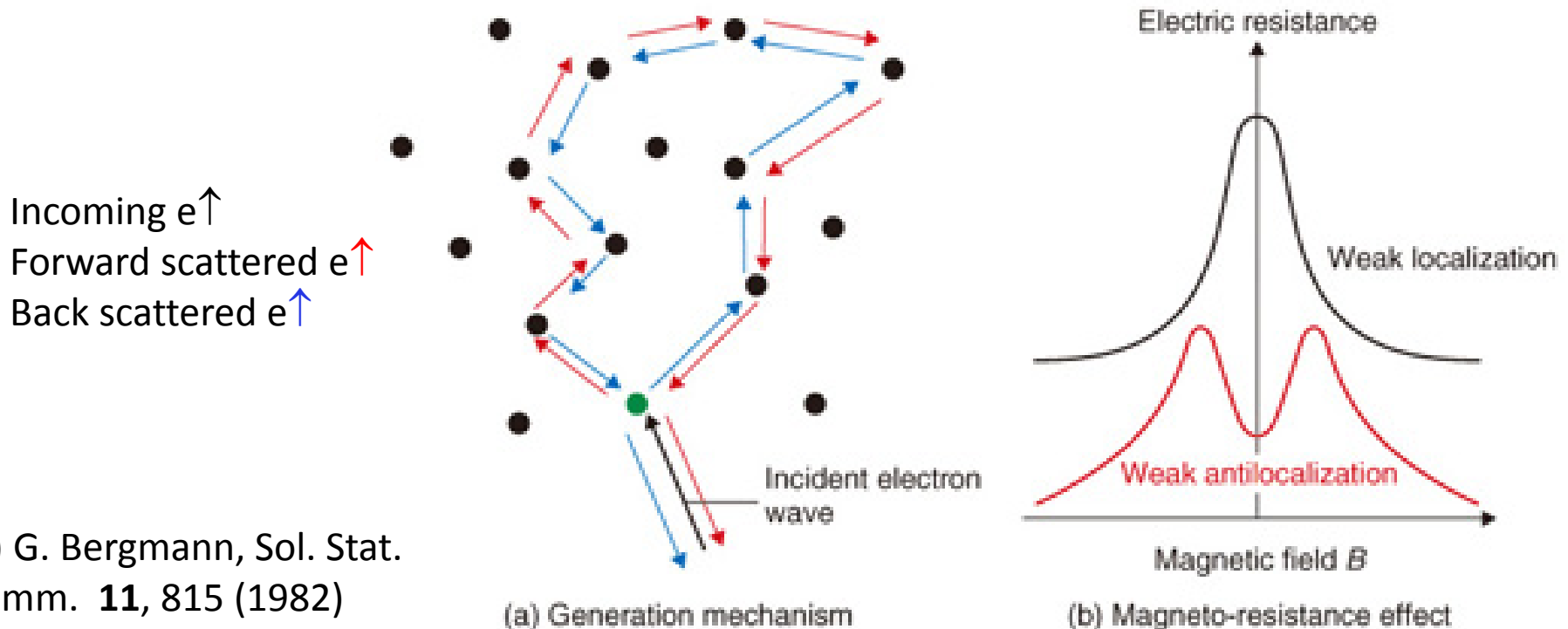
- Linear MR at low H results from edge currents with linear dispersion (Dirac-like)

- See Weak Anti-Localization (WAL) analysis next



Weak localization (WL) and Anti-localization (WAL)

- Disordered 2D electron systems can have coherent closed-loop electron trajectories due to elastic scattering (a), which lead to WL when interfere constructively, and WAL when interfere destructively.
- Since $MR \propto dR/dH$ & added flux destroys pure WL and WAL, $MR < 0$ for WL & $MR > 0$ for WAL, see (b)
- Under strong spin-orbit int., the spins rotate & $\psi(e\uparrow)$ returns to itself only after 2 loops - yielding added phase of $\Delta\phi = 4\pi$.
- For 1 loop $\Delta\phi = 2\pi$, the spins \uparrow & \downarrow rotate in opposite directions & one can show that they interfere destructively, thus WAL occurs (*).



(*) G. Bergmann, Sol. Stat. Comm. **11**, 815 (1982)

Weak anti-localization – WAL & quantum diffusion

The Hikami-Larkin-Nagaoka (HLN) model (*)

$$\Delta G_{\square}(B) \cong \alpha \frac{e^2}{\pi h} \left[\psi\left(\frac{1}{2} + \frac{B_{\phi}}{B}\right) - \ln\left(\frac{B_{\phi}}{B}\right) \right]$$

ψ is the Digamma function $d/dz[\ln \Gamma(z)]$ & for $z=n$, $\Gamma=(n-1)!$

$$B_{\phi} = \hbar / 4eL_{\phi}^2 \quad \& \quad \alpha \approx -1/2$$

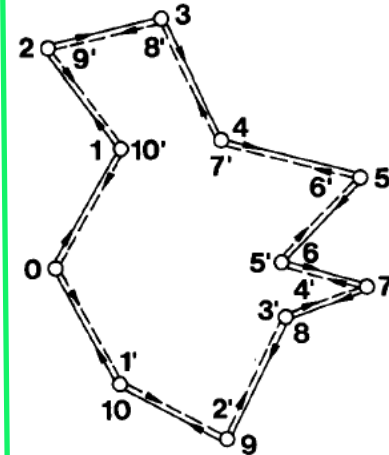
$$\Delta G_{\square}(B) = G_{\square}(B) - G_{\square}(B=0) \quad \& \quad G_{\square}(B) = L/W R_{\square,xx}$$

For $B=1T$ & phase coherence length L_{ϕ} in nm:

$$1.2 \times 10^5 \frac{R(B) - R(0)}{R(0)R(B)} \cong \psi\left(\frac{1}{2} + \frac{156}{L_{\phi}^2}\right) - \ln\left(\frac{156}{L_{\phi}^2}\right)$$

- $R(B)-R(0)$ is the un-normalized magnetoresistance (MR)
- Since R is temperature dependent, this formula yields $L_{\phi}(T)$

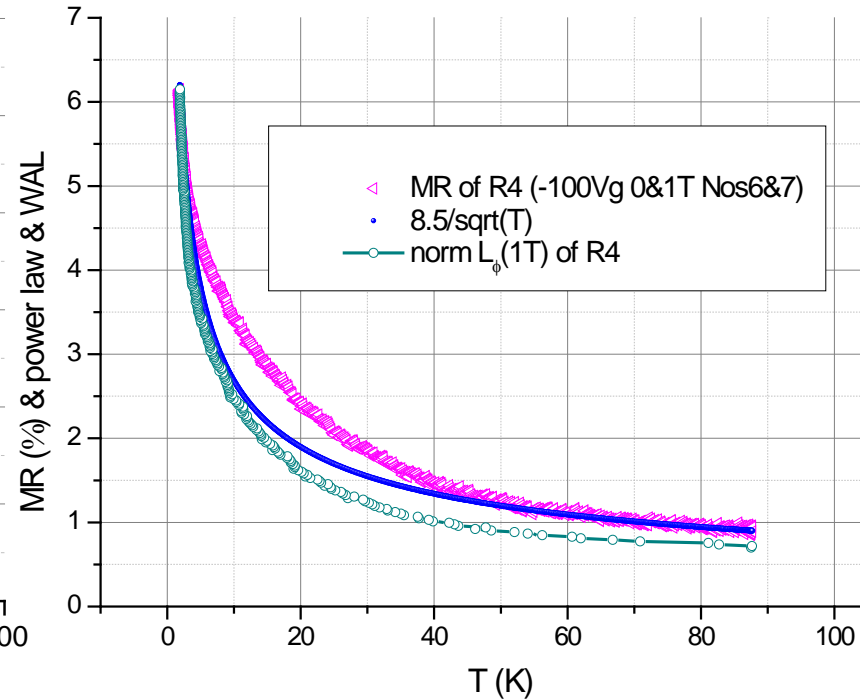
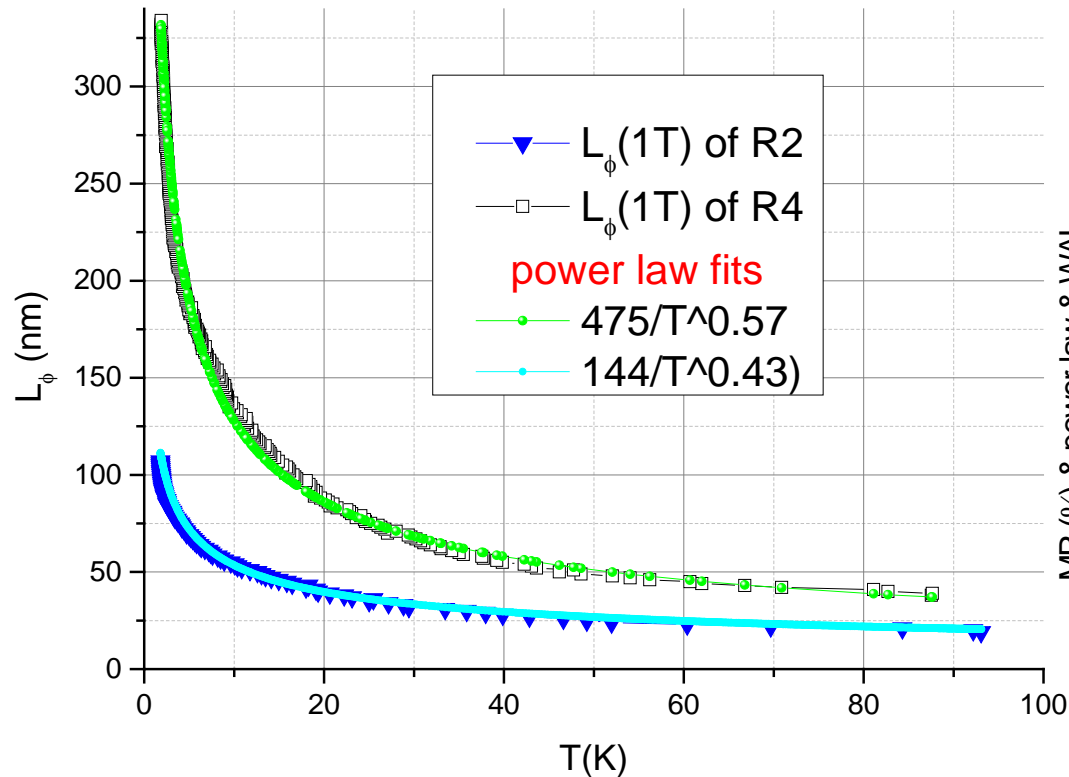
2D + disorder
+ spin-orbit =>
Interference
effects



(*) Prog. Theor. Phys. **63**, 707 (1980)

10 nm Bi_2Se_3 reference film on fused silica

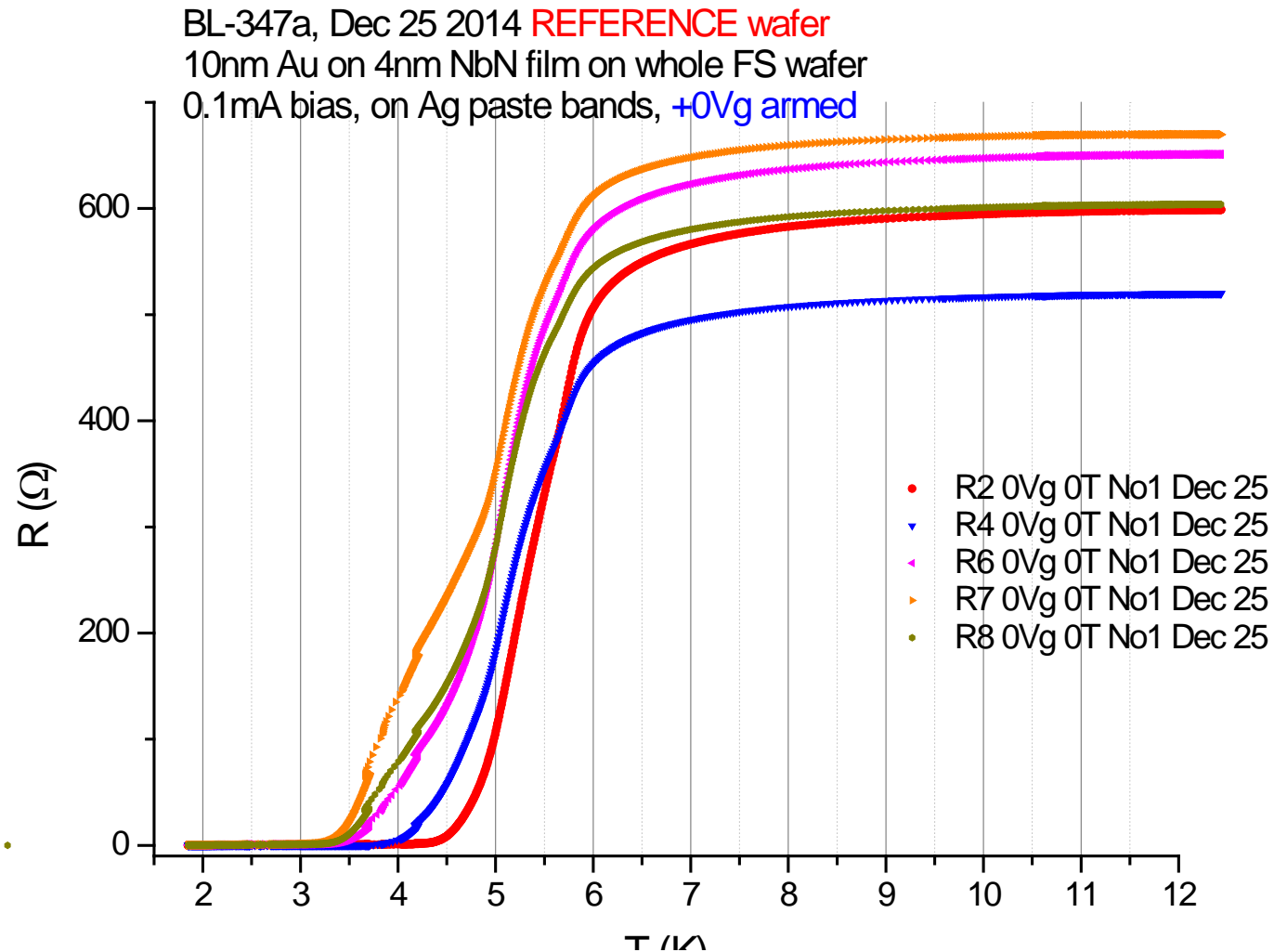
(4) MR, WAL & power law results vs T



- On the same wafer, different L_ϕ & power-law exponents for different contacts
- On same contact, different behavior of MR, power-law ($-1/2$ for 2D) & L_ϕ (WAL)
- $L_\phi = \sqrt{D\tau_i}$ where for $T > 2\text{K}$, τ_i is the electron-phonon scattering time (shortens vs T)

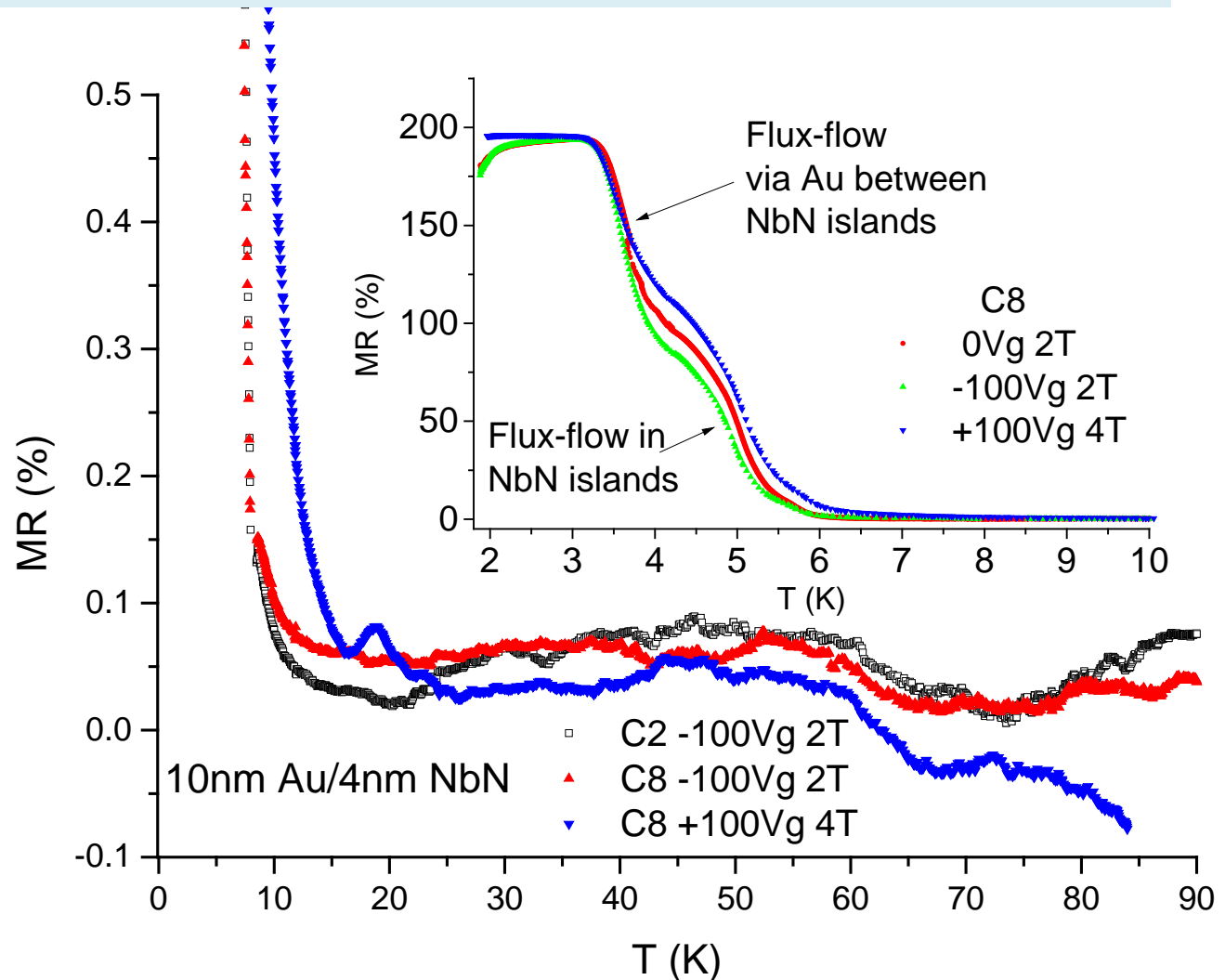
(1) A second reference bilayer of 10 nm gold (Au) on 4nm NbN on fused silica

R vs T results



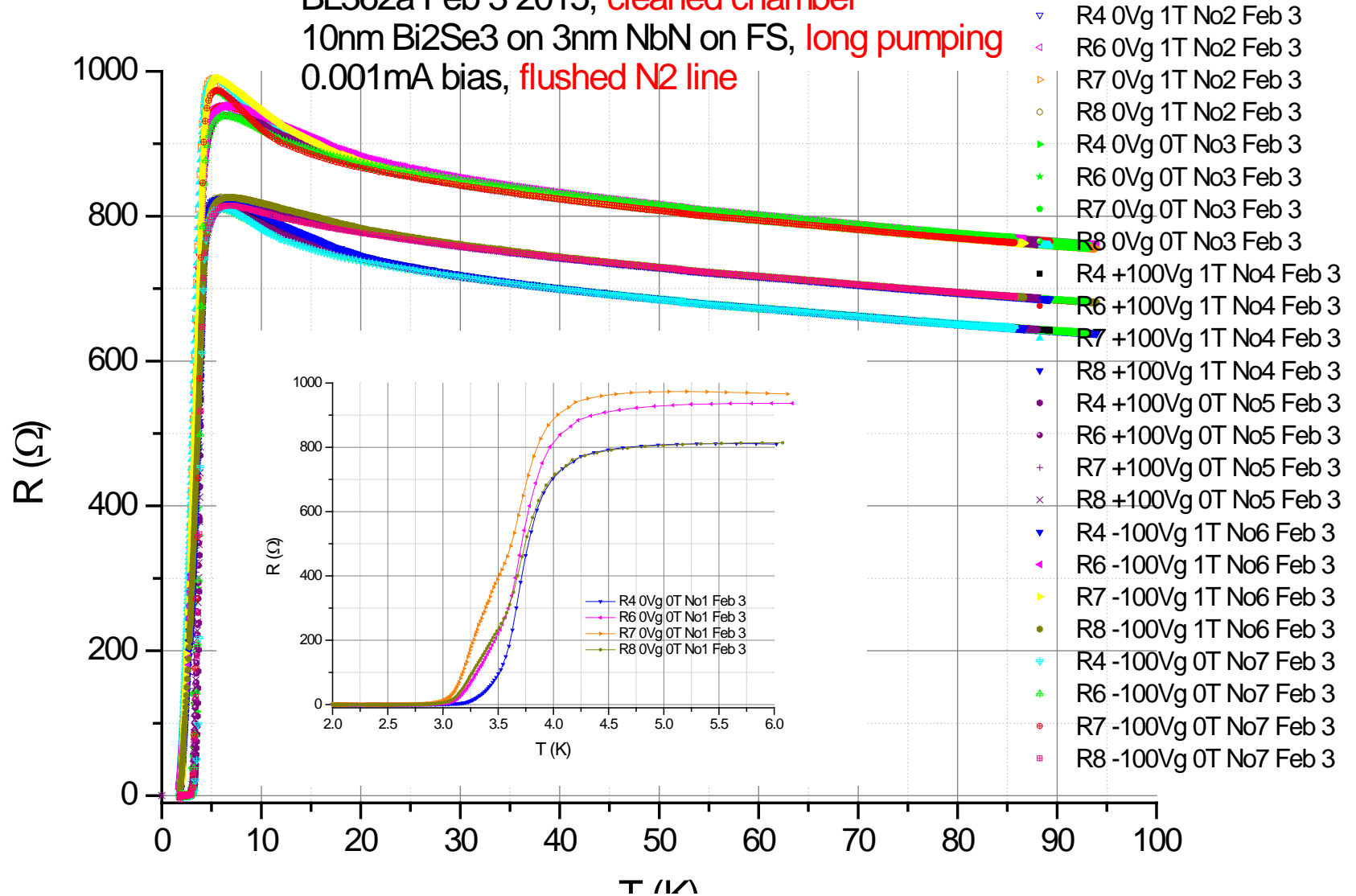
(2) MR results & Flux-flow (FF) in this bilayer **below T_c** (10 nm gold (Au) on 4nm NbN on fused silica)

- H is **2 & 4T** here
- MR($T < T_c$) due to flux-flow (FF) of NbN grains and in between the grains in the Bi_2Se_3 cap-layer
- For 2T, negligible MR of $\sim \pm 0.1\%$ above **$T_c \sim 7-8\text{ K}$**
- At 4T, the SC MR starts at **$\sim 12\text{ K}$** due to **$\text{FF}(4\text{T}) > \text{FF}(2\text{T})$**



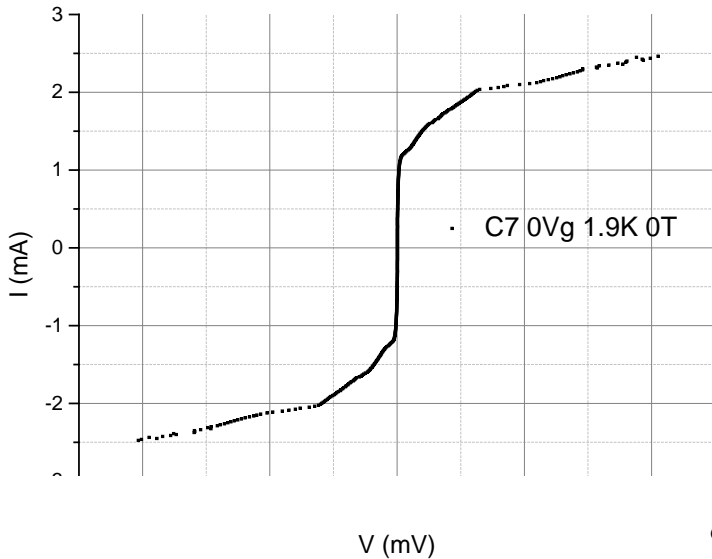
(1) R vs T of a bilayer of 10 nm Bi₂Se₃ on 3nm NbN on fused silica [low R_{max} case]

BL362a Feb 3 2015, **cleaned chamber**
 10nm Bi₂Se₃ on 3nm NbN on FS, **long pumping**
 0.001mA bias, **flushed N₂ line**

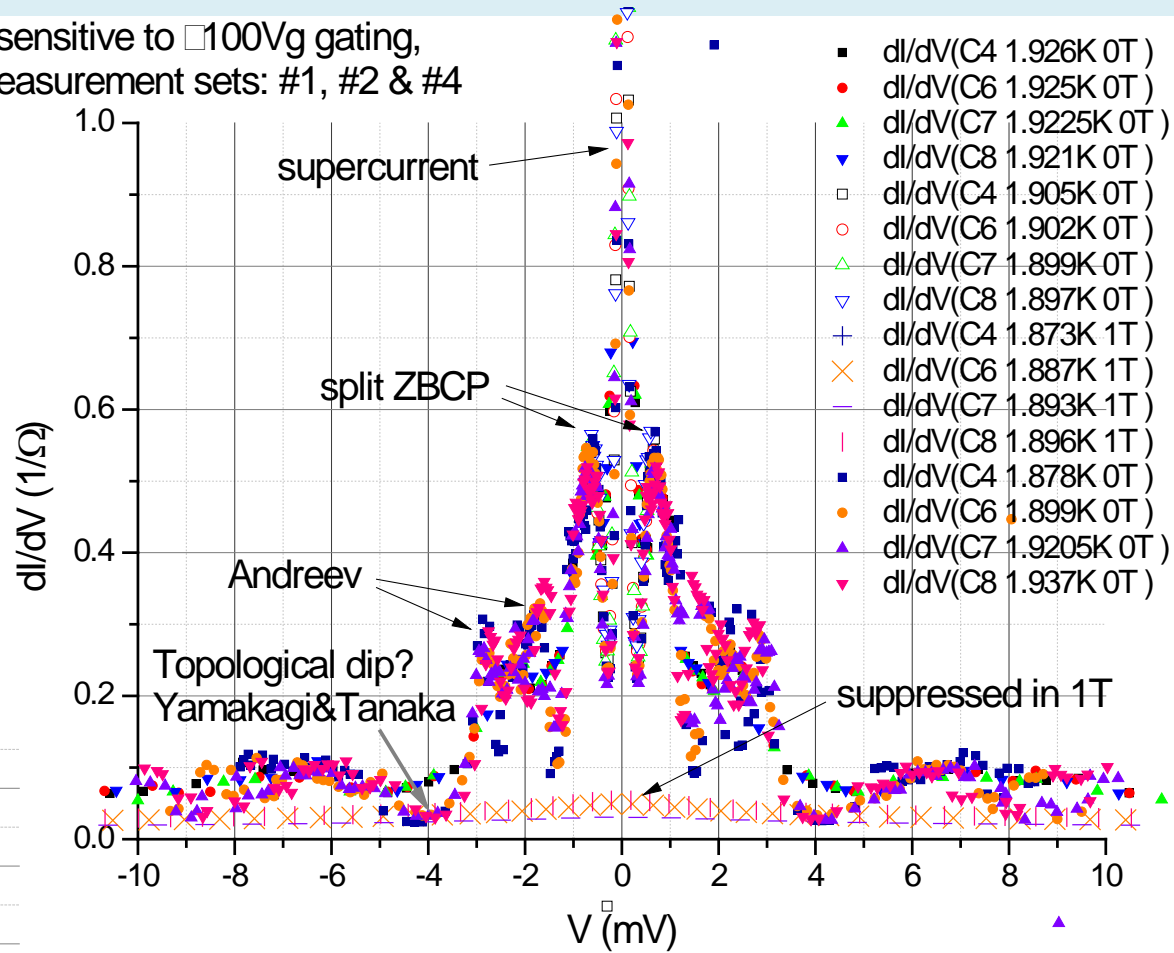


(2) dI/dV & IVC of BL362a (10 nm Bi_2Se_3 on 3nm NbN on FS)

- $V_g=0\text{V}$
- $I_c(1.9\text{K})\sim 1.2\text{ mA}$
(strong links)
- dI/dV is almost fully suppressed at 1T



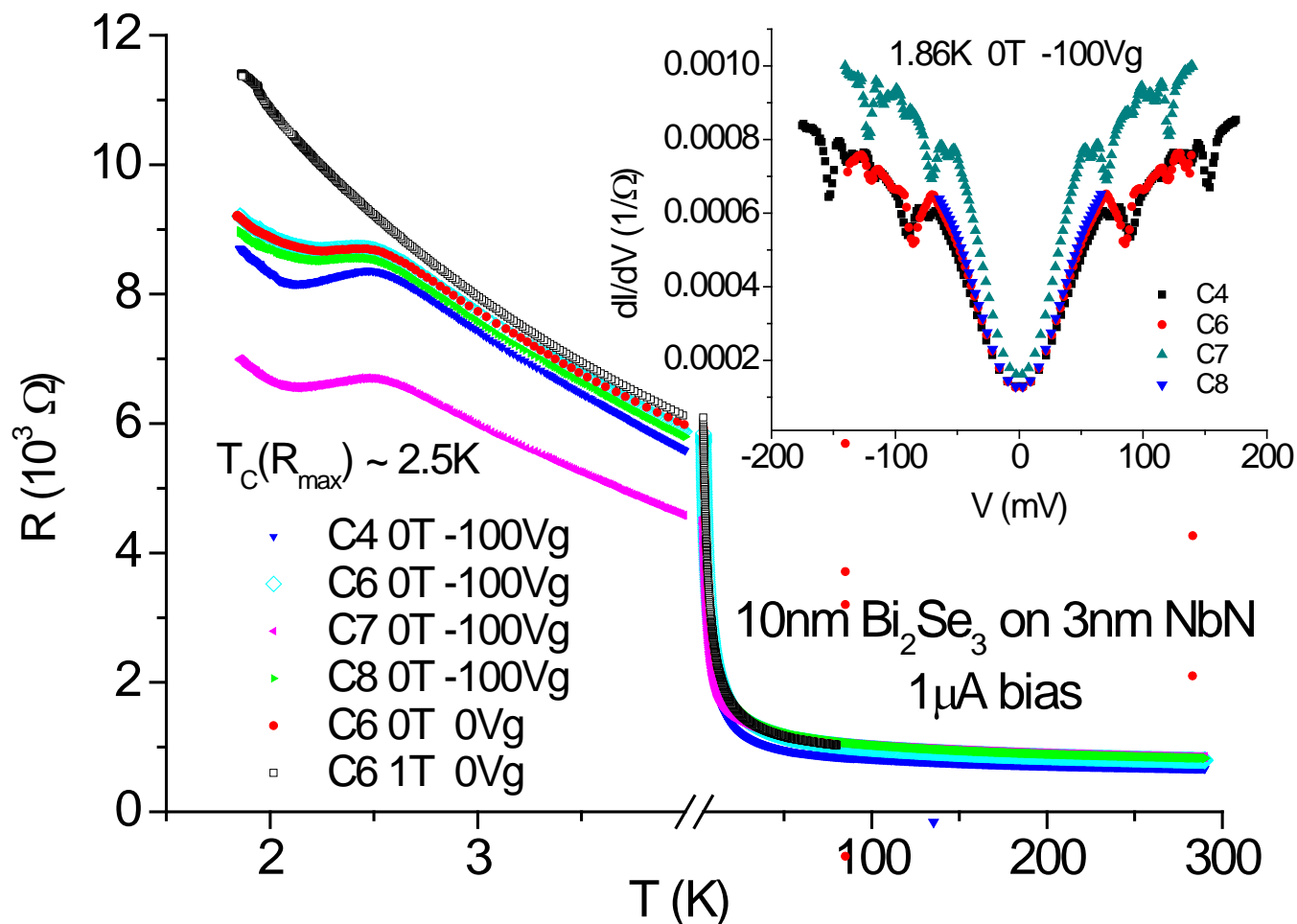
Insensitive to $\square 100\text{V}_g$ gating,
Measurement sets: #1, #2 & #4



- Monotonous decreasing MR vs temperature (not shown)

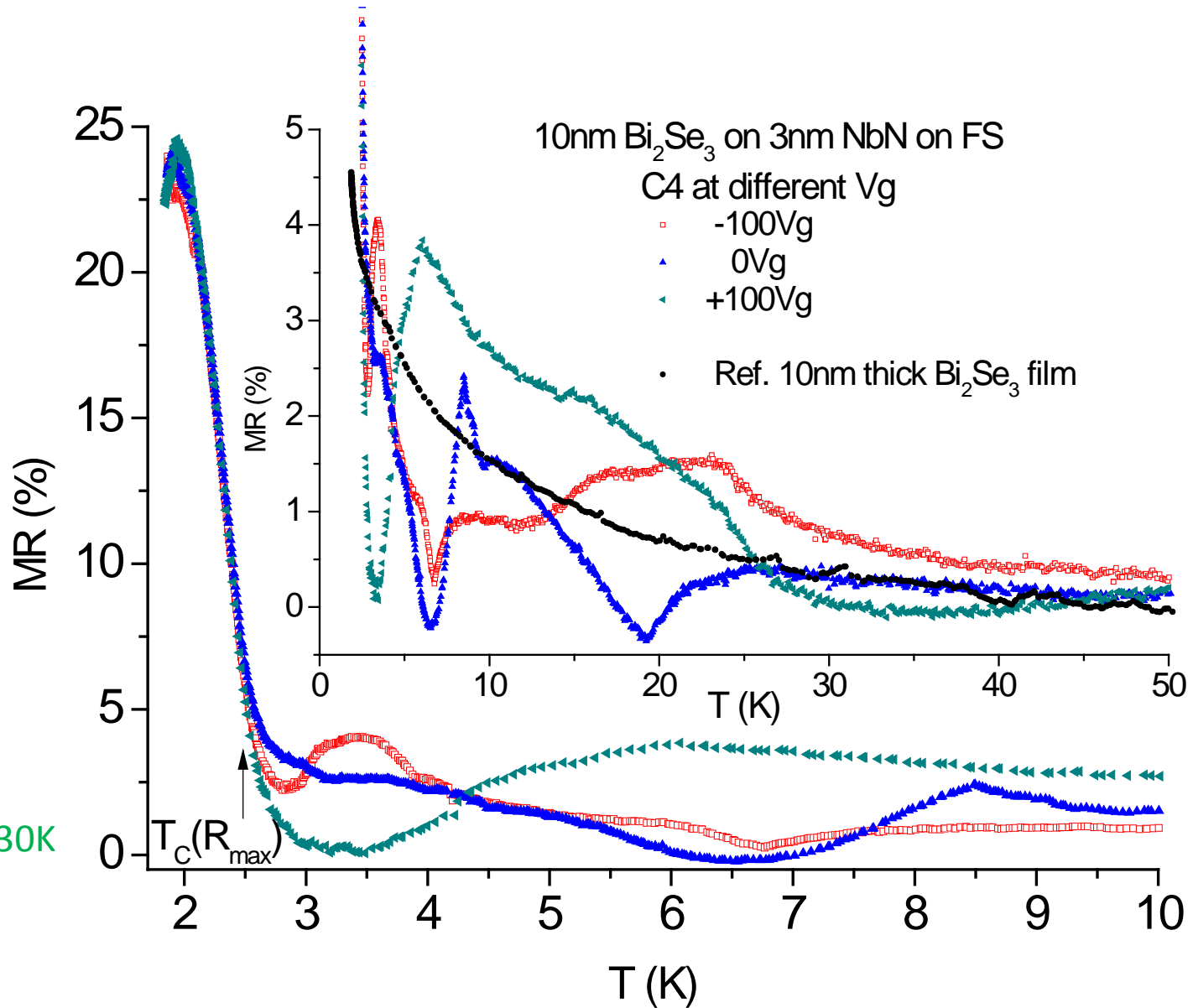
(1) R vs T of another bilayer of 10 nm Bi_2Se_3 on 3nm NbN on fused silica [highest resistance, some air in NbN deposition?]

- Semiconducting
- Very weak SC suppressed under 1T
- Tunneling between NbN grains



(2) MR of this bilayer of 10 nm Bi_2Se_3 on 3nm NbN on FS

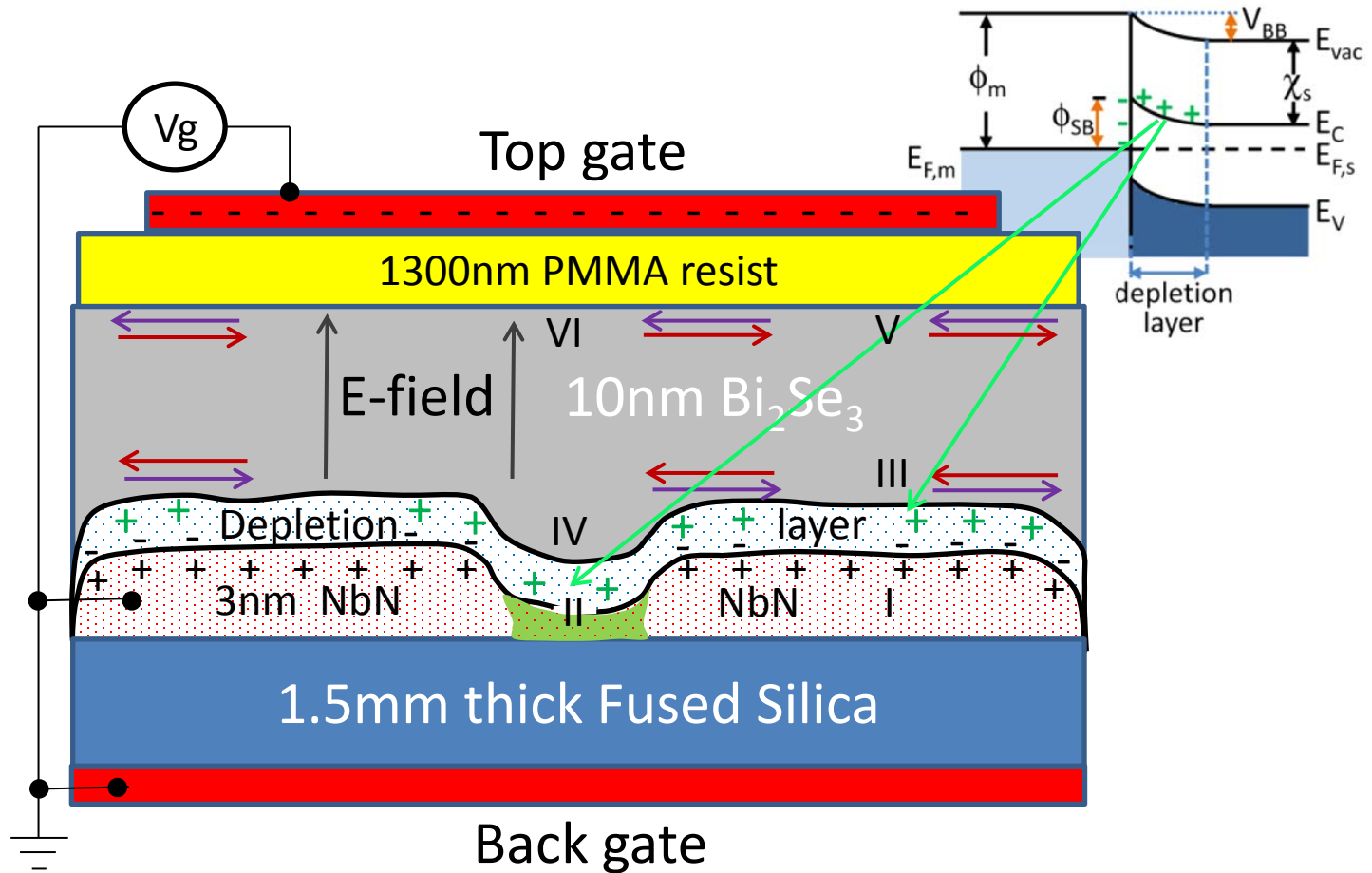
- H is 0&1T for all measurements
- All contacts show the same behavior vs Vg
- Most MR Peaks are due to flux flow \rightarrow Analysis next, on the model cross-section of SC islands & PE regions of the TI cap-layer
- Possible flux flow in a pseudogap at 15-30K
- Possible Majorana contribution at 1.9K



Model: electron density (n) under E-field in the bilayer

- +E-field
[V_g of top gate < 0]
Binds electrons of the Bi_2Se_3 to the NbN surface, leaving a positively charged depletion layer - DL [less n]

- -E-field binds holes, leaving electrons in the DL



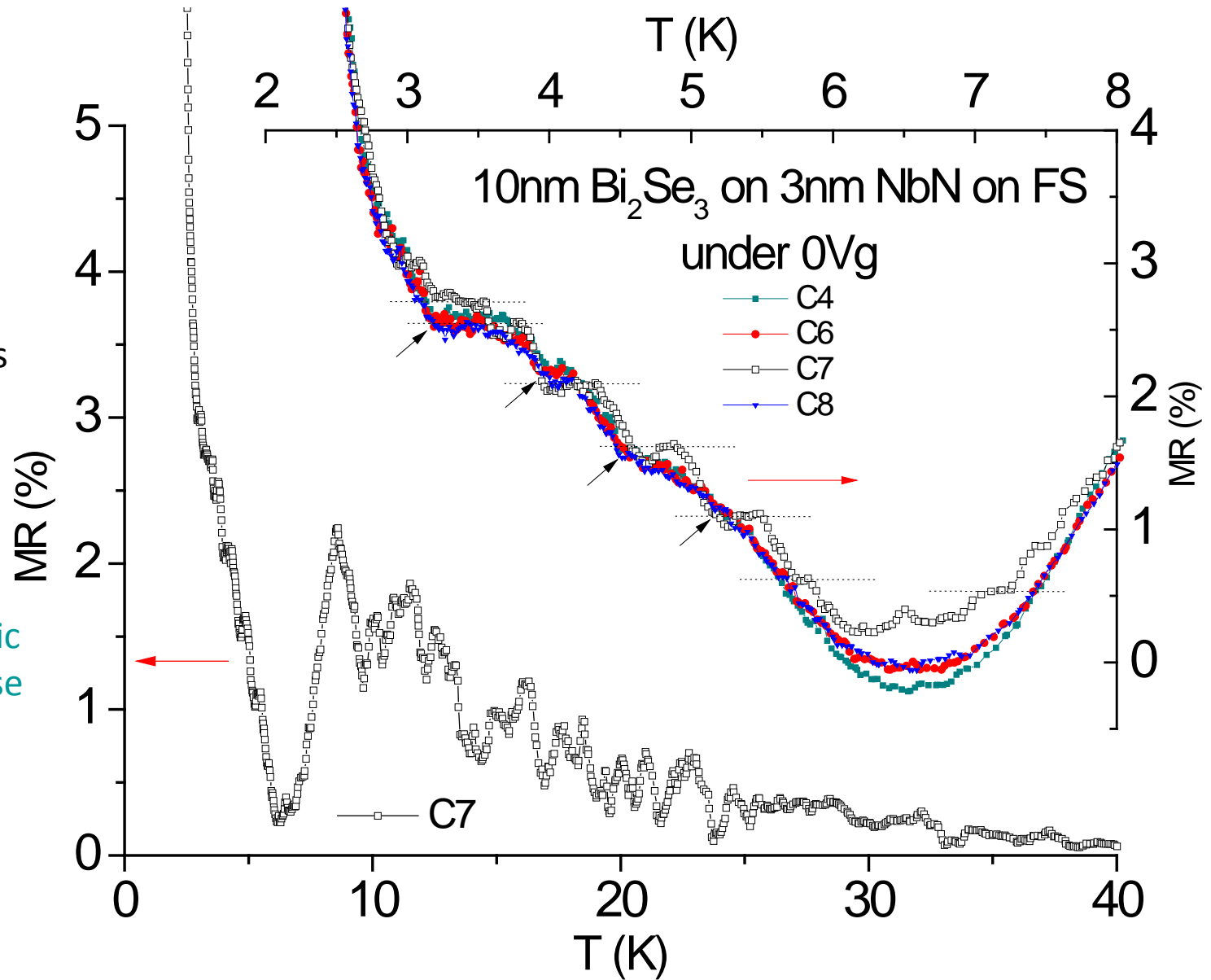
MR peaks analysis:

- For 0Vg: MR peaks at 7-15K, due to NbN islands – regions I, and PE in region III
MR knee at 2.5-6K is due to PE in region II (& IV ?)
Large MR peak below 2.5 K can be due to enhanced PR in region IV or to other effects
- For -100Vg: MR peak at 3-4K originates in the -e depleted region II
- For +100Vg: Broad MR peak at 6K originates in -e rich region II

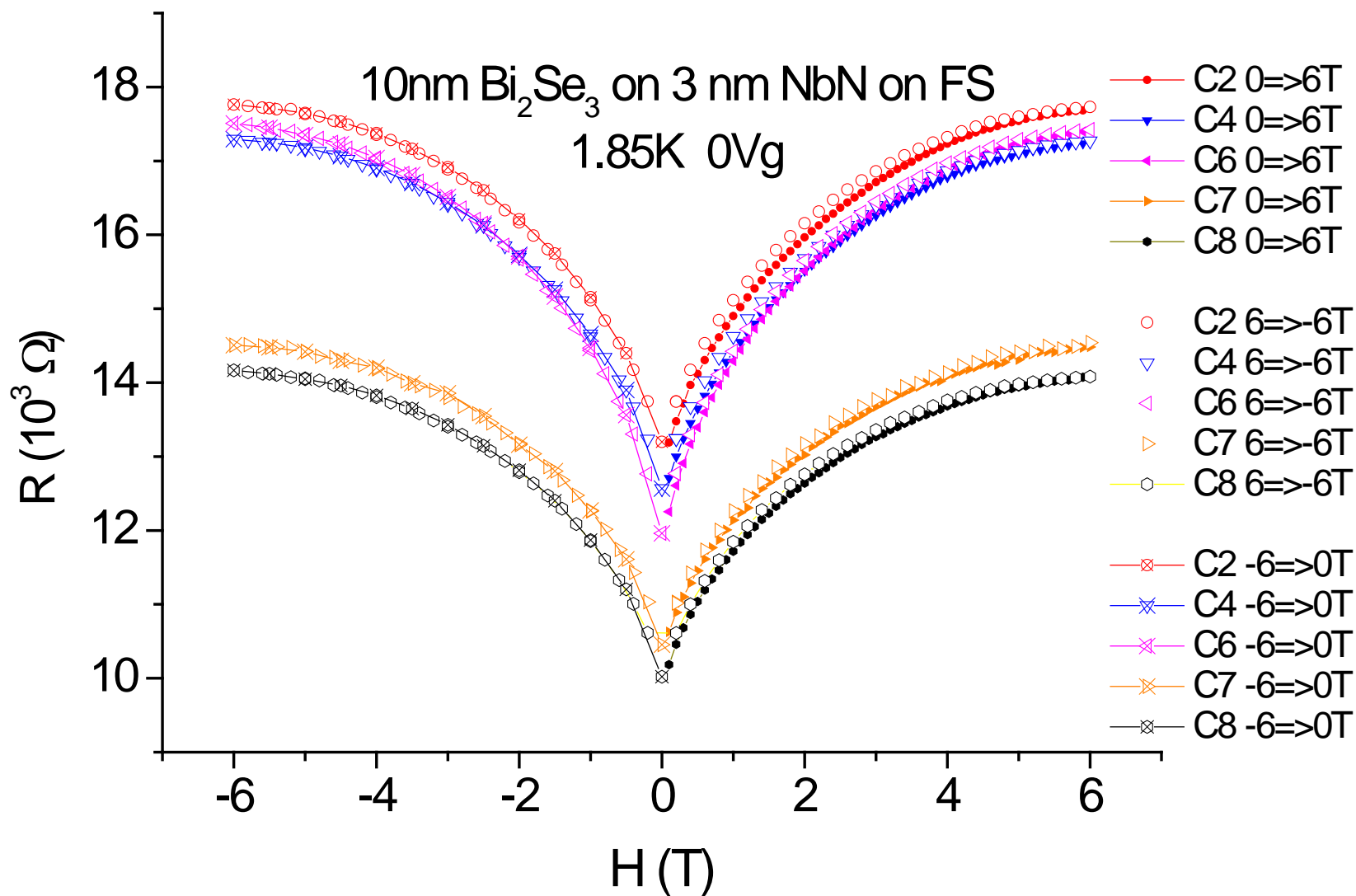
(3) MR of C7 of this 10 nm Bi_2Se_3 on 3 nm NbN on FS bilayer

- Only C7 shows these oscillations under 0Vg
- No oscillations under $\pm 100\text{Vg}$

• Is the magnetic field causing these oscillations?
See next....



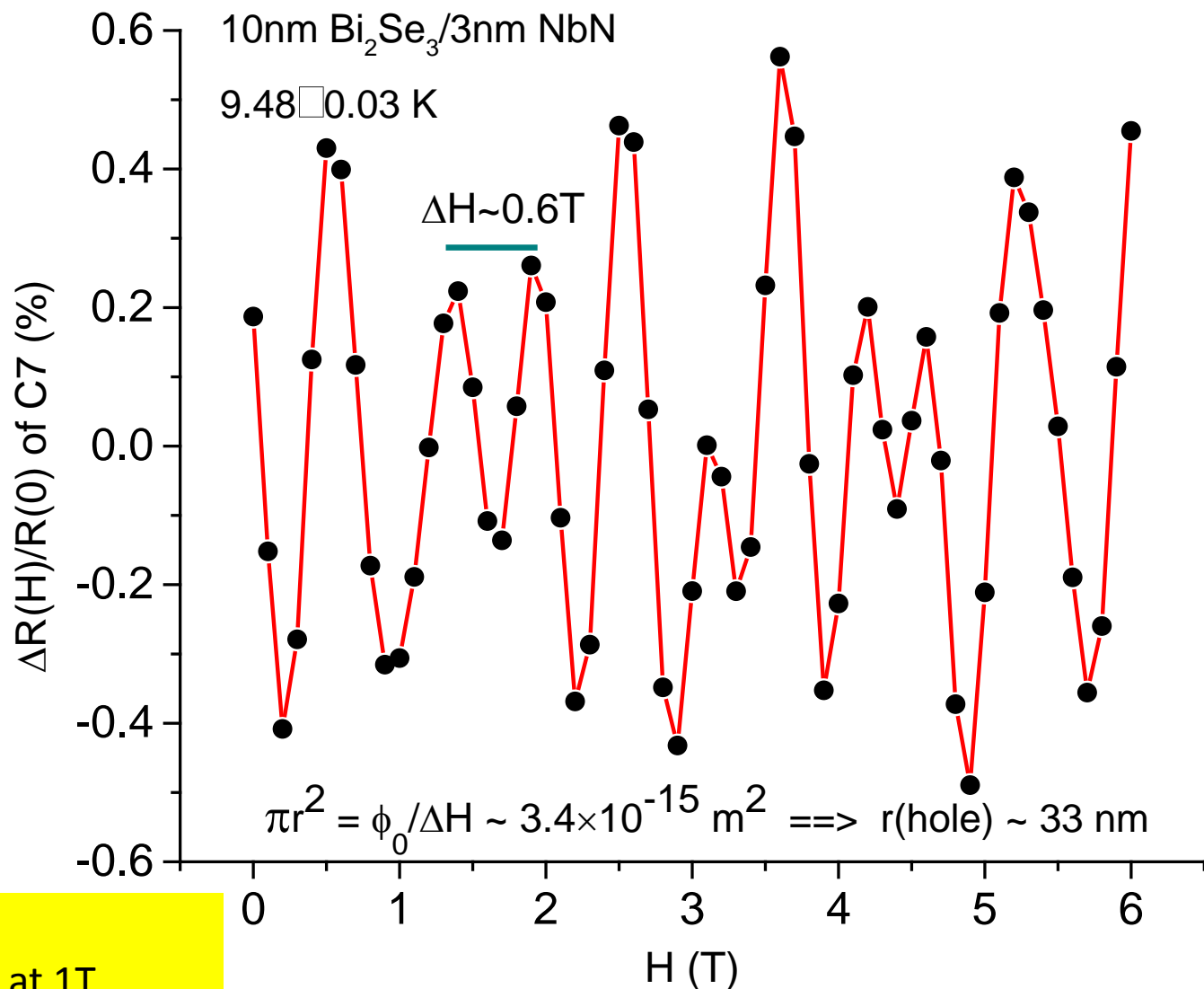
(4) R vs H of this 10 nm Bi_2Se_3 on 3 nm NbN on FS bilayer



No oscillations here, but see next...

(5) $\Delta R/R(0)$ vs H at 9.5K of this bilayer (10 nm Bi_2Se_3 on 3nm NbN)

- $\Delta R(H)$ is $R(H)$ minus a smooth background
- Oscillations vs H with a period of $\Delta H \sim 0.6\text{T}$
adding ϕ_0 for each period of $\Delta H \sim 0.6\text{T}$
- Corresponding to a hole radius of $r \sim 33\text{nm}$
- In agreement with the AFM image
- $T_c(\text{islands}) \geq 10\text{K}$



Similar energy scales:

Magnetic $\sim \mu H \sim 0.06 \text{ meV}$ at 1T

Thermal $\sim kT \sim 0.08 \text{ meV}$ at 1K

$\Delta E(\text{Landau at 1T}) = \hbar \omega_c / 2\pi = 0.12 \text{ meV}$

Conclusions II

- MR & WAL of **10nm Bi₂Se₃ films** were observed in agreement with the literature
- MR of the **10nm Bi₂Se₃ on 3nm NbN bilayers** was:
 1. Strongly dependent on the gate voltage V_g
 2. Varied with the peak resistance at low T
 3. Showed V_g dependent peaks and dips structure
 4. Oscillations vs H at 9.5K are

due to **flux quantization in nano holes**

& indicate **T_c above 10K of the SC islands**

5. MR vs T response is due mostly to **vortex physics & pinning**
6. **Enhanced PE** in the Bi₂Se₃ in between NbN islands at T=1.9 K can be due to: helical surface currents contribution,
or to Majorana zero mode contribution